## Chapter 15

### Application of Aqueous Equilibria

### Chapter 15 Preview App. Aqueous Equilibria

#### Acid-bases Equilibria

- Acid-base, Common ion, Equilibria calculation
- Buffer solution, Buffer capacity
- Titration and pH curve, strong A-Strong B, Weak A-Strong B, Strong A-Weak B, Acid-Base indicators

### Solubility Equilibria

- Solubility product, Relative solubilities, Common ion effect, pH and solubility
- Precipitation and qualitative analysis
- Complex Ion Equilibria
   Complex ions and solubilities

## Introduction

All the chemistry of the natural world occurs in aqueous solution, three equilibria will be cover:

- More application of Acid-Base chemistry
- Solubility of salts and their equilibria
- Formation of complex ions and their equilibria



### 15.1 Solutions of Acid or Bases Containing a Common Ion

Consider mixture of  $CH_3COONa$  (strong electrolyte) and  $CH_3COOH$  (weak acid).

 $CH_{3}COONa (s) \longrightarrow Na^{+} (aq) + CH_{3}COO^{-} (aq)$  common  $CH_{3}COOH (aq) \longrightarrow H^{+} (aq) + CH_{3}COO^{-} (aq)$ ion

The presence of a common ion **suppresses** the ionization of a weak acid or a weak base.

The *common ion effect* is the shift in equilibrium caused by the addition of a compound having an ion in common with the dissolved substance.

### **Equilibrium Calculations**

Consider mixture of salt NaA and weak acid HA.

NaA (s) Na<sup>+</sup> (aq) + A<sup>-</sup> (aq)  
HA (aq) H<sup>+</sup> (aq) + A<sup>-</sup> (aq)  

$$K_{a} = \frac{[H^{+}][A^{-}]}{[HA]}$$

$$[H^{+}] = \frac{K_{a}[HA]}{[A^{-}]}$$
Henderson-Hasselbalch  
equation

$$-\log [H^{+}] = -\log K_{a} - \log \frac{[HA]}{[A^{-}]} \qquad \text{equation}$$

$$-\log [H^{+}] = -\log K_{a} + \log \frac{[A^{-}]}{[HA]} \qquad pH = pK_{a} + \log \frac{[\text{conjugate base}]}{[\text{acid}]}$$

$$pH = pK_{a} + \log \frac{[A^{-}]}{[HA]} \qquad pK_{a} = -\log K_{a}$$



## What is the pH of a solution containing 0.30 *M* HCOOH and 0.52 *M* HCOOK?

Mixture of weak acid and conjugate base!

HCOOH (aq)  $\longrightarrow$  H<sup>+</sup> (aq) + HCOO<sup>-</sup> (aq) Initial (M) 0.30 0.00 0.52 Change (M) -X +X+XEquilibrium (M) 0.30 - x0.52 + xX  $pH = pK_a + \log \frac{[HCOO^-]}{[HCOOH]}$ Common ion effect  $0.30 - x \approx 0.30$  $pH = 3.77 + log \frac{[0.52]}{[0.30]} = 4.01$  $0.52 + x \approx 0.52$ HCOOH  $pK_{a} = 3.77$ 



### 15.2 Buffered Solutions

A **buffer solution** is a solution of:

- 1. A weak acid or a weak base and
- 2. The salt of the weak acid or weak base

#### Both must be present!

A buffer solution has the ability to resist changes in pH upon the addition of small amounts of either acid or base.

Consider an equal molar mixture of CH<sub>3</sub>COOH and CH<sub>3</sub>COONa

Add strong acid  $H^+(aq) + CH_3COO^-(aq) \longrightarrow CH_3COOH(aq)$ Add strong base  $OH^-(aq) + CH_3COOH(aq) \longrightarrow CH_3COO^-(aq) + H_2O(l)$ 





not a buffer solution

(c)  $CO_3^{2-}$  is a weak base and  $HCO_3^{-}$  is it conjugate acid buffer solution

# QUESTION

The dissociation constant of propanoic acid  $(HC_3H_5O_2)$  is  $1.3 \times 10^{-5}$ . What is the pH of a buffer made with 0.50 M propanoic acid and 0.25 M NaC<sub>3</sub>H<sub>5</sub>O<sub>2</sub> (the sodium salt of propanoic acid)?

