

**KING FAHD UNIVERSITY OF PETROLEUM & MINERALS**

**ELECTRICAL ENGINEERING DEPARTMENT**

**EE 201\_102**

**EXAM II**

**DATE: Saturday April 30, 2011**

**TIME: 7:00 PM-8:30 PM**

<b>SER#</b>	<b>Key Solution</b>
<b>ID#</b>	
<b>Name</b>	
<b>Section#</b>	

Course Instructors:

- Dr. Jamil Bakhashwain
- Dr. Adil Balghonaim
- Dr. Zaki Al-Akhdhar
- Dr. Mohammad Sharawi
- Dr. Abdallah Al-Ahmari

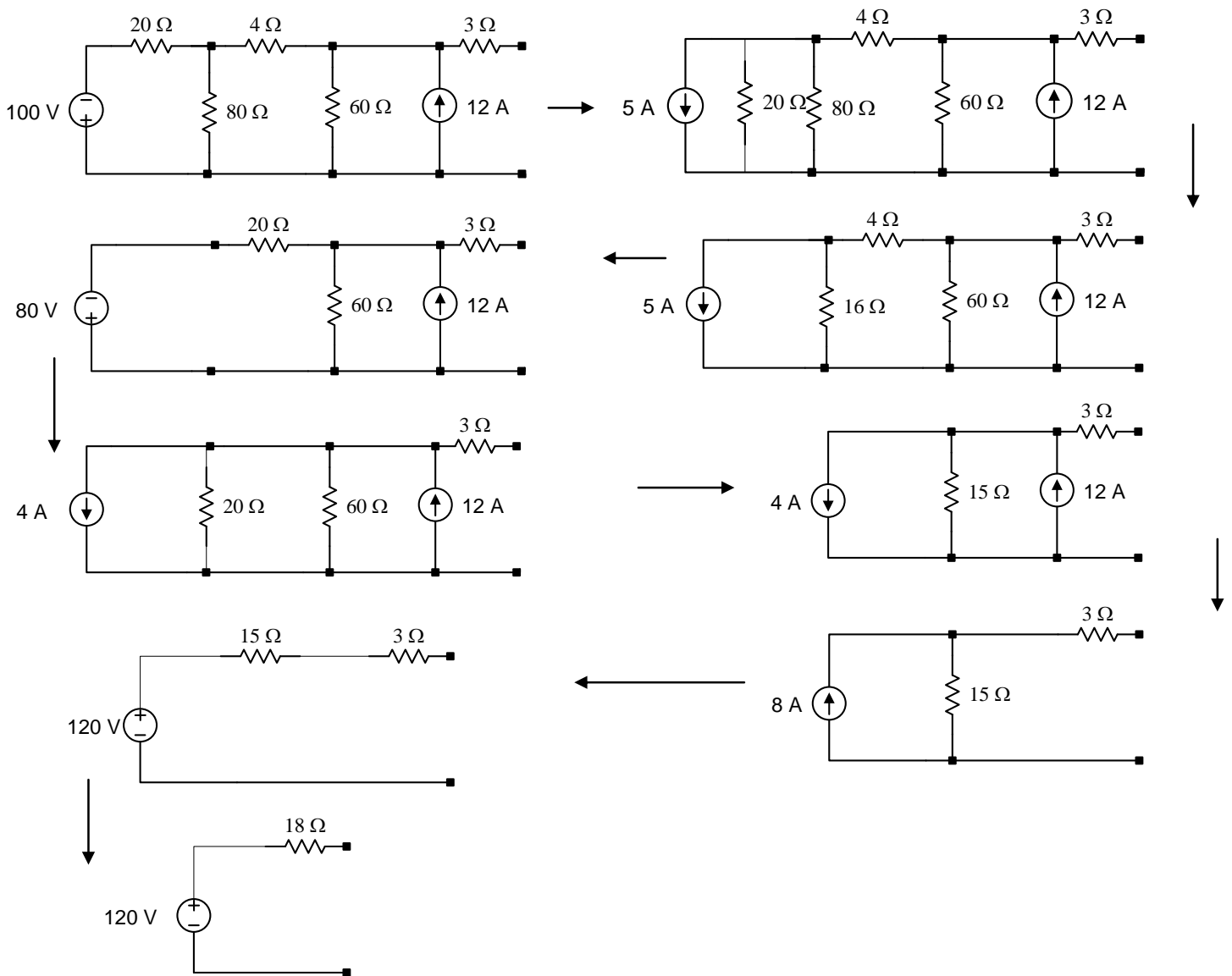
	<b>Maximum Score</b>	<b>Score</b>
<b>Q1</b>	<b>25</b>	
<b>Q2</b>	<b>25</b>	
<b>Q3</b>	<b>25</b>	
<b>Q4</b>	<b>25</b>	
<b>TOTAL</b>	<b>100</b>	

# Q1

- Apply as many as possible of source transformations to reduce the circuit connected between terminal *ab* to its equivalent Thevenin's.
- Calculate the value of  $R_L$  that absorbs maximum power in the circuit when connected to terminals *ab*.
- Calculate the power absorbed by  $R_L$  if it is selected to be  $12\ \Omega$ .

