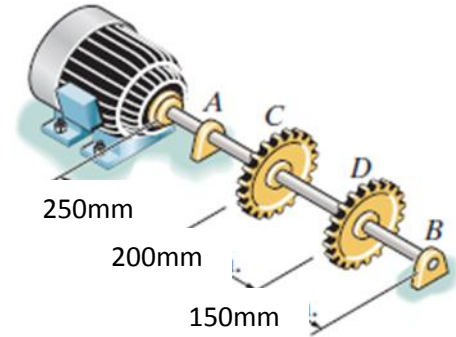


5-58. The motor delivers 33 kW to the 304 stainless steel solid shaft while it rotates at 20 Hz. The shaft has a diameter of 37.5 mm. and is supported on smooth bearings at *A* and *B*, which allow free rotation of the shaft. The gears *C* and *D* fixed to the shaft remove 20 kW and 12 kW, respectively. Determine the absolute maximum stress in the shaft and the angle of twist of gear *C* with respect to gear *D*.



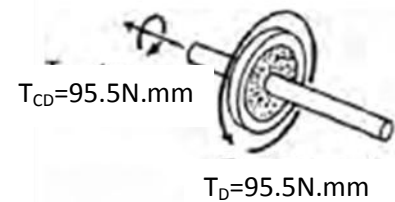
$$T_m = \frac{33 * 1000}{2\pi * 20} = 262.61 \text{ N.m}, \quad T_C = \frac{20 * 1000}{2\pi * 20} = 159.15 \text{ N.m},$$

$$T_D = \frac{12 * 1000}{2\pi * 20} = 95.5 \text{ N.m},$$

$$T_{max} = T_{AC} = 262.61 \text{ N.m},$$

$$\tau_{max} = \frac{T_{max} * C}{J} = \frac{262.61 * 1000 * \frac{37.5}{2}}{\frac{\pi}{2} * (\frac{37.5}{2})^4} = \mathbf{25.36 \text{ MPa}} \quad \text{Ans.}$$

$$\phi_{C/D} = \frac{T_{CD} * L_{CD}}{JG} = \frac{95.5 * 1000 * 200}{\frac{\pi}{2} * (\frac{37.5}{2})^4 * 75 * 1000} = \mathbf{0.001311 \text{ Rad.}} \quad \text{Ans}$$



5.62 The two shafts are made of A-36 steel. Each has a diameter of 25 mm., and they are supported by bearings at *A*, *B*, and *C*, which allow free rotation. If the support at *D* is fixed, determine the angle of twist of end *A* when the torques is applied to the assembly as shown.

Internal Torque: As shown on FBD.

Angle of Twist:

$$\phi_E = \sum \frac{TL}{JG}$$

$$= \frac{1}{\frac{\pi}{2}(12.5)^4 * 75 * 1000} [-90 * 1000 * 750 + 30 * 1000 * 250] =$$

