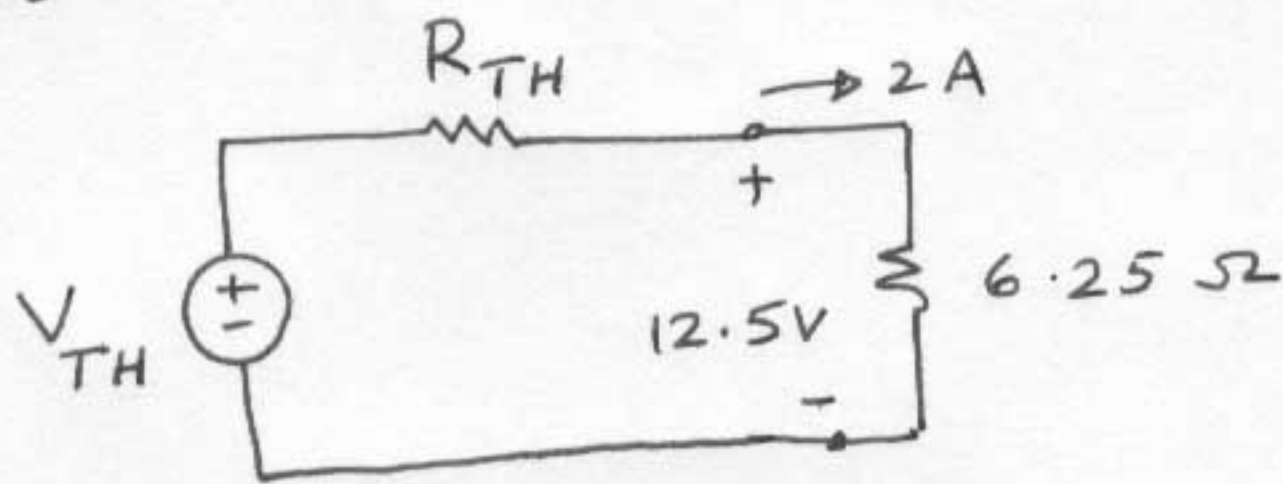
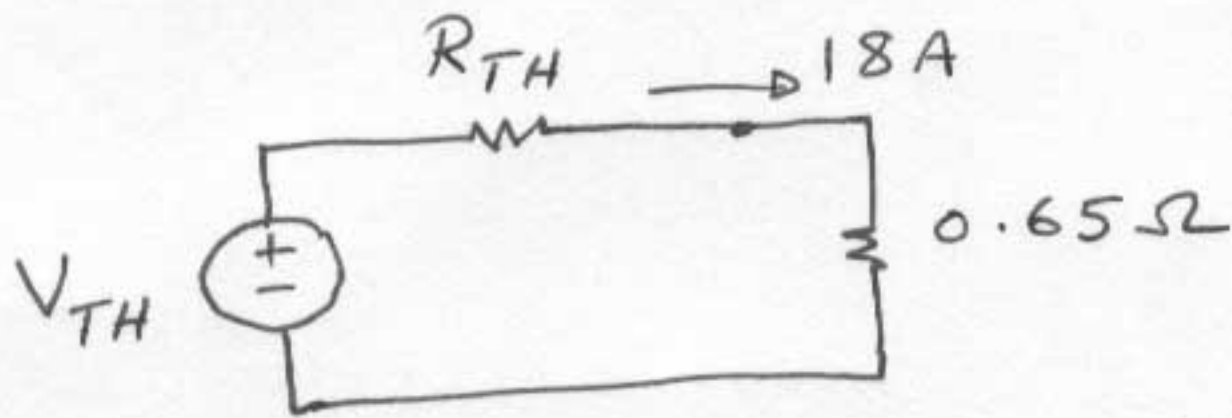