- 1. 4.59
- 2. 5.19
- 3. 7.00
- 4. I'm not getting any of these answers.

Choice 1 is the correct pH of the buffer. There is an assumption being made here about the concentration of the salt to be only from the salt added. This ignores the small amount of propionate  $[C_3H_5O_2^{-}]$  that may be produced from the acid dissociation.

Calculate the pH of the 0.30 M NH<sub>3</sub>/0.36 M NH<sub>4</sub>Cl buffer system. What is the pH after the addition of 20.0 mL of 0.050 M NaOH to 80.0 mL of the buffer solution?

$$NH_4^+ (aq) \longrightarrow H^+ (aq) + NH_3 (aq)$$

$$pH = pK_a + \log \frac{[NH_3]}{[NH_4^+]}$$
  $pK_a = 9.25$   $pH = 9.25 + \log \frac{[0.30]}{[0.36]} = 9.17$ 

start (moles)0.0290.0010.024 $NH_4^+(aq) + OH^-(aq) \longrightarrow H_2O(l) + NH_3(aq)$ end (moles)0.0280.00.025

final volume = 80.0 mL + 20.0 mL = 100 mL

$$[NH_4^+] = \frac{0.028}{0.10} [NH_3] = \frac{0.025}{0.10} pH = 9.25 + log \frac{[0.25]}{[0.28]} = 9.20$$



### **15.3 Buffered Capacity**

The ability of buffers to absorb amount of H<sup>+</sup> or OH<sup>-</sup> without a significant change in pH. It is determined by the ratio [A<sup>-</sup>]/[HA].

Solution A

Adding 0.010 mol gaseous HCl to 1L of the following solutions:

A- 1.0 M HAc & 1.0 M NaAc (before): pH = 4.74(after): pH = 4.74 - 0.0088 = 4.730.2 % change



Solution B

B- 0.010 M HAc & 1.0 M NaAc (before): pH = 4.74 + 2.00 = 6.74(after): pH = 4.74 + 1.69 = 6.43**4.5 % change** 

The best buffer is the one has ratio closest to 1 or its equilibrium constant is of value close to the desired pH.

## QUESTION

To culture a certain bacteria a microbiologist would like to buffer the media at a pH of 3.75. To maximize the efficiency of the system a 1:1 ratio of acid to salt will be used. Which of the following acids would make the best choice for the buffer?

- 1. Acetic acid;  $K_a = 1.8 \times 10^{-5}$
- 2. Propanoic acid;  $K_a = 1.3 \times 10^{-5}$
- 3. Formic acid;  $K_a = 1.8 \times 10^{-4}$
- 4. Nitrous acid;  $K_a = 4.0 \times 10^{-4}$

Choice 3 represents the best selection for this buffer. If the acid:salt ratio is to be 1:1, the pH will equal  $K_a$ . At a pH of 3.75 the closest p $K_a$  would be from formic acid:  $1.3 \times 10^{-4}$ .

#### 15.4 Titrations and pH Curves

In a *titration* a solution of accurately known concentration is added gradually added to another solution of unknown concentration until the chemical reaction between the two solutions is complete.

*Equivalence point* – the point at which the reaction is complete

Indicator – substance that changes color at (or near) the equivalence point ... End Point



Slowly add base to unknown acid UNTIL

The indicator changes color (pink)





#### <u>Strong Acid-Strong Base Titrations</u> NaOH (aq) + HCl (aq) → H<sub>2</sub>O (I) + NaCl (aq) OH<sup>-</sup> (aq) + H<sup>+</sup> (aq) → H<sub>2</sub>O (I)



Volume of NaOH added (mL)

Before: [H<sup>+</sup>] = Left moles (Acid-Added Base)/Total volume At: [H<sup>+</sup>] = Water After: [OH<sup>-</sup>] = Left moles (Added Base-Acid)/Total volume



