

## Summary of Discrete Compounding Formulas with Discrete Payments

Flow Type	Factor Notation	Formula	Excel Command	Cash Flow Diagram
S I N G L E	Compound amount ( $F/P, i, N$ )	$F = P(1 + i)^N$	= FV( $i, N, P, , 0$ )	
	Present worth ( $P/F, i, N$ )	$P = F(1 + i)^{-N}$	= PV( $i, N, F, , 0$ )	
E Q U A L  P A Y M E N T  S E R I E S	Compound amount ( $F/A, i, N$ )	$F = A \left[ \frac{(1 + i)^N - 1}{i} \right]$	= FV( $i, N, A, , 0$ )	
	Sinking fund ( $A/F, i, N$ )	$A = F \left[ \frac{i}{(1 + i)^N - 1} \right]$	= PMT( $i, N, P, F, 0$ )	
	Present worth ( $P/A, i, N$ )	$P = A \left[ \frac{(1 + i)^N - 1}{i(1 + i)^N} \right]$	= PV( $i, N, A, , 0$ )	
G R A D I E N T  S E R I E S	Linear gradient  Present worth ( $P/G, i, N$ ) Conversion factor ( $A/G, i, N$ )	$P = G \left[ \frac{(1 + i)^N - iN - 1}{i^2(1 + i)^N} \right]$ $A = G \left[ \frac{(1 + i)^N - iN - 1}{i(1 + i)^N - 1} \right]$		
	Geometric gradient  Present worth ( $P/A_1, g, i, N$ )	$P = \begin{cases} A_1 \left[ \frac{1 - (1 + g)^N(1 + i)^{-N}}{i - g} \right] \\ A_1 \left( \frac{N}{1 + i} \right) \text{ (if } i = g) \end{cases}$		

## Summary of Formulas

### Effective Interest Rate per Payment Period

Discrete compounding  $i = [(1 + r/(CK))^C - 1]$

Continuous compounding  $i = e^{r/K} - 1$

where  $i$  = effective interest rate per payment period

$r$  = nominal interest rate or APR

$C$  = number of interest periods per payment period

$K$  = number of payment periods per year

$r/K$  = nominal interest rate per payment period

### Market Interest Rate

$$i = i' + \bar{f} + i'\bar{f}$$

where  $i$  = market interest rate

$i'$  = inflation-free interest rate

$\bar{f}$  = general inflation rate

### Present Value of Perpetuities

$$P = \frac{A}{i}$$

### Capital Recovery with Return

$$CR(i) = (I - S)(A/P, i, N) + iS$$

### Book Value

$$BV_n = I - \sum_{j=1}^n D_j$$

### Straight-Line Depreciation

$$D_n = \frac{(I - S)}{N}$$

### Declining Balance Depreciation

$$D_n = \alpha I (1 - \alpha)^{n-1}$$

where  $\alpha$  = declining balance rate, and  $0 < \alpha \leq \frac{2}{N}$

### Cost of Equity

$$i_e = r_f + \beta[r_M - r_f]$$

where  $i_e$  = cost of equity

$r_f$  = risk-free interest rate

Modified ACRS Factors				
	Recovery Period (Years)			
Year	3	5	7	10
1	33.33	20.00	14.29	10.00
2	44.45	32.00	24.49	18.00
3	14.81	19.20	17.49	14.44
4	7.41	11.52	12.49	11.52
5		11.52	8.93	9.22
6		5.76	8.92	7.37
7			8.93	6.55
8			4.46	6.55
9				6.55
10				6.56
11				3.28

$\beta$  = market related risk index

$r_M$  = market rate of return

### Cost of Debt

$$i_d = \left(\frac{c_s}{c_d}\right)k_s(1 - t_m) + \left(\frac{c_b}{c_d}\right)k_b(1 - t_m)$$

where  $i_d$  = cost of debt

$c_s$  = the amount of term loan

$c_b$  = the amount of bond financing

$c_d$  = total debt =  $c_s + c_b$

$k_s$  = the before-tax interest rate on the term loan

$k_b$  = the before-tax interest rate on the bond

$t_m$  = the firm's marginal tax rate

### Weighted—Average Cost of Capital

$$k = \frac{i_d c_d}{V} + \frac{i_e c_e}{V}$$

where  $k$  = cost of capital

$c_e$  = total equity capital

$V = c_d + c_e$