P 4.55



$$12.5 = V_{TH} - 2 R_{TH} \quad (1)$$

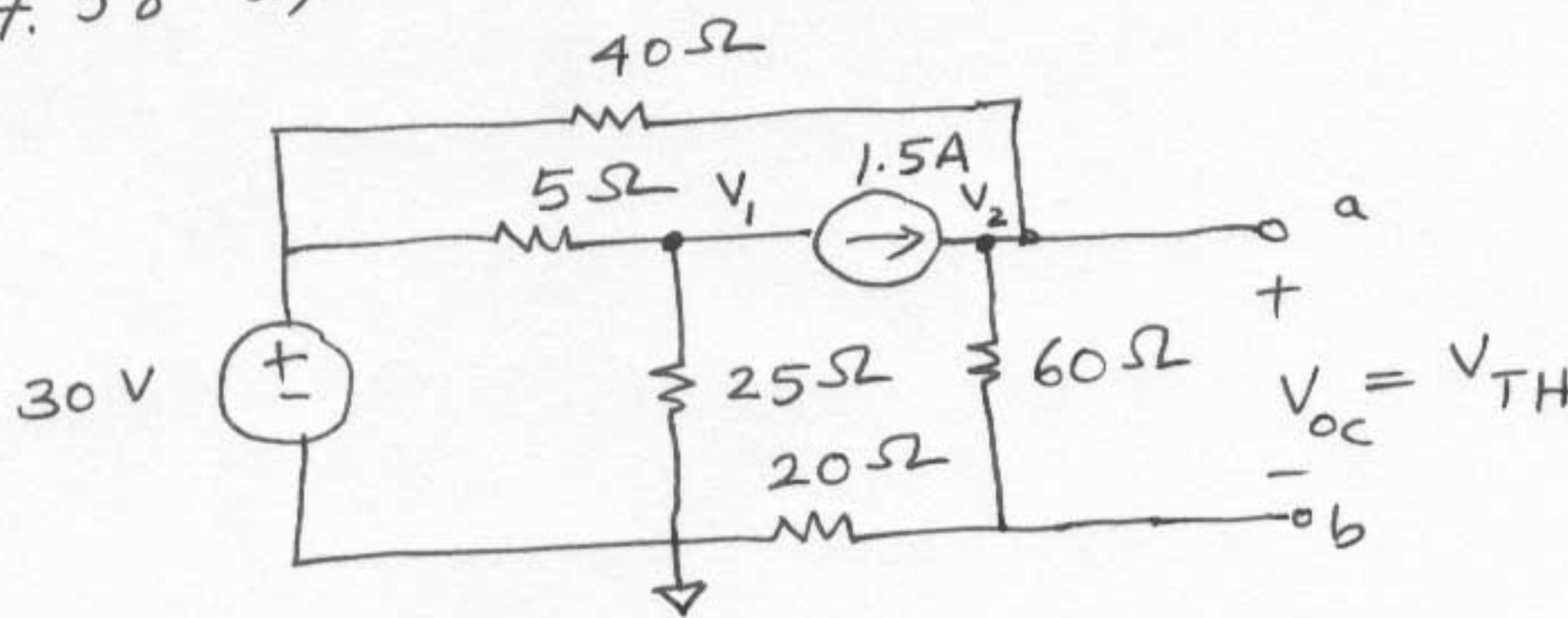


$$11.7 = V_{TH} - 18 R_{TH} \quad (2)$$

Solving (1) & (2)  $\Rightarrow V_{TH} = 12.6 \text{ V}, R_{TH} = 50 \text{ m}\Omega.$

$$\therefore I_N = 252 \text{ A}, R_N = 50 \text{ m}\Omega.$$

P 4.58 a)