<u>Weak Acid-Strong Base Titrations</u> CH<sub>3</sub>COOH (aq) + NaOH (aq) → CH<sub>3</sub>COONa (aq) + H<sub>2</sub>O (*I* CH<sub>3</sub>COOH (aq) + OH<sup>-</sup> (aq) → CH<sub>3</sub>COO<sup>-</sup> (aq) + H<sub>2</sub>O (*I*)

At equivalence point (pH > 7):

 $CH_3COO^-(aq) + H_2O(l) \longrightarrow OH^-(aq) + CH_3COOH(aq)$ 



Before:  $[H^+] =$  Left moles (Acid-Added Base)/Total volume then use ICE At:  $[H^+] =$  Use ICE for Salt of weak acid and strong base After:  $[OH^-] =$  Left moles (Added Base-Acid)/Total volume



Exactly 100 mL of 0.10 M HNO<sub>2</sub> are titrated with a 0.10 M NaOH solution. What is the pH at the equivalence point ?

start (moles) 0.01 0.01  $HNO_2(aq) + OH^-(aq) \longrightarrow NO_2^-(aq) + H_2O(l)$ end (moles) 0.0 0.0 0.01  $[NO_2^{-1}] = \frac{0.01}{0.200} = 0.05 M$ Final volume = 200 mL  $NO_2^-(aq) + H_2O(l) \longrightarrow OH^-(aq) + HNO_2(aq)$ Initial (M) 0.05 0.00 0.00 Change (M) -X +X+XEquilibrium (M) 0.05 - xX X  $K_b = \frac{[OH^-][HNO_2]}{[NO_2^-]} = \frac{x^2}{0.05 \cdot x} = 2.2 \times 10^{-11}$ pOH = 5.98pH = 14 - pOH = 8.02 $0.05 - x \approx 0.05$   $x \approx 1.05 \times 10^{-6} = [OH^{-1}]$ 



At equivalence point (pH < 7):

 $NH_4^+(aq) + H_2O(l) \longrightarrow NH_3(aq) + H^+(aq)$ Volume HCI 11 added (mL) pH 10 After 0.0 11.13 5.0 9.86 9 10.0 9.44 8 15.0 9.08 20.0 8.66 7 22.0 8.39 pH 6 24.0 7.88 Equivalence ---- At 25.0 5.28 5 point 26.0 2.7028.0 2.22 30.0 2.00 3 35.0 1.70 2 1.5240.045.0 1.40 1 Before 50.0 1.30 0 10 20 30 40 50

Volume of HCI added (mL)

Before:  $[OH^-] = Left$  moles (Base-Added Acid)/Total volume then use ICE At:  $[H^+] = Use$  ICE for Salt of strong acid and weak base After:  $[H^+] = Left$  moles (Added Acid-Base)/Total volume



### 15.5 Acid-Base Indicators HIn (aq) $\overrightarrow{H^+}$ (aq) + In<sup>-</sup> (aq)

[HIn]  $\geq 10$  Color of acid (HIn) predominates

 $\frac{[HIn]}{[In^{-}]} \leq 10$  Color of conjugate base (In<sup>-</sup>) predominates

The useful range for any indicator is given by

 $pKa \pm 1$ 





### Which indicator(s) would you use for a titration of $HNO_2$ with KOH ?

Weak acid titrated with strong base.

At equivalence point, will have conjugate base of weak acid. At equivalence point, pH > 7

Use cresol red or phenolphthalein

	Color			
Indicator	In Acid	In Base	pH Range*	
Thymol blue	Red	Yellow	1.2-2.8	
Bromophenol blue	Yellow	Bluish purple	3.0-4.6	
Methyl orange	Orange	Yellow	3.1-4.4	
Methyl red	Red	Yellow	4.2-6.3	
Chlorophenol blue	Yellow	Red	4.8-6.4	
Bromothymol blue	Yellow	Blue	6.0-7.6	
Cresol red	Yellow	Red	7.2-8.8	
Phenolphthalein	Colorless	Reddish pink	8.3-10.0	



