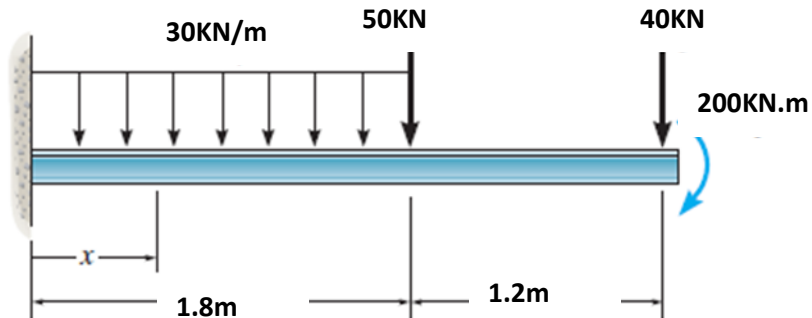


6-18. Draw the shear and moment diagrams for the beam, and determine the shear and moment throughout the beam as functions of  $x$ .



Support Reactions: As shown on FBD.

Shear and Moment Function:

For  $0 \leq x < 1.8 \text{ m}$ :

$$+\uparrow \sum F_y = 0; \quad 144 - 30x - V = 0$$

$$V = (144 - 30x) \text{ kN. Ans.}$$

$$\zeta + \sum M_{NA} = 0; \quad M + 458.6 + 30x \left( \frac{x}{2} \right) - 144x = 0;$$

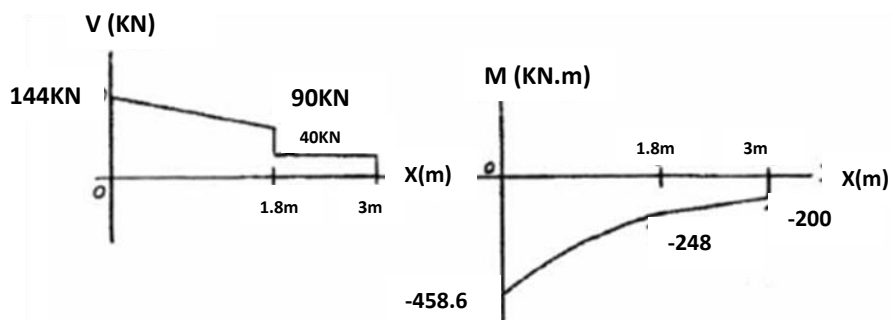
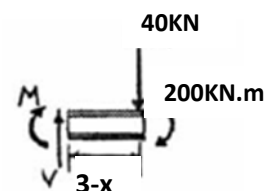
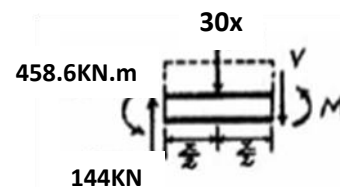
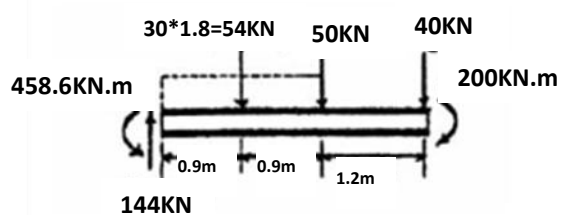
$$M = (-15x^2 + 144x - 458.6) \text{ kN.m Ans.}$$

For  $1.8 \text{ m} < x \leq 3 \text{ m}$ :

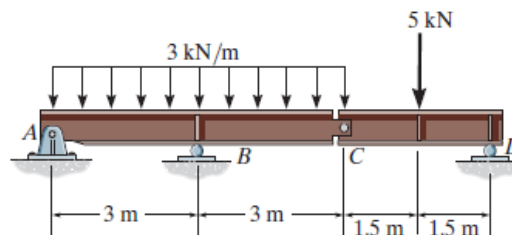
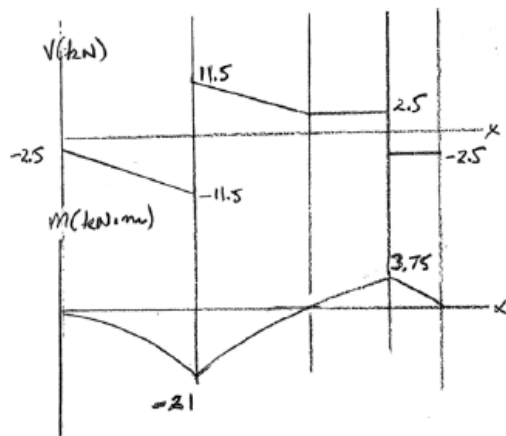
$$+\uparrow \sum F_y = 0; \quad V - 40 = 0; \quad V = 40 \text{ kN Ans.}$$

$$\zeta + \sum M_{NA} = 0; \quad -M - 40(x - 3) - 200 = 0;$$

$$M = (40x - 320) \text{ kN.m Ans.}$$



6-34. Draw the shear and moment diagrams for the compound beam.