$$-0.02086 = \mathbf{0.02086 \text{ Rad}},$$

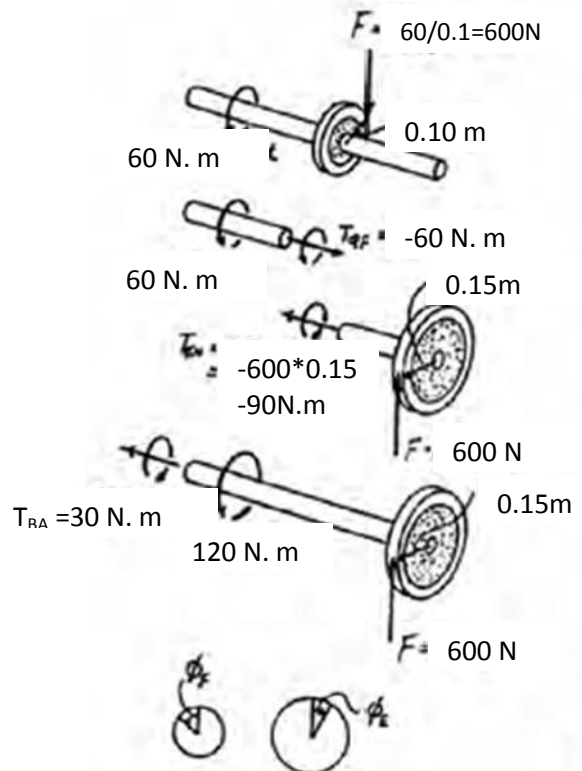
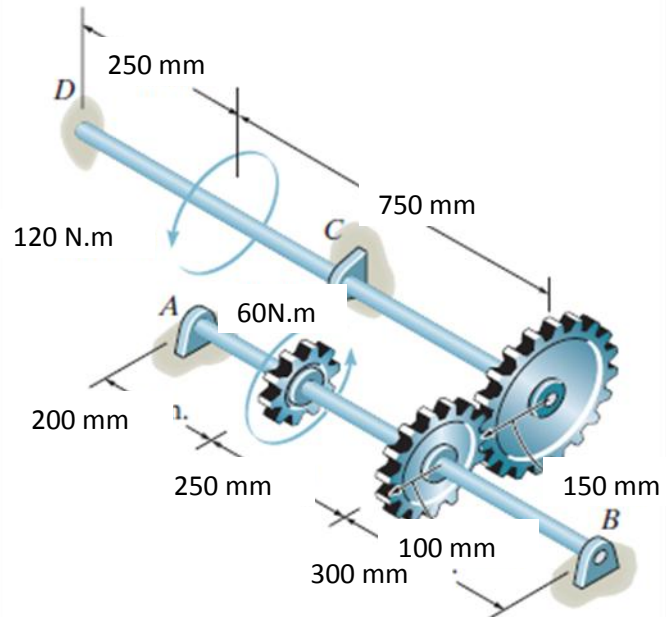
$$\phi_F = \frac{6}{4} \phi_E = \frac{6}{4} * 0.02086 = \mathbf{0.03129 \text{ Rad.}}$$

$$\phi_{A/F} = \frac{-60 * 1000 * 250}{\frac{\pi}{2}(12.5)^4 * 75 * 1000} = -0.0052$$

$$= \mathbf{0.0052 \text{ Rad.}}$$

$$\phi_A = \phi_F + \phi_{A/F} = 0.03129 + 0.0052$$

$$= \mathbf{0.03651 \text{ Rad.} \quad \text{Ans}}$$



5-70. The shafts are made of A-36 steel and each has a diameter of 80 mm. Determine the angle of twist of gear D .

Equilibrium: Referring to the free-body diagram of shaft CDE shown in Fig. a ,

$$\Sigma M_x = 0; \quad 10(10^3) - 2(10^3) - F(0.2) = 0 \quad F = 40(10^3) \text{ N}$$

Internal Loading: Referring to the free-body diagram of gear B , Fig. b ,

$$\Sigma M_x = 0; \quad -T_{AB} - 40(10^3)(0.15) = 0 \quad T_{AB} = -6(10^3) \text{ N}\cdot\text{m}$$

Referring to the free-body diagram of gear D , Fig. c ,

$$\Sigma M_x = 0; \quad 10(10^3) - 2(10^3) - T_{CD} = 0 \quad T_{CD} = 8(10^3) \text{ N}\cdot\text{m}$$

Angle of Twist: The polar moment of inertia of the shafts are

$$J = \frac{\pi}{2} (0.04^4) = 1.28(10^{-6})\pi \text{ m}^4. \text{ We have}$$

$$\phi_B = \frac{T_{AB} L_{AB}}{JG_{st}} = \frac{-6(10^3)(0.6)}{1.28(10^{-6})\pi(75)(10^9)} = -0.01194 \text{ rad} = 0.01194 \text{ rad}$$

Using the gear ratio,

$$\phi_C = \phi_B \left(\frac{r_B}{r_C} \right) = 0.01194 \left(\frac{150}{200} \right) = 0.008952 \text{ rad}$$