## Solution:

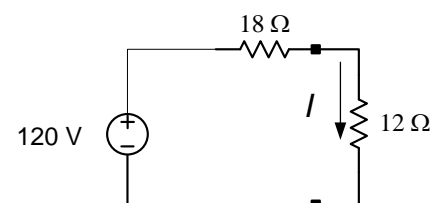
a)



b) For maximum power transfer  $R_L = 18\ \Omega$

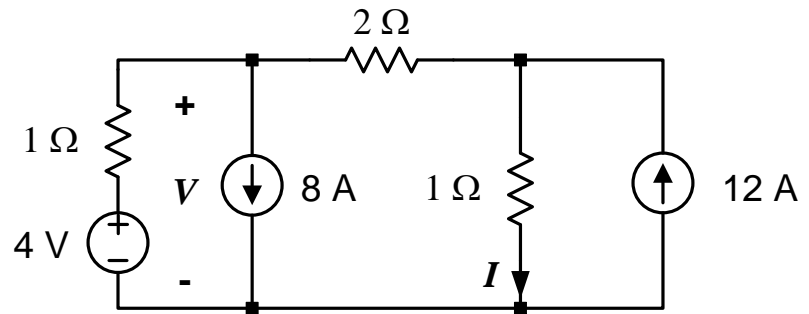
c) From the circuit  $I = 120 / (18 + 12) = 4\ \text{A}$

$$P_{12\Omega} = 12(4)^2 = 192\ \text{watts}$$



## Q2

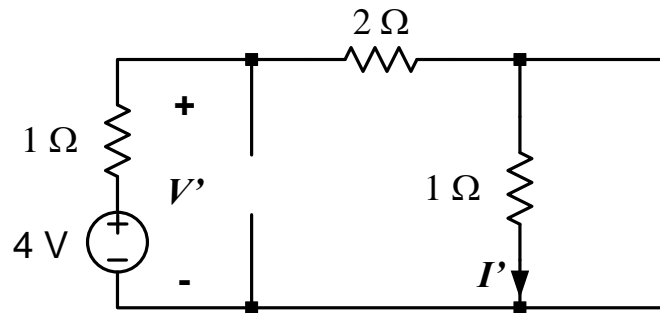
For the circuit shown use the superposition principle to calculate the current  $I$  and the voltage  $V$ . (No points for using any other method)



### Solution:

$$I' = 4/4 = 1\text{ A}$$

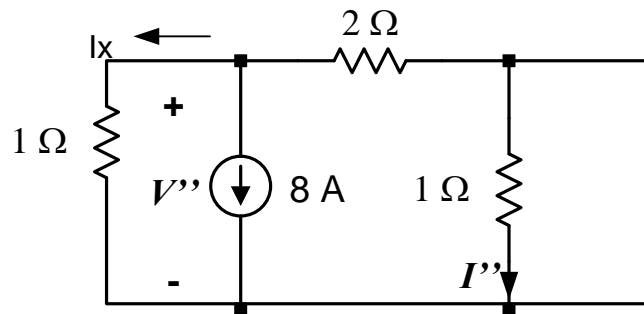
$$V' = 4 - 1(1) = 3\text{ V}$$



$$I'' = -8(1)/4 = -2\text{ A}$$

$$I_x = -8(3)/4 = -6\text{ A}$$

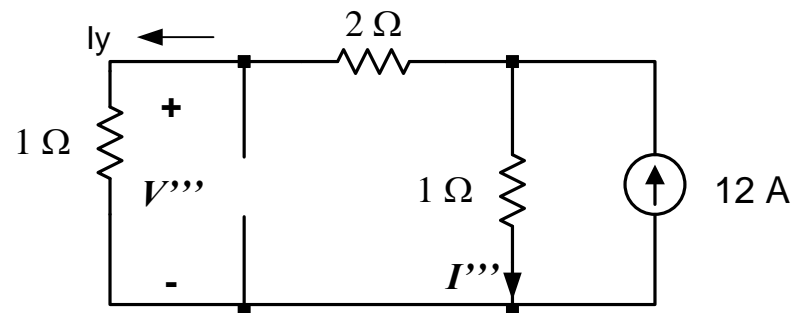
$$V'' = -6(1) = -6\text{ V}$$



$$I''' = 12(3)/4 = 9\text{ A}$$

$$I_y = 12(1)/4 = 3\text{ A}$$

$$V''' = 3(1) = 3\text{ V}$$



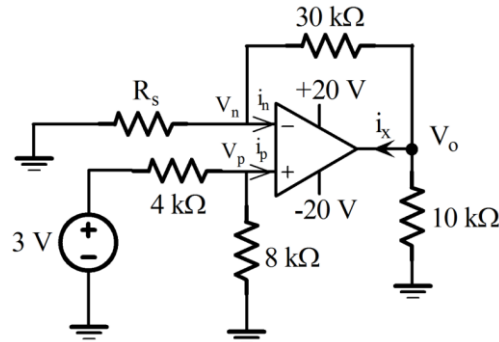
$$I = 1 - 2 + 9 = 8\text{ A}$$

$$V = 3 - 6 + 3 = 0\text{ V}$$

### Q 3:

For the circuit shown below:

- Derive the expression of the voltage  $V_o$  as a function of  $R_s$ .
- If  $R_s = 5 \text{ k}\Omega$ , find the value of  $V_o$  and the current  $i_x$ .
- Find the range of  $R_s$  to avoid the saturation region.



### Solution:

- a) Assuming ideal op-amp and linear region

The current  $i_p = 0$  &  $i_n = 0 \text{ A}$ ,

Also  $V_p - V_n = 0 \rightarrow V_n = V_p$

Apply VDR in the  $8 \text{ k}\Omega$  resistor or apply KVL at the loop of  $3\text{V}$ ,  $4\text{k Ohms}$ , &  $8 \text{ KOhms}$  to get:  
 $V_p = 8k/(8k+4k) * 3 = 2 \text{ V}$

Going back to our assumption  $V_p - V_n = 0 \rightarrow V_n = 2 \text{ V}$ .

Applying KCL at node n:

$$\frac{V_n}{R_s} + \frac{V_n - V_o}{30k} = 0$$

Multiply with  $30k$

$$V_o = V_n \left( \frac{30k}{R_s} + 1 \right) = 2 \left( \frac{30k}{R_s} + 1 \right) = 2 + \frac{60k}{R_s}$$

- b) If  $R_s = 5 \text{ k}\Omega$  then

$$V_o = 2 \left( \frac{30k}{5k} + 1 \right) = 2(6+1) = 14 \text{ V}$$

$$i_x + \frac{V_o}{10k} + \frac{V_o - V_n}{30k} = 0$$

$$i_x = - \left( \frac{V_o}{10k} + \frac{V_o - V_n}{30k} \right) = - \left( \frac{14}{10k} + \frac{14-2}{30k} \right) = -1.8 \text{ mA}$$

- c) The range of  $R_s$  to avoid saturation region

$$-20 \leq V_o \leq 20$$

$$-20 \leq \left( \frac{60k}{R_s} + 2 \right) \leq 20$$

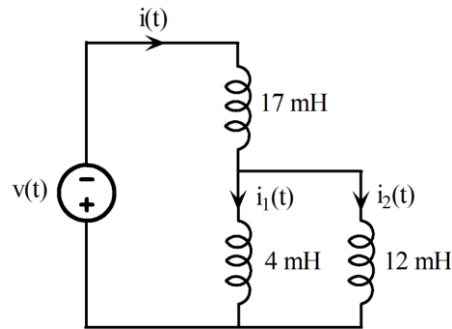
$$-22 \leq \left( \frac{60k}{R_s} \right) \leq 18$$

$$R_s \geq \frac{60k}{18} = \frac{10}{3} \text{ k}\Omega$$

### Q 4:

For the circuit shown below it is given that,  $i_1(0) = 5 \text{ A}$ ,  $i_2(0) = 15 \text{ A}$ , and  $v(t) = 200e^{-500t} \text{ V}$ , for  $t > 0$ .

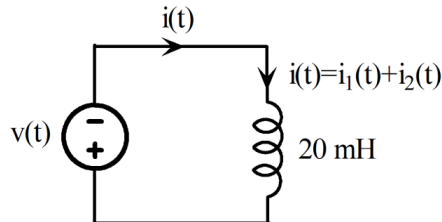
- Find the current  $i(t)$  for  $t \geq 0$ .
- Sketch the current  $i(t)$  for  $t \geq 0$ .



### Solution:

- First of all we combine the three inductors into one inductor in two steps:  
Step 1:  $(4\text{mH} // 12\text{mH}) = 3\text{mH}$   
Step 2:  $L_{\text{eq}} = 17\text{mH} + 3\text{mH} = 20 \text{ mH}$ .

We also use KCL to find  $i(0) = i_1(0) + i_2(0) = 5 \text{ A} + 15 \text{ A} = 20 \text{ A}$ .



Then we have:

$$i(t) = i(0) + \frac{1}{L_{\text{eq}}} \int_0^t \{-v(x)\} dx$$

$$i(t) = 20 + \frac{1}{20\text{m}} \int_0^t \{-200e^{-500x}\} dx$$

$$i(t) = 20 + \frac{200}{(20\text{m})(500)} \left[ e^{-500x} \right]_0^t$$

$$i(t) = 20e^{-500t}, \text{ for } t \geq 0$$

- Sketching of  $i(t)$  for  $t \geq 0$ :