6-55. The beam is made from three boards nailed together as shown. If the moment acting on the cross section is  $M = 600 \text{ N}\cdot\text{m}$ , determine the resultant force the bending stress produces on the top board.

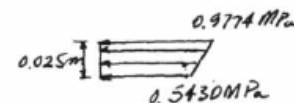
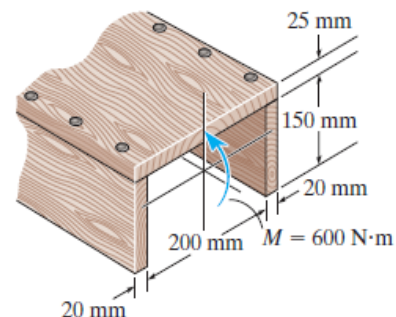
$$\bar{y} = \frac{(0.0125)(0.24)(0.025) + 2(0.15)(0.1)(0.02)}{0.24(0.025) + 2(0.15)(0.02)} = 0.05625 \text{ m}$$

$$I = \frac{1}{12}(0.24)(0.025^3) + (0.24)(0.025)(0.04375^2) + 2\left(\frac{1}{12}\right)(0.02)(0.15^3) + 2(0.15)(0.02)(0.04375^2) = 34.53125(10^{-6}) \text{ m}^4$$

$$\sigma_1 = \frac{My}{I} = \frac{600(0.05625)}{34.53125(10^{-6})} = 0.9774 \text{ MPa}$$

$$\sigma_b = \frac{My}{I} = \frac{600(0.05625 - 0.025)}{34.53125(10^{-6})} = 0.5430 \text{ MPa}$$

$$F = \frac{1}{2}(0.025)(0.9774 + 0.5430)(10^6)(0.240) = 4.56 \text{ kN}$$



Ans.

**6-66.** If  $M = 6 \text{ KN.m}$ , determine the resultant force the bending stress produces on the top board A of the beam.

The moment of inertia of the cross-section about the neutral axis is

$$I = \frac{1}{12} * 300 * 380^3 - \frac{1}{12} * 260 * 300^3 = 786800000 \text{ mm}^4$$

Along the top edge of the flange  $c = y = 190 \text{ mm}$ . Thus

$$\sigma_{max} = \frac{Mc}{I} = \frac{6 * 10^6 * 190}{786800000} = \mathbf{1.45 \text{ MPa}}$$

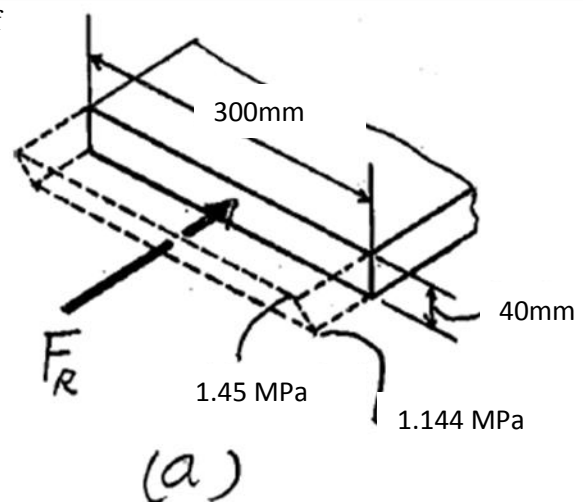
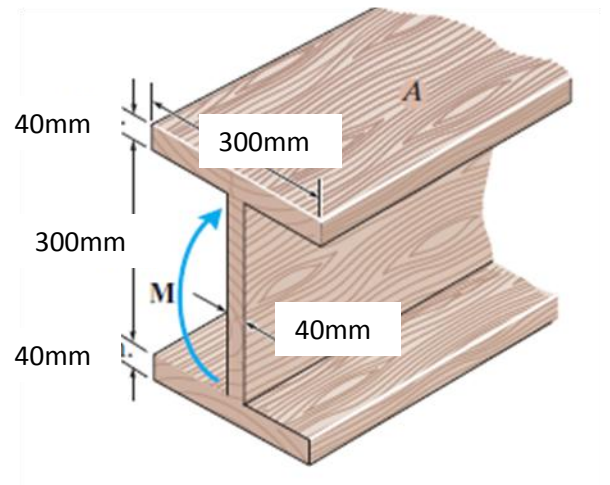
Along the bottom edge of the flange  $y = 150 \text{ mm}$ . Thus

$$\sigma_{max} = \frac{My}{I} = \frac{6 * 10^6 * 150}{786800000} = \mathbf{1.144 \text{ MPa}}$$