15.6 Solubility Equilibria and Solubility Product AgCl (s)  $\rightarrow$  Ag<sup>+</sup> (aq) + Cl<sup>-</sup> (aq)

 $K_{sp} = [Ag^{+}][CI^{-}] \qquad K_{sp} \text{ is the solubility product constant}$   $MgF_{2}(s) \longleftrightarrow Mg^{2+}(aq) + 2F^{-}(aq) \qquad K_{sp} = [Mg^{2+}][F^{-}]^{2}$   $Ag_{2}CO_{3}(s) \rightleftharpoons 2Ag^{+}(aq) + CO_{3}^{2^{-}}(aq) \qquad K_{sp} = [Ag^{+}]^{2}[CO_{3}^{2^{-}}]$   $Ca_{3}(PO_{4})_{2}(s) \rightleftharpoons 3Ca^{2+}(aq) + 2PO_{4}^{3^{-}}(aq) \qquad K_{sp} = [Ca^{2+}]^{3}[PO_{3}^{3^{-}}]^{2}$ 

Dissolution of an ionic solid in aqueous solution:

- $Q < K_{sp}$  Unsaturated solution No precipitate
- $Q = K_{sp}$  Saturated solution
- $Q > K_{sp}$  Supersaturated solution Precipitate will form



### Solubility Equilibria

*Molar solubility* (mol/L) is the number of moles of solute dissolved in 1 L of a saturated solution.

**Solubility** (g/L) is the number of grams of solute dissolved in 1 L of a saturated solution.



#### **Relative Solubility**

•Salts being compared produce same no. of ions, e.g., AgI, CuI, CaSO4, KSP used for comparison.

•Salts being compared produce different no. of ions, e.g., AgI,  $Ag_2S..K_{SP}$  cannot be used for comparison.



#### What is the solubility of silver chloride in g/L?

AgCl (s) 
$$\longrightarrow$$
 Ag<sup>+</sup> (aq) + Cl<sup>-</sup> (aq)
  $K_{sp} = 1.6 \times 10^{-10}$ 

 Initial (M)
 0.00
 0.00
  $K_{sp} = [Ag^+][Cl^-]$ 

 Change (M)
 +s
 +s
  $K_{sp} = s^2$ 

 Equilibrium (M)
 s
 s
 s
 s =  $\sqrt{K_{sp}}$ 

 [Ag<sup>+</sup>] = 1.3 × 10^{-5} M
 [Cl<sup>-</sup>] = 1.3 × 10^{-5} M
  $S = 1.3 \times 10^{-5}$ 

 Solubility of AgCl =  $\frac{1.3 \times 10^{-5} \text{ mol AgCl}}{1 \text{ L soln}} \times \frac{143.35 \text{ g AgCl}}{1 \text{ mol AgCl}} = 1.9 \times 10^{-3} \text{ g/L}$ 



What concentration of Ag is required to precipitate ONLY AgBr in a solution that contains both Br<sup>-</sup> and Cl<sup>-</sup> at a concentration of 0.02 *M*?

AgBr (s) 
$$\longrightarrow$$
 Ag<sup>+</sup> (aq) + Br<sup>-</sup> (aq)  $K_{sp} = 7.7 \times 10^{-13}$   
 $K_{sp} = [Ag^+][Br^-]$   

$$[Ag^+] = \frac{K_{sp}}{[Br^-]} = \frac{7.7 \times 10^{-13}}{0.020} = 3.9 \times 10^{-11} M$$
AgCl (s)  $\longrightarrow$  Ag<sup>+</sup> (aq) + Cl<sup>-</sup> (aq)  $K_{sp} = 1.6 \times 10^{-10}$   
 $K_{sp} = [Ag^+][Cl^-]$   

$$[Ag^+] = \frac{K_{sp}}{[Br^-]} = \frac{1.6 \times 10^{-10}}{0.020} = 8.0 \times 10^{-9} M$$

 $3.9 \times 10^{-11} M < [Ag^+] < 8.0 \times 10^{-9} M$ 

### The Common Ion Effect and Solubility

The presence of a common ion **decreases** the solubility of the salt.

