

Name: _____

Key

ID # _____

1- The two vectors A and B shown in Fig. 1 have equal magnitudes of 10.0 m. Write the resultant vector, R, of these vectors in unit vector notation, find its magnitude and the angle theta it makes with the positive x-axis.

$$A_x = 10 \cos 30 = 8.66$$

$$A_y = 10 \sin 30 = 5$$

$$B_x = 10 \cos 120 = -5$$

$$B_y = 10 \sin 120 = 8.66$$

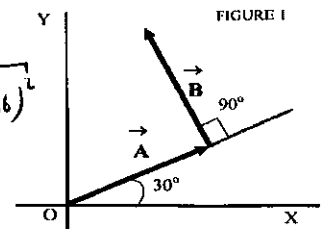
$$R_x = A_x + B_x \\ = 3.66$$

$$R_y = A_y + B_y \\ = 13.66$$

$$\vec{R} = (3.66\hat{i}) + (13.66\hat{j})$$

$$|R| = \sqrt{(3.66)^2 + (13.66)^2} \\ = 14.14$$

$$\phi = \tan^{-1} \left(\frac{13.66}{3.66} \right) = 75^\circ$$



2- Consider two vectors \vec{A} and \vec{B} with magnitudes 5 cm and 8 cm, respectively. Vector \vec{A} is along the positive x-axis and vector \vec{B} is along the positive y-axis. Find $\vec{A} \cdot (\vec{A} + \vec{B})$.

$$\vec{A} = 5\hat{i}$$

$$\vec{B} = 8\hat{j}$$

$$\vec{A} + \vec{B} = 5\hat{i} + 8\hat{j}$$

$$\vec{A} \cdot (\vec{A} + \vec{B}) = (5\hat{i}) \cdot (5\hat{i} + 8\hat{j}) \\ = \boxed{25}$$

3- Three vectors \vec{F} , \vec{v} and \vec{B} are related through $\vec{F} = 5.0(\vec{v} \times \vec{B})$. If vector $\vec{v} = 3.0\hat{i} - 5.0\hat{j}$ and $\vec{B} = -2.0\hat{k}$

Write the vector \vec{F} in unit vector notation.

$$\vec{v} \times \vec{B} = (6\hat{j} + 10\hat{i})$$

$$\vec{F} = 5(\vec{v} \times \vec{B}) = (30\hat{j} + 50\hat{i})$$