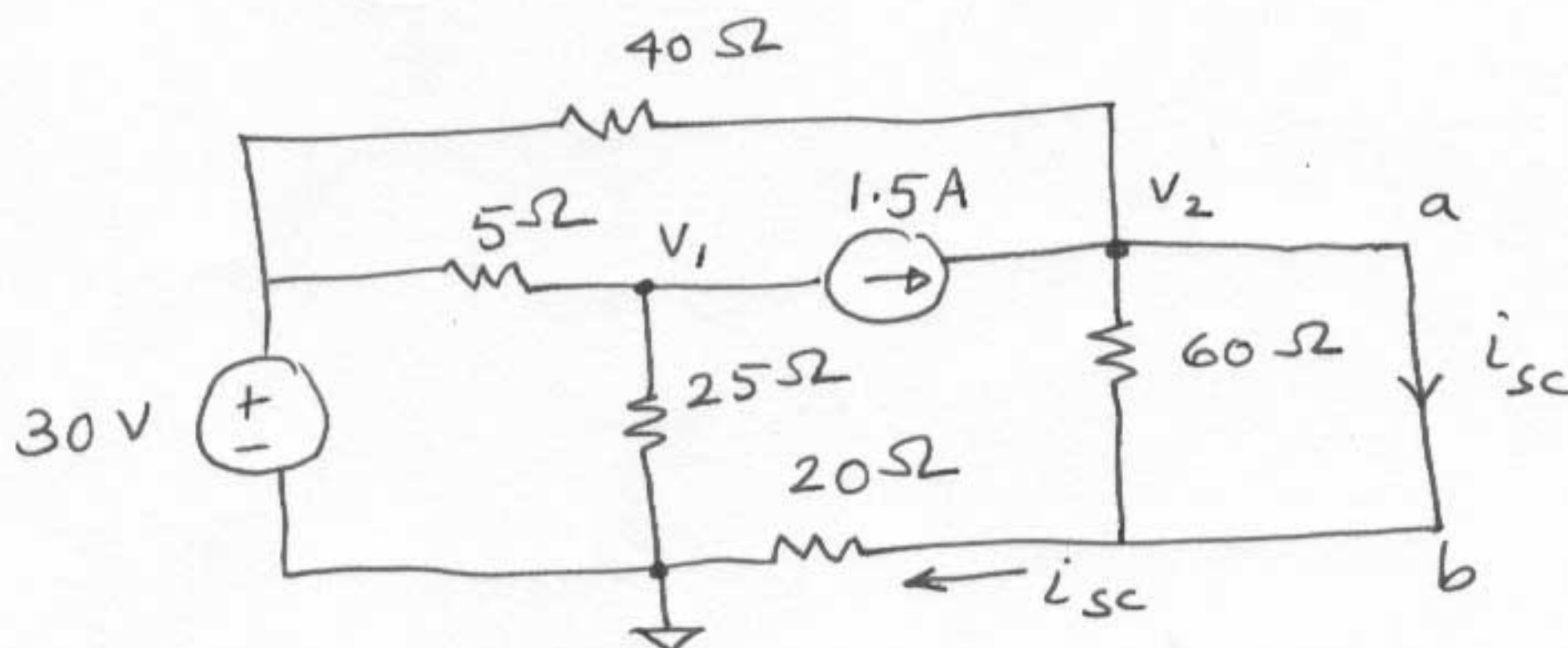


open circuit

$$\frac{V_2}{80} + \frac{V_2 - 30}{40} - 1.5 = 0 \Rightarrow V_2 = 60 \text{ V}$$

But  $V_{oc} = \frac{60}{80} V_2$  (VDR)