What is the molar solubility of AgBr in (a) pure water and (b) 0.0010 *M* NaBr?

AgBr (s)  $\longrightarrow$  Ag<sup>+</sup> (aq) + Br<sup>-</sup> (aq)

 $K_{sp} = 7.7 \times 10^{-13}$ 

 $s^2 = K_{sp}$  $s = 8.8 \times 10^{-7}$  NaBr (s)  $\longrightarrow$  Na<sup>+</sup> (aq) + Br<sup>-</sup> (aq) [Br<sup>-</sup>] = 0.0010 *M* AgBr (s)  $\overrightarrow{}$  Ag<sup>+</sup> (aq) + Br<sup>-</sup> (aq) [Ag<sup>+</sup>] = s [Br<sup>-</sup>] = 0.0010 + s  $\approx$  0.0010  $K_{sp} = 0.0010 \times s$  $s = 7.7 \times 10^{-10}$ 

### pH and Solubility

- The presence of a common ion **decreases** the solubility.
- Insoluble bases dissolve in acidic solutions
- Insoluble acids dissolve in basic solutions
   readd/e

 $Mg(OH)_2$  (s)  $\longrightarrow$   $Mg^{2+}(aq) + 2OH^-(aq)$ 

At pH less than 10.45

$$K_{sp} = [Mg^{2+}][OH^{-}]^{2} = 1.2 \times 10^{-17}$$
  
 $K_{sp} = (s)(2s)^{2} = 4s^{3}$   
 $4s^{3} = 1.2 \times 10^{-11}$ 

 $s = 1.4 \times 10^{-4} M$ 

 $[OH^{-}] = 2s = 2.8 \times 10^{-4} M$ 

pOH = 3.55 pH = 10.45

Lower [OH-]

 $OH^{-}(aq) + H^{+}(aq) \longrightarrow H_{2}O(l)$ 

Increase solubility of Mg(OH)<sub>2</sub>

At pH greater than 10.45

Raise [OH-]

Decrease solubility of Mg(OH)<sub>2</sub>



#### 15.7 Precipitation and Qualitative Analysis

If 2.00 mL of 0.200 M NaOH are added to 1.00 L of 0.100 M CaCl<sub>2</sub>, will a precipitate form?

The ions present in solution are Na<sup>+</sup>, OH<sup>-</sup>, Ca<sup>2+</sup>, Cl<sup>-</sup>.

Only possible precipitate is  $Ca(OH)_2$  (solubility rules).

Is  $Q > K_{sp}$  for Ca(OH)<sub>2</sub>?

 $\begin{bmatrix} Ca^{2+} \end{bmatrix}_{0} = \begin{bmatrix} OH^{-} \end{bmatrix}_{0} = 4.0 \times \\ 10^{-4} M \\ Q = \begin{bmatrix} Ca^{2+} \end{bmatrix}_{0} \begin{bmatrix} OH^{-} \end{bmatrix}_{0}^{2} = 0.10 \times (4.0 \times 10^{-4})^{2} = 1.6 \\ \times 10^{-8} \\ K_{sp} = \begin{bmatrix} Ca^{2+} \end{bmatrix} \begin{bmatrix} OH^{-} \end{bmatrix}^{2} = 8.0 \\ \times 10^{-6} \\ Q < \\ No \text{ precipite will} \\ K_{sp} & \text{form} \\ \end{bmatrix}$ 



## Selective Precipitation and Qualitative Analysis





### 15.8 Complex Ion Equilibria and Solubility

A *complex ion* is an ion containing a central metal cation bonded to one or more molecules or ions.

$$\operatorname{CO}^{2+}(aq) + 4\operatorname{Cl}^{-}(aq) \longrightarrow \operatorname{Co}\operatorname{Cl}_{4}^{2-}(aq)$$

The formation constant or stability constant  $(K_f)$  is the equilibrium constant for the complex ion formation.