Also,

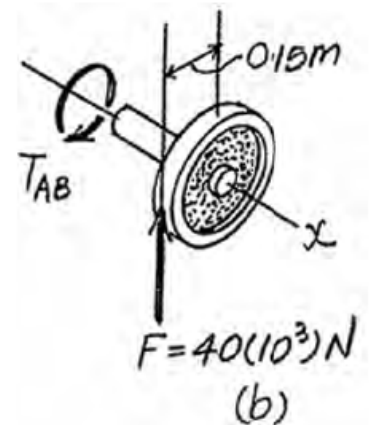
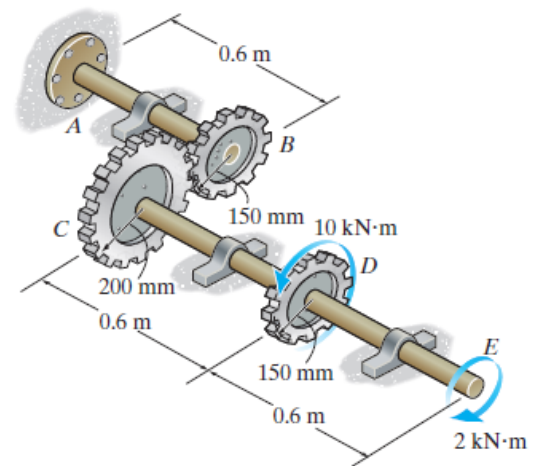
$$\phi_{D/C} = \frac{T_{CD} L_{CD}}{JG_{st}} = \frac{8(10^3)(0.6)}{1.28(10^{-6})\pi(75)(10^9)} = 0.01592 \text{ rad}$$

Thus,

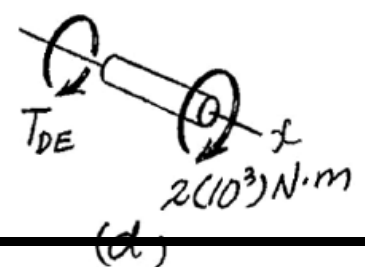
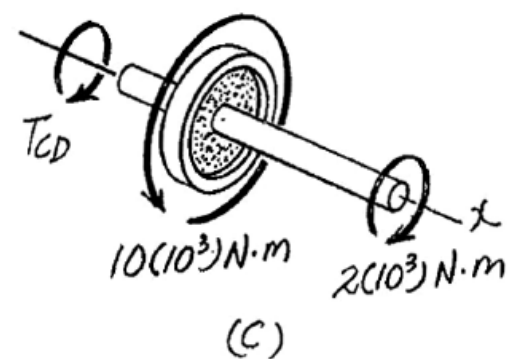
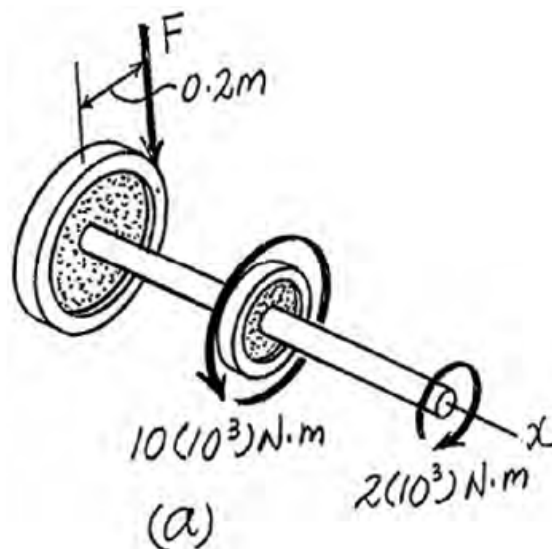
$$\phi_D = \phi_C + \phi_{D/C}$$

$$\phi_D = 0.008952 + 0.01592$$

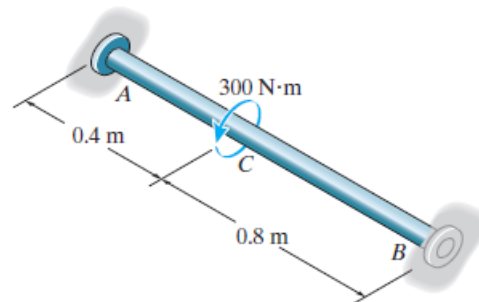
$$= 0.02487 \text{ rad} = 1.42^\circ$$



Ans.