$$\therefore V_{oc} = V_{TH} = 45 \text{ V}$$

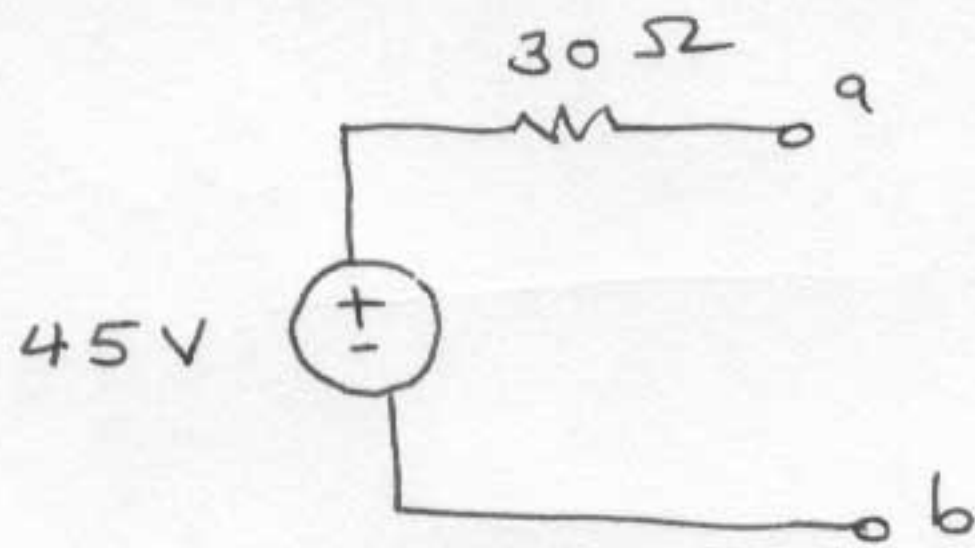


Short Circuit

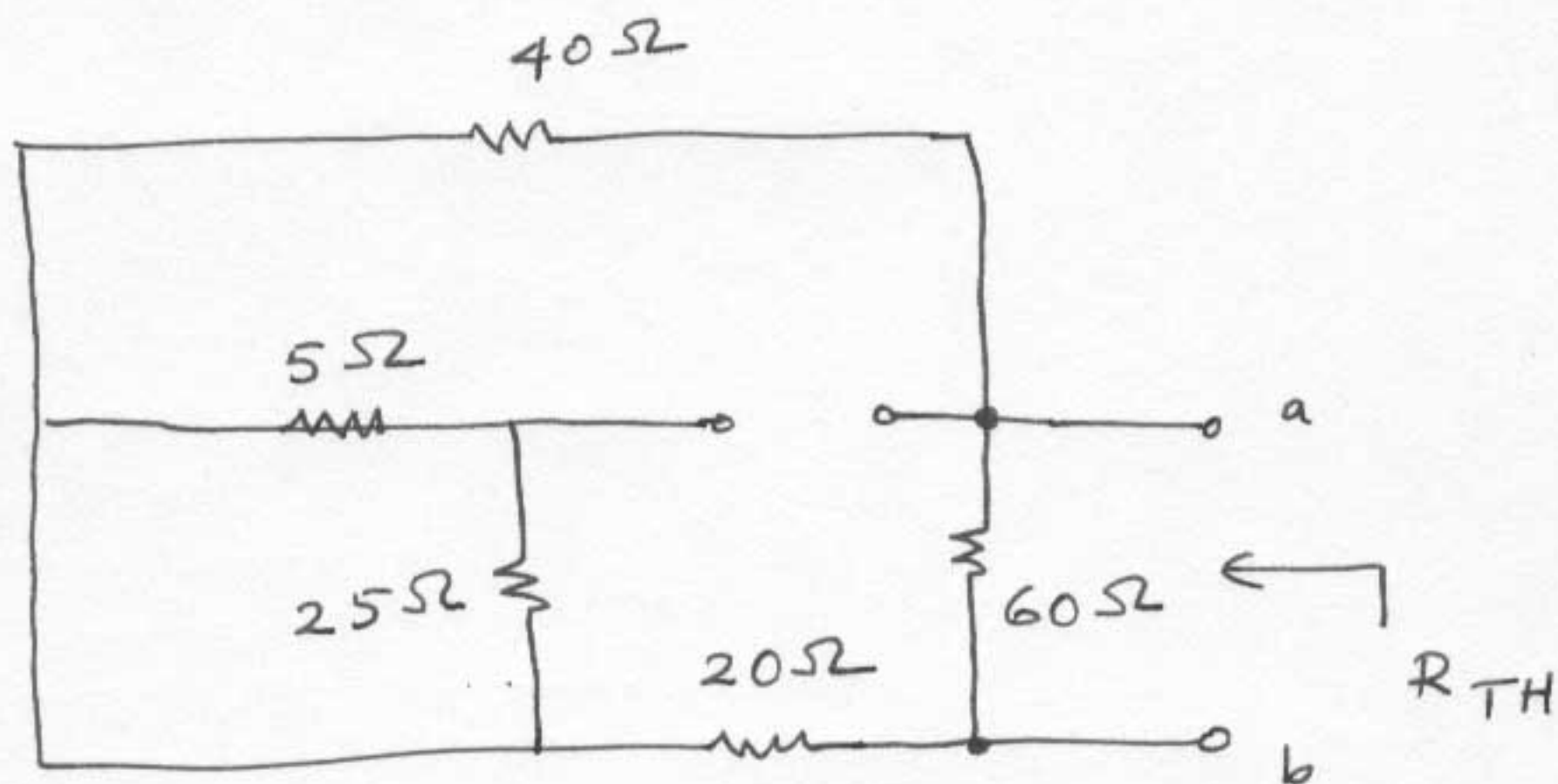
$$\therefore \frac{V_2 - 30}{40} - 1.5 + \frac{V_2}{20} = 0, \therefore V_2 = 30 \text{ V}, I_{sc} = \frac{V_2}{20} = 1.5 \text{ A}$$

$$R_{TH} = \frac{V_{oc}}{I_{sc}} = \frac{45}{1.5} = 30 \Omega$$

The Thevenin equivalent circuit is:

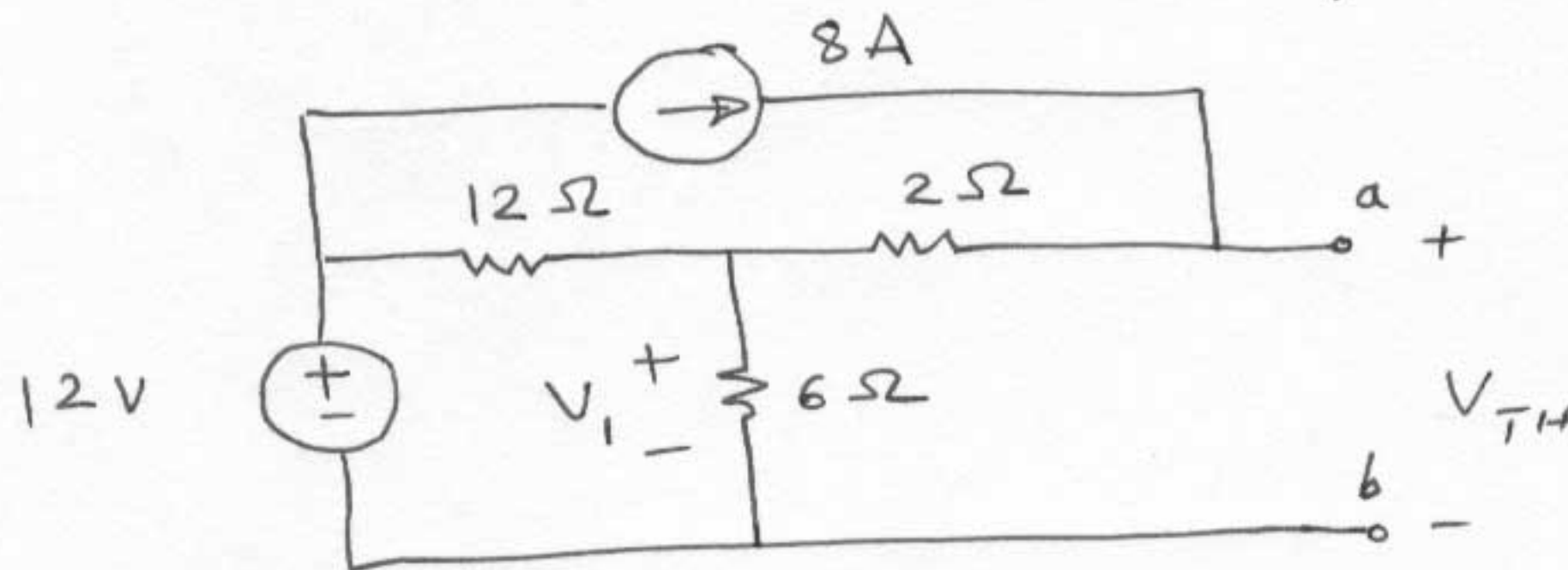


b) Find  $R_{TH}$  directly, set all independent sources to zero:



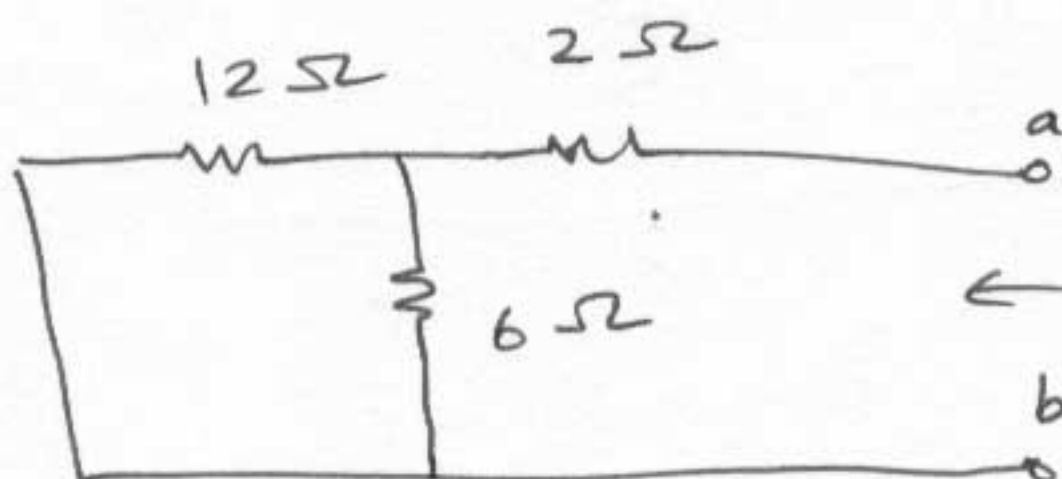
$$R_{TH} = (20 + 40) // 60 = 30 \Omega \text{ (checks).}$$