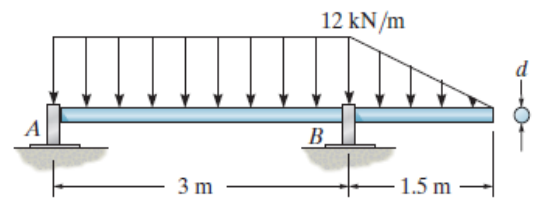
The resultant force acting on board A is equal to the volume of the trapezoidal stress block shown in Fig. a.

$$F_R = \frac{1}{2} (1.45 + 1.144) * 40 * 300$$

$$F_R = 15563.24 \text{ N}$$



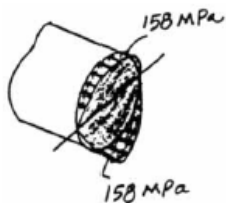
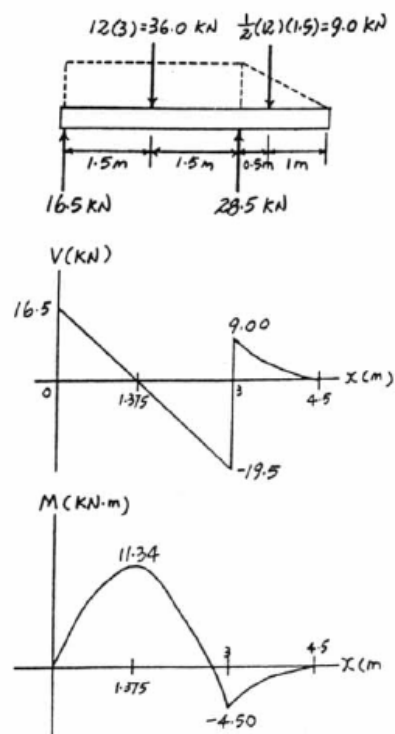
6-67. The rod is supported by smooth journal bearings at  $A$  and  $B$  that only exert vertical reactions on the shaft. If  $d = 90$  mm, determine the absolute maximum bending stress in the beam, and sketch the stress distribution acting over the cross section.



**Absolute Maximum Bending Stress:** The maximum moment is  $M_{\max} = 11.34$  kN · m as indicated on the moment diagram. Applying the flexure formula

$$\begin{aligned}\sigma_{\max} &= \frac{M_{\max} c}{I} \\ &= \frac{11.34(10^3)(0.045)}{\frac{\pi}{4}(0.045^4)} \\ &= 158 \text{ MPa}\end{aligned}$$

Ans.



\*6-76. Determine the moment  $M$  that must be applied to the beam in order to create a maximum stress of 80 MPa. Also sketch the stress distribution acting over the cross section.

The moment of inertia of the cross-section about the neutral axis is

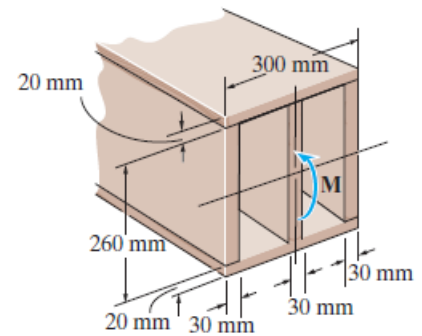
$$I = \frac{1}{12} (0.3)(0.3^3) - \frac{1}{12} (0.21)(0.26^3) = 0.36742(10^{-3}) \text{ m}^4$$

Thus,

$$\sigma_{\max} = \frac{Mc}{I}; \quad 80(10^6) = \frac{M(0.15)}{0.36742(10^{-3})}$$

$$M = 195.96 (10^3) \text{ N} \cdot \text{m} = 196 \text{ kN} \cdot \text{m}$$

The bending stress distribution over the cross-section is shown in Fig. *a*.



Ans.

