

## COE 405, Term 131

### Design & Modeling of Digital Systems

#### HW# 1

**Due date: Sunday, Sep. 29**

- Q.1.** Consider the two functions  $f = a b c + a' b' c'$  and  $g = a b + a' c$ .
- (i) Implement the function  $f$  using a single  $4 \times 1$  MUX.
  - (ii) Compute the complement of  $f$ .
  - (iii) Compute the function  $f \oplus g$  based on orthonormal basis expansion.
- Q.2.** It is required to design a combinational circuit that computes the equation  $Y = 5 * X$ , where  $X$  is an  $n$ -bit unsigned number.
- (i) Design the circuit as a modular circuit where each module receives a single bit of the input,  $X_i$ .
  - (ii) Derive the truth table of your 1-bit module in (i).
  - (iii) Derive minimized two-level sum-of-product equations for your 1-bit module circuit.
  - (iv) Verify the correctness of your design by modeling and simulating a 4-bit circuit using logicworks.
  - (v) Assume that the delay of a gate is related to the number of its inputs, i.e. the delay of an inverter is 1, the delay of a 2-input gate is 2, etc. Compute the maximum propagation delay of your  $n$ -bit circuit.
  - (vi) Verify the correctness of your maximum propagation delay calculation by measuring the longest delay for a 4-bit circuit using logicworks.