

King Fahd University of Petroleum and Minerals
College of Computer Science and Engineering
Computer Engineering Department

COE 301 COMPUTER ORGANIZATION
ICS 233: COMPUTER ARCHITECTURE & ASSEMBLY LANGUAGE
Term 151 (Fall 2015-2016)
Major Exam 2
Saturday Nov. 21, 2015

Time: 120 minutes, Total Pages: 15

Name: _____ **ID:** _____ **Section:** _____

Notes:

- Do not open the exam book until instructed
- Answer all questions
- All steps must be shown
- Any assumptions made must be clearly stated

Question	Max Points	Score
Q1	16	
Q2	20	
Q3	20	
Q4	30	
Total	86	

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[16 Points]**(Q1)**

- (i) **[6 points]** A recursive procedure TH(N) returns $1+2\text{TH}(N-1)$ for $N > 1$, 1 if $N=1$, and zero otherwise. This is called Tower of Hanoi. TH(N) is defined as follows:

```
int TH(int N) {
    if (N <= 0) return 0;
    else if (N=1) return 1;
    else return (1 + 2*TH(N-1));
}
```

Assume TH receives its argument N in register \$a0 and return its results in \$v0. The above procedure is called from some Main program, which needs **not** to be implemented here. Write a minimal MIPS program for the above procedure.

- (ii) **[10 points]** Suppose we enter i integers $q(1), q(2), \dots, q(i)$. The objective is to compute the result $p(i) = q(1) + \dots + q(i)$ for each i , where p is an array of results. A better way to compute the results is $p(i) = p(i-1) + q(i)$ for $i \geq 1$ after setting $p(0) = 0$. The above function is called **prefix sum**. For example, if we enter 4, 3, 5, 2, 3, 0 (termination) as follows:

Order of entries 1 2 3 4 5 6

Value of entries q : 4 3 5 2 3 0 then the results will be:

Value of results p : 4 7 12 14 17

Assume the following strings in the data segments:

prompt-1: .asciiz "Please enter at most 100 signed integers terminating with 0: \n"

prompt-2: .asciiz "Prefix sum of the entered integers: \n"

Use $\$s0$ to store the address of array of words p as a base address and $\$s1$ to store the number of entered integers by the user.

Write a MIPS program with minimal instructions that carries out the following steps:

1. Print "prompt-1",
2. Reads at most 100 signed integers $q(i)$ terminated with a zero,
3. Compute the results $p(i)$ and store them in memory,
4. Print "prompt-2", and
5. Print all the results $p(i)$.

[20 Points]

(Q2)

- (i) **[10 points]** You are required to design a circuit that can be used to perform **signed** multiplication of two 32-bit operands A and B. Show the block diagram of all used components and their sizes. Explain how the circuit will be used to perform signed multiplication by showing a flow chart or pseudo code.

- (ii) [4 points] Given that **Multiplicand=1001** and **Multiplier=1011**, using the **signed multiplication** hardware, show the **signed** multiplication of **Multiplicand** by **Multiplier**. The result of the multiplication should be an 8 bit **signed** number in HI and LO registers. Show the steps of your work.

Iteration		Multiplicand	Sign	Product = HI,LO
0	Initialize			
1				
2				
3				
4				

- (iii) [6 points] Given that **Dividend=1001** and **Divisor=0011** represent two **4-bit signed numbers in 2's complement representation**, using the **unsigned division** hardware, show the **signed** division of **Dividend** by **Divisor**. The result of division should be stored in the Remainder and Quotient registers. Show the steps of your work.

Iteration		Remainder (HI)	Quotient (LO)	Divisor	Difference
0	Initialize				
1					
2					
3					
4					

(Q3)

1. [2 Points] What is the **decimal value** of following single precision float:

[1, 1000 0101, 0101 1101 0000 0000 0000 000]

2. [2 Points] What is the **decimal value** of following single precision float:

[0, 0000 0000, 0100 0000 0000 0000 0000 000]

3. [3 Points] Find the normalized single precision float representation of +59.25.