P4.59

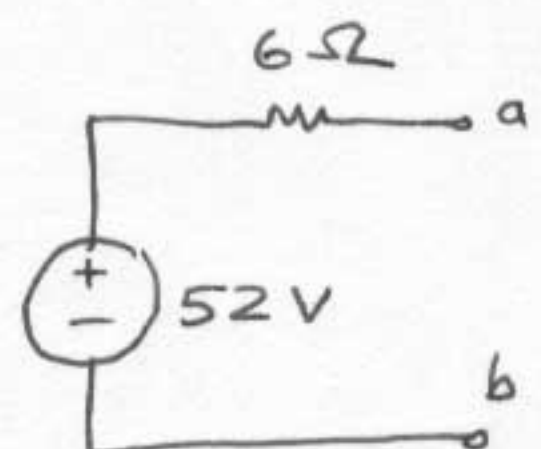


$$\frac{V_1 - 12}{12} + \frac{V_1}{6} - 8 = 0$$

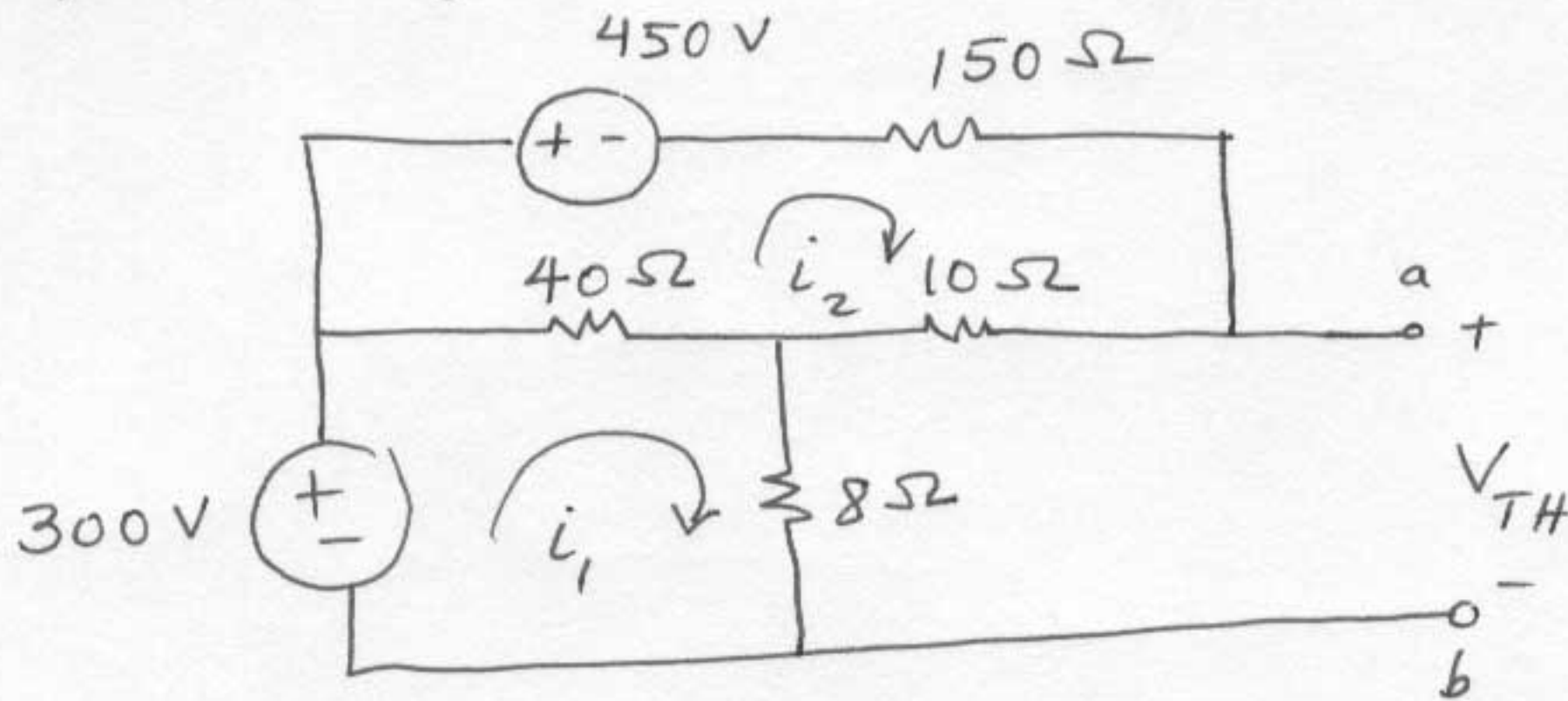
$$\therefore V_1 = 36 \text{ V}, \quad V_{TH} = V_1 + 8(2) = 52 \text{ V}$$



$$R_{TH} = 2 + 12 // 6 = 2 + \frac{12(6)}{12+6} = 6 \Omega$$

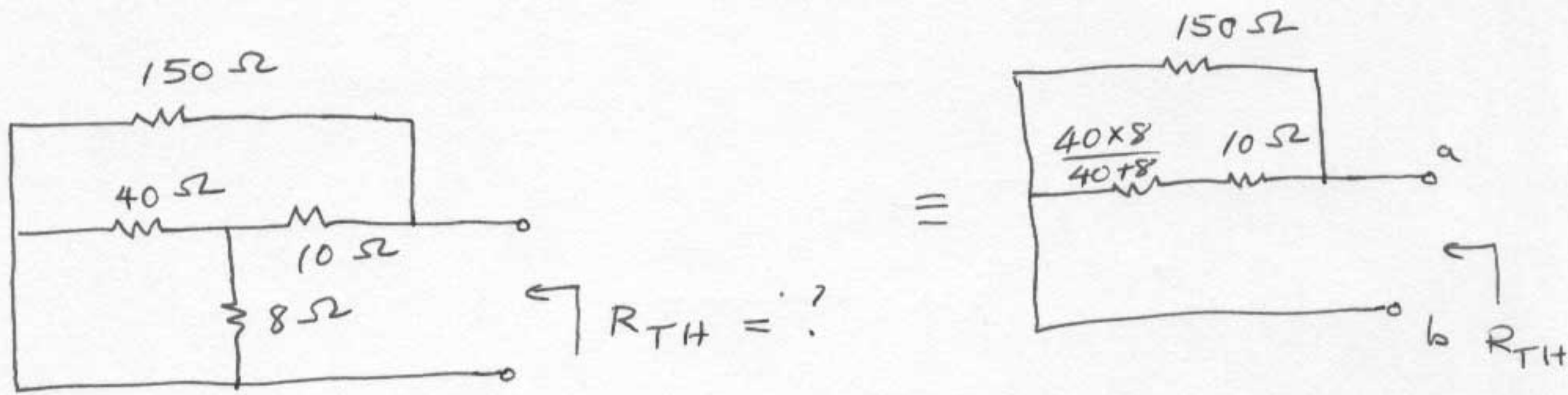


After using source transformation, we have:



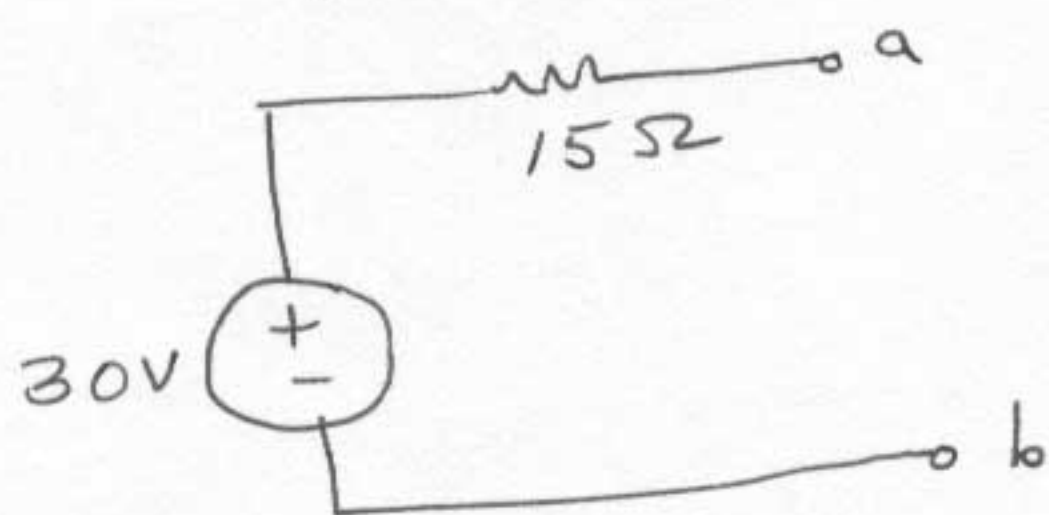
$$\begin{cases} 300 = 48i_1 - 40i_2 \\ -450 = -40i_1 + 200i_2 \end{cases} \therefore i_1 = 5.25A, i_2 = -1.2A$$

$$V_{TH} = 8i_1 + 10i_2 = 30V$$

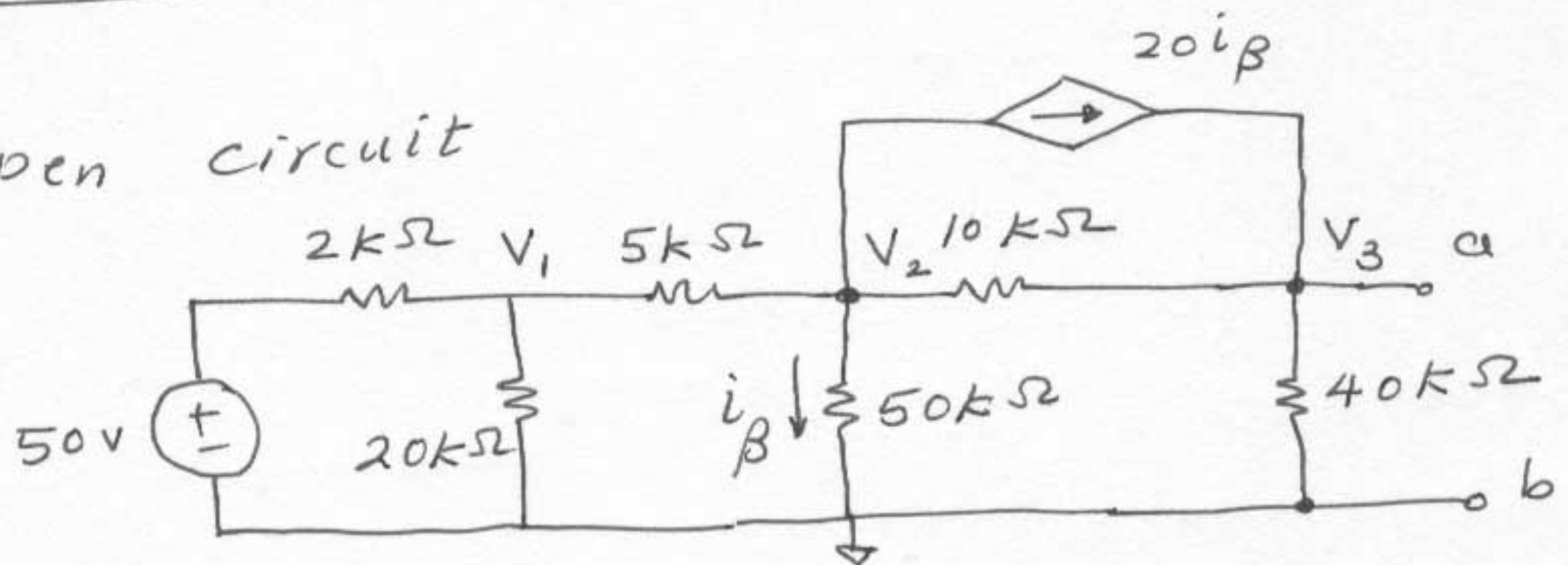


$$\therefore R_{TH} = \left( \frac{40}{6} + 10 \right) \parallel 150 = \frac{\frac{100}{6} \times 150}{\frac{100}{6} + 150} = \frac{15000}{1000} = 15\Omega$$