#### $Co(H_2O)_6^{2+}$ $CoCl_4^{2-}$



$$K_f = \frac{[CoCl_4^{2-}]}{[Co^{2+}][Cl^{-}]^4}$$

 $K_{f}$  f stability of complex

## QUESTION

Given the following values of equilibrium constants:  $Cu(OH)_{2}(s) \Longrightarrow Cu^{2+}(aq) + 2OH^{-}(aq) K_{sp} = 1.6 \times 19^{-19}$  $Cu(NH_{3})_{4}^{2+} \Longrightarrow Cu^{2+}(aq) + 4NH_{3}(aq) K = 1.0 \times 10^{-13}$ 

What is the value of the equilibrium constant for the reaction:  $Cu(OH)_2(s) + 4NH_3(aq) \Longrightarrow Cu(NH_3)_4^{2+}(aq) + 2OH^{-}(aq)$ 

- $1.6 \times 10^{-19}$ 1) 2)  $6.2 \times 10^{31}$ 3)  $1.6 \times 10^{-6}$
- 4)  $1.6 \times 10^{-32}$
- $1.0 \times 10^{13}$ 5)

3) 1.6  $\times$  10  $^{-6}$ The equilibrium constant equal to  $K_{sp}/K$ 

#### **Table 16.5** Separation of Cations into Groups According toTheir Precipitation Reactions with Various Reagents

Group	Cation	Precipitating Reagents	Insoluble Compound	K <sub>sp</sub>
1	$Ag^+$	HCI	AgCl	$1.6  imes 10^{-10}$
	$Hg_2^{2+}$		$Hg_2Cl_2$	$3.5  imes 10^{-18}$
	$Pb^{2+}$	$\downarrow$	PbCl <sub>2</sub>	$2.4 imes10^{-4}$
2	Bi <sup>3+</sup>	H <sub>2</sub> S	Bi <sub>2</sub> S <sub>3</sub>	$1.6  imes 10^{-72}$
	$Cd^{2+}$	in acidic	CdS	$8.0  imes 10^{-28}$
	Cu <sup>2+</sup>	solutions	CuS	$6.0  imes 10^{-37}$
	Sn <sup>2+</sup>	$\downarrow$	SnS	$1.0  imes 10^{-26}$
3	$AI^{3+}$	H <sub>2</sub> S	Al(OH) <sub>3</sub>	$1.8  imes 10^{-33}$
	Co <sup>2+</sup>	in basic	CoS	$4.0  imes 10^{-21}$
	Cr <sup>3+</sup>	solutions	Cr(OH) <sub>3</sub>	$3.0 imes10^{-29}$
	$Fe^{2+}$		FeS	$6.0  imes 10^{-19}$
	Mn <sup>2+</sup>		MnS	$3.0 imes10^{-14}$
	Ni <sup>2+</sup>		NiS	$1.4  imes 10^{-24}$
	Zn <sup>2+</sup>		ZnS	$3.0  imes 10^{-23}$
4	Ba <sup>2+</sup>	Na <sub>2</sub> CO <sub>3</sub>	BaCO <sub>3</sub>	$8.1  imes 10^{-9}$
	Ca <sup>2+</sup>		CaCO <sub>3</sub>	$8.7 imes10^{-9}$
	$\mathrm{Sr}^{2+}$	$\downarrow$	SrCO <sub>3</sub>	$1.6 imes10^{-9}$
5	$K^+$	No precipitating	None	
	$Na^+$	reagent	None	
	$NH_4^+$		None	



### **Cation Analysis**



Qualitative Analysis of Cations





### **Chemistry In Action:** How an Eggshell is Formed

$$Ca^{2+}(aq) + CO_3^{2-}(aq) \longrightarrow CaCO_3(s)$$

$$CO_2(g) + H_2O(I) \xrightarrow[anhydrase]{\text{carbonic}} H_2CO_3(aq)$$

$$H_2CO_3(aq) \longrightarrow H^+(aq) + HCO_3^-(aq)$$

 $HCO_3^-(aq) \longrightarrow H^+(aq) + CO_3^{2-}(aq)$ 