4. [4 Points] Round the given single precision float with the given GRS bits using the following rounding modes showing the resulting normalized number:

-1.111 1111 1111 1111 1111 1111 1111 ^{GRS} 100 x 2²³

Zero: []

+infinity: []

-infinity: []

Nearest Even: []

5. **[5 Points]** Find the normalized difference between A and B by using rounding to nearest even. Perform the operation using **guard, round** and **sticky** bits:

$$A = + 1.000000000000000000000000 \times 2^4$$

$$B = +1.111100000000000000000001 \times 2^3$$

6. **[4 Points]** Find the normalized result of the operation A+B+C, by performing A+B first followed by adding C, using rounding to nearest even. Perform the operation using **guard, round** and **sticky** bits:

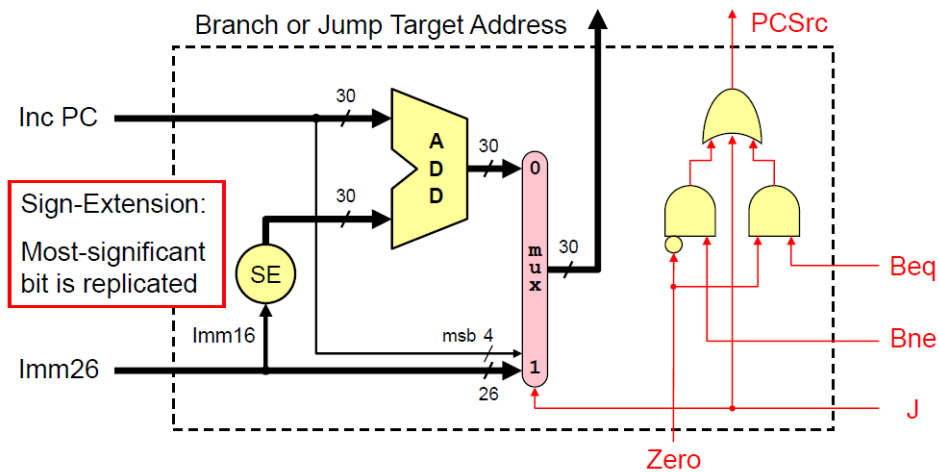
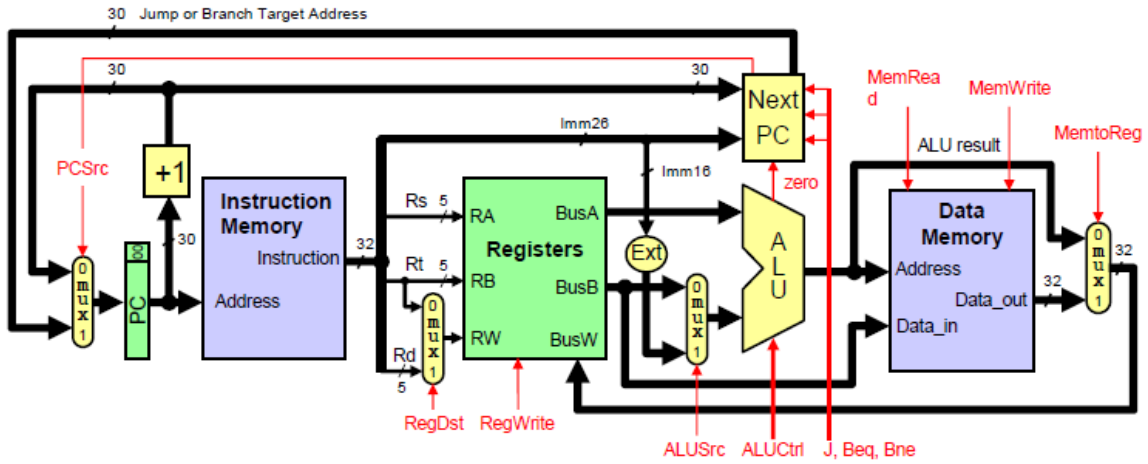
$$A = + 1.011 \ 1110 \ 0100 \ 0000 \ 0000 \ 0000 \ 000 \quad \mathbf{x} \ 2^{32}$$

$$B = +1.111 \ 1000 \ 0000 \ 0000 \ 0000 \ 0000 \ 000 \quad \mathbf{x} \ 2^4$$

$$C = - 1.011 \ 1110 \ 0100 \ 0000 \ 0000 \ 0000 \ 000 \quad \mathbf{x} \ 2^{32}$$

Is the obtained result intuitive? Justify your answer.

- (v) [5 Points] Assume that we want to add the instruction JAL to the MIPS datapath. Make all the necessary modifications to the MIPS Datapath for implementing the JAL instruction including the NextPC block. The NextPC block implementation is given below.



