# KING FAHD UNIVERSITY OF PETROLEUM & MINERALS ELECTRICAL ENGINEERING DEPARTMENT EE 306 – Term 171 HW # 5: Synchronous Machines Due Date: UT Classes: December 10, 2017 MW Classes: December 11, 2017

## Problem 1

A 9 kVA, 208 V, 1200 rpm, three phase, 60 Hz, Y-connected synchronous generator has a field winding resistance of 4.5  $\Omega$  and armature winding impedance of 0.3+j5 $\Omega$  per phase. When the generator operates at its full load and 0.8 PF lagging, the field winding current is 5 A. The rotational loss is 500 W. Determine:

- (a) The voltage regulation
- (b) Efficiency
- (c) The torque applied by the prime mover

## Problem 2

A three phase, 14 kV, 10 MVA, 60 Hz, two pole, 0.85 PF lagging, star connected, synchronous generator has  $X_s=20 \Omega$  per phase and  $R_a=2 \Omega$  per phase. The generator is connected to an infinite bus.

- (a) Determine the excitation voltage at the rated condition. Draw the phasor diagram for this condition.
- (b) Determine the torque angle at the rated condition.
- (c) If the field current is kept constant, determine the maximum power the generator can supply. Neglect R<sub>a</sub>.
- (d) For the condition in part (c), determine the generator current and the power factor. Draw the phasor diagram for this condition.

# **Problem 3**

A three phase, 120 MVA, 12 kV, 60 Hz, two pole, 0.85 PF lagging, Y-connected steam turbine driven alternator(synchronous generator) has a stator resistance of  $R_a$ = 0.018  $\Omega$  and a synchronous reactance of  $X_s$ = 1.02  $\Omega$ . At full load (rated) condition, the efficiency is 92% (the field winding loss is neglected). At this condition, determine

- (a) The synchronous speed
- (b) The power loss in the armature resistance
- (c) The rotational loss
- (d) The torque applied to the shaft by the steam turbine prime mover

# Problem 4

A 208-V Y-connected synchronous motor is drawing 40 A at unity power factor from a 208-V power system. The field current flowing under these conditions is 2.7 A. Its synchronous reactance is  $0.8 \Omega$ . Assume a linear open-circuit characteristic.

(*a*) Find the torque angle  $\delta$ .

(b) How much field current would be required to make the motor operate at 0.8 PF leading?

(c) What is the new torque angle in part (b)?

### Problem 5

A 480-V, 100-kW, 50-Hz, four-pole, Y-connected synchronous motor has a rated power factor of 0.85 leading. At full load, the efficiency is 91%. The armature resistance is 0.08  $\Omega$ , and the synchronous reactance is 1.0  $\Omega$ . Find the following quantities for this machine when it is operating at full load:

- (a) Output torque
- (b) Input power
- (c)  $n_m$  (Mechanical speed of the machine)
- (d)  $E_A$

- (e)  $|I_A|$
- (f)  $P_{conv}$
- (g) Rotational loss=  $P_{mech} + P_{core} + P_{stray}$