

Instructions: Show Your Work!

1. (3 pts) Find and sketch the domain of the function

$$f(x, y) = \frac{\sqrt{y - x^2}}{1 - x^2}$$

2. (3 pts) Determine the set of the points at which the function is continuous.

$$f(x, y) = \begin{cases} \frac{xy^2}{x^3 + xy^2 + y^3} & \text{if } (x, y) \neq (0, 0) \\ 0 & \text{if } (x, y) = (0, 0) \end{cases}$$

3. (4 pts) At $(0, 0)$, find the linear approximation of the function

$$f(x, y) = e^x \cos(xy)$$

Instructions: Show Your Work!

1. (3 pts) Find and sketch the domain of the function

$$f(x, y, z) = \sqrt{4 - x^2} + \sqrt{4 - y^2} + \sqrt{1 - z^2}$$

2. (3 pts) Determine the set of the points at which the function is continuous.

$$f(x, y) = \begin{cases} \frac{xy}{x^2+xy+y^2} & \text{if } (x, y) \neq (0, 0) \\ 0 & \text{if } (x, y) = (0, 0) \end{cases}$$

3. (4 pts) At $(0, 0)$, find the linear approximation of the function

$$f(x, y) = \frac{y - 1}{x + 1}$$