Syscall Services:

Service	\$v0	Arguments / Result
Print Integer	1	\$a0 = integer value to print
Print Float	2	\$f12 = float value to print
Print Double	3	\$f12 = double value to print
Print String	4	\$a0 = address of null-terminated string
Read Integer	5	Return integer value in \$v0
Read Float	6	Return float value in \$f0
Read Double	7	Return double value in \$f0
Read String	8	\$a0 = address of input buffer \$a1 = maximum number of characters to read
Print Char	11	\$a0 = character to print
Read Char	12	Return character read in \$v0

MIPS Instructions:

Instruction	Meaning	R-Type Format						
add \$s1, \$s2, \$s3	$\$s1 = \$s2 + \$s3$	op = 0	rs = \$s2	rt = \$s3	rd = \$s1	sa = 0	f = 0x20	
addu \$s1, \$s2, \$s3	$\$s1 = \$s2 + \$s3$	op = 0	rs = \$s2	rt = \$s3	rd = \$s1	sa = 0	f = 0x21	
sub \$s1, \$s2, \$s3	$\$s1 = \$s2 - \$s3$	op = 0	rs = \$s2	rt = \$s3	rd = \$s1	sa = 0	f = 0x22	
subu \$s1, \$s2, \$s3	$\$s1 = \$s2 - \$s3$	op = 0	rs = \$s2	rt = \$s3	rd = \$s1	sa = 0	f = 0x23	

Instruction	Meaning	R-Type Format						
and \$s1, \$s2, \$s3	$\$s1 = \$s2 \& \$s3$	op = 0	rs = \$s2	rt = \$s3	rd = \$s1	sa = 0	f = 0x24	
or \$s1, \$s2, \$s3	$\$s1 = \$s2 \$s3$	op = 0	rs = \$s2	rt = \$s3	rd = \$s1	sa = 0	f = 0x25	
xor \$s1, \$s2, \$s3	$\$s1 = \$s2 \wedge \$s3$	op = 0	rs = \$s2	rt = \$s3	rd = \$s1	sa = 0	f = 0x26	
nor \$s1, \$s2, \$s3	$\$s1 = \sim(\$s2 \$s3)$	op = 0	rs = \$s2	rt = \$s3	rd = \$s1	sa = 0	f = 0x27	

Instruction	Meaning	R-Type Format						
sll \$s1, \$s2, 10	$\$s1 = \$s2 \ll 10$	op = 0	rs = 0	rt = \$s2	rd = \$s1	sa = 10	f = 0	
srl \$s1, \$s2, 10	$\$s1 = \$s2 \gg 10$	op = 0	rs = 0	rt = \$s2	rd = \$s1	sa = 10	f = 2	
sra \$s1, \$s2, 10	$\$s1 = \$s2 \gg 10$	op = 0	rs = 0	rt = \$s2	rd = \$s1	sa = 10	f = 3	
sllv \$s1, \$s2, \$s3	$\$s1 = \$s2 \ll \$s3$	op = 0	rs = \$s3	rt = \$s2	rd = \$s1	sa = 0	f = 4	
srlv \$s1, \$s2, \$s3	$\$s1 = \$s2 \gg \$s3$	op = 0	rs = \$s3	rt = \$s2	rd = \$s1	sa = 0	f = 6	
srav \$s1, \$s2, \$s3	$\$s1 = \$s2 \gg \$s3$	op = 0	rs = \$s3	rt = \$s2	rd = \$s1	sa = 0	f = 7	

Instruction	Meaning	I-Type Format				
addi \$s1, \$s2, 10	$\$s1 = \$s2 + 10$	op = 0x8	rs = \$s2	rt = \$s1	imm ¹⁶ = 10	
addiu \$s1, \$s2, 10	$\$s1 = \$s2 + 10$	op = 0x9	rs = \$s2	rt = \$s1	imm ¹⁶ = 10	
andi \$s1, \$s2, 10	$\$s1 = \$s2 \& 10$	op = 0xc	rs = \$s2	rt = \$s1	imm ¹⁶ = 10	
ori \$s1, \$s2, 10	$\$s1 = \$s2 10$	op = 0xd	rs = \$s2	rt = \$s1	imm ¹⁶ = 10	
xori \$s1, \$s2, 10	$\$s1 = \$s2 \wedge 10$	op = 0xe	rs = \$s2	rt = \$s1	imm ¹⁶ = 10	
lui \$s1, 10	$\$s1 = 10 \ll 16$	op = 0xf	0	rt = \$s1	imm ¹⁶ = 10	