Thevenin equivalent:



Open circuit



$$\frac{V_1 - 50}{2} + \frac{V_1}{20} + \frac{V_1 - V_2}{5} = 0$$

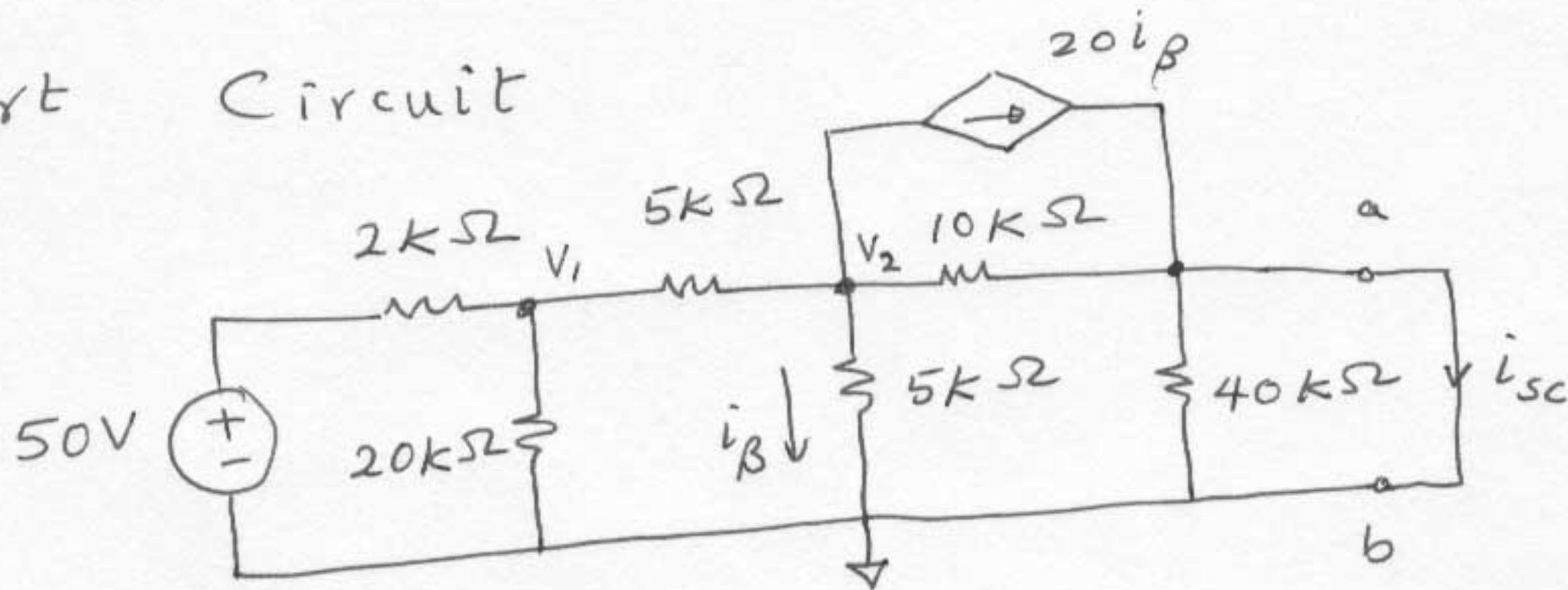
$$\frac{V_2 - V_1}{5} + \frac{V_2}{50} + \frac{V_2 - V_3}{10} + 20 \left( \frac{V_2}{50} \right) = 0$$

$$\frac{V_3}{40} + \frac{V_3 - V_2}{10} - 20 \left( \frac{V_2}{50} \right) = 0$$

solving  $\Rightarrow$

$$V_3 = V_{TH} = 100 \text{ V}$$

Short Circuit



$$\frac{V_1}{20} + \frac{V_1 - 50}{2} + \frac{V_1 - V_2}{5} = 0$$

$$\frac{V_2 - V_1}{5} + \frac{V_2}{50} + \frac{V_2}{10} + 20 \left( \frac{V_2}{50} \right) = 0$$

solving  $\Rightarrow$

$$V_2 = 10 \text{ V}$$

$$\therefore i_{sc} = \frac{20(10)}{50} + \frac{10}{10} = 4 + 1 = 5 \text{ mA}$$

$$\therefore R_{TH} = \frac{V_{TH}}{i_{sc}} = \frac{100}{5 \text{ mA}} = 20 \Omega \times 1000 = 20 \text{ k}\Omega$$

