

1. Find the numbers  $b$  such that the average value of  $f(x) = 2 + 6x - 3x^2$  on the interval  $[0, b]$  is equal to 3.

2. The region bounded by  $y = x^3$ ,  $y = 0$  and  $x = 1$  is rotating about  $y = 1$ . Find the *volume* of the resulted solid.

3. Find  $\int \frac{\sin \theta}{\cos^3 \theta} d\theta$

4. Find the value of  $\int_4^9 \frac{\ln y}{\sqrt{y}} dy$

5. Find the value of  $\int_0^1 \cos(\pi x) \cos(4\pi x) dx$

6. Evaluate  $I = \int e^{-\theta} \cos 2\theta d\theta$ .