•5-77. The A-36 steel shaft has a diameter of 50 mm and is fixed at its ends A and B . If it is subjected to the torque, determine the maximum shear stress in regions AC and CB of the shaft.



Equilibrium:

$$T_A + T_B - 300 = 0 \quad [1]$$

Compatibility:

$$\begin{aligned} \phi_{C/A} &= \phi_{C/B} \\ \frac{T_A(0.4)}{JG} &= \frac{T_B(0.8)}{JG} \\ T_A &= 2.00T_B \end{aligned} \quad [2]$$

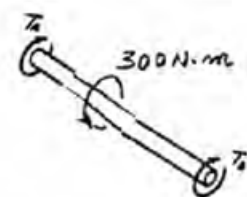
Solving Eqs. [1] and [2] yields:

$$T_A = 200 \text{ N} \cdot \text{m} \quad T_B = 100 \text{ N} \cdot \text{m}$$

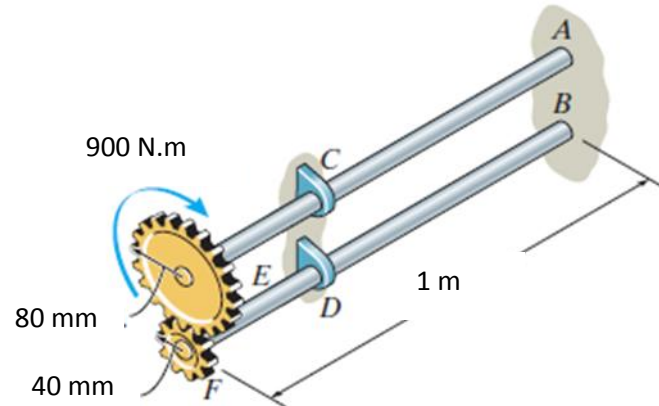
Maximum Shear stress:

$$(\tau_{AC})_{\max} = \frac{T_{AC}}{J} = \frac{200(0.025)}{\frac{\pi}{2}(0.025^4)} = 8.15 \text{ MPa} \quad \text{Ans.}$$

$$(\tau_{CB})_{\max} = \frac{T_{BC}}{J} = \frac{100(0.025)}{\frac{\pi}{2}(0.025^4)} = 4.07 \text{ MPa} \quad \text{Ans.}$$



5–90. The two 1-m-long shafts are made of 2014-T6 aluminum. Each has a diameter of 30 mm, and they are connected using the gears fixed to their ends. Their other ends are attached to fixed supports at *A* and *B*. They are also supported by bearings at *C* and *D*, which allow free rotation of the shafts along their axes. If a torque of 900 N.m is applied to the top gear as shown, determine the maximum shear stress in each shaft.



$$T_A + F(80) - 900 \cdot 1000 = 0 \quad (1)$$

$$T_B - F(40) = 0 \quad (2)$$

From Eqs. (1) and (2)

$$T_A + 2T_B - 900 \cdot 1000 = 0 \quad (3)$$

$$4(\phi_E) = 2(\phi_F); \quad \phi_E = 0.5\phi_F$$

$$\frac{T_A L}{JG} = 0.5 \left(\frac{T_B L}{JG} \right); \quad T_A = 0.5T_B \quad (4)$$

Solving Eqs. (3) and (4) yields:

$$T_A = 180000 \text{ N.m} ; T_B = 360000 \text{ N.m}$$

$$(\tau_{BD})_{\max} = \frac{T_B C}{J} = \frac{360000 \cdot 15}{\frac{\pi}{2}(15)^4} = 67.9 \text{ MPa.}$$

Ans.

$$(\tau_{AC})_{\max} = \frac{T_A C}{J} = \frac{180000 \cdot 15}{\frac{\pi}{2}(15)^4} = 33.95 \text{ MPa.}$$

Ans.