Instruction	Meaning	Format				
j label	jump to label	op ⁶ = 2	imm ²⁶			
beq rs, rt, label	branch if (rs == rt)	op ⁶ = 4	rs ⁵	rt ⁵	imm ¹⁶	
bne rs, rt, label	branch if (rs != rt)	op ⁶ = 5	rs ⁵	rt ⁵	imm ¹⁶	
blez rs, label	branch if (rs <= 0)	op ⁶ = 6	rs ⁵	0	imm ¹⁶	
bgtz rs, label	branch if (rs > 0)	op ⁶ = 7	rs ⁵	0	imm ¹⁶	
bltz rs, label	branch if (rs < 0)	op ⁶ = 1	rs ⁵	0	imm ¹⁶	
bgez rs, label	branch if (rs >= 0)	op ⁶ = 1	rs ⁵	1	imm ¹⁶	

Instruction	Meaning	Format						
slt rd, rs, rt	rd=(rs<rt?1:0)	op ⁶ = 0	rs ⁵	rt ⁵	rd ⁵	0	0x2a	
sltu rd, rs, rt	rd=(rs<rt?1:0)	op ⁶ = 0	rs ⁵	rt ⁵	rd ⁵	0	0x2b	
slti rt, rs, imm ¹⁶	rt=(rs<imm?1:0)	0xa	rs ⁵	rt ⁵	imm ¹⁶			
sltiu rt, rs, imm ¹⁶	rt=(rs<imm?1:0)	0xb	rs ⁵	rt ⁵	imm ¹⁶			

Instruction	Meaning	I-Type Format				
lb rt, imm ¹⁶ (rs)	rt = MEM[rs+imm ¹⁶]	0x20	rs ⁵	rt ⁵	imm ¹⁶	
lh rt, imm ¹⁶ (rs)	rt = MEM[rs+imm ¹⁶]	0x21	rs ⁵	rt ⁵	imm ¹⁶	
lw rt, imm ¹⁶ (rs)	rt = MEM[rs+imm ¹⁶]	0x23	rs ⁵	rt ⁵	imm ¹⁶	
lbu rt, imm ¹⁶ (rs)	rt = MEM[rs+imm ¹⁶]	0x24	rs ⁵	rt ⁵	imm ¹⁶	
lhu rt, imm ¹⁶ (rs)	rt = MEM[rs+imm ¹⁶]	0x25	rs ⁵	rt ⁵	imm ¹⁶	
sb rt, imm ¹⁶ (rs)	MEM[rs+imm ¹⁶] = rt	0x28	rs ⁵	rt ⁵	imm ¹⁶	
sh rt, imm ¹⁶ (rs)	MEM[rs+imm ¹⁶] = rt	0x29	rs ⁵	rt ⁵	imm ¹⁶	
sw rt, imm ¹⁶ (rs)	MEM[rs+imm ¹⁶] = rt	0x2b	rs ⁵	rt ⁵	imm ¹⁶	

Instruction	Meaning	Format							
jal label	\$31=PC+4, jump	op ⁶ = 3	imm ²⁶						
jr Rs	PC = Rs	op ⁶ = 0	rs ⁵	0	0	0	0	8	
jalr Rd, Rs	Rd=PC+4, PC=Rs	op ⁶ = 0	rs ⁵	0	rd ⁵	0	0	9	

Instruction	Meaning	Format						
<u>mult</u> Rs, Rt	Hi, Lo = <u>Rs</u> × <u>Rt</u>	op ⁶ = 0	Rs ⁵	Rt ⁵	0	0	0x18	
<u>multu</u> Rs, Rt	Hi, Lo = <u>Rs</u> × <u>Rt</u>	op ⁶ = 0	Rs ⁵	Rt ⁵	0	0	0x19	
<u>mul</u> Rd, Rs, Rt	Rd = <u>Rs</u> × <u>Rt</u>	0x1c	Rs ⁵	Rt ⁵	Rd ⁵	0	0x02	
<u>div</u> Rs, Rt	Hi, Lo = <u>Rs</u> / <u>Rt</u>	op ⁶ = 0	Rs ⁵	Rt ⁵	0	0	0x1a	
<u>divu</u> Rs, Rt	Hi, Lo = <u>Rs</u> / <u>Rt</u>	op ⁶ = 0	Rs ⁵	Rt ⁵	0	0	0x1b	
<u>mfhi</u> Rd	Rd = Hi	op ⁶ = 0	0	0	Rd ⁵	0	0x10	
<u>mflo</u> Rd	Rd = Lo	op ⁶ = 0	0	0	Rd ⁵	0	0x12	