

# FINAL Exam 172

MATH 513

**Quiz 1:**

Is  $F = \{(x,y,z) \in \mathbb{R}^3 : x - 2y + 3z = 0\} \cup \{(x,y,z) \in \mathbb{R}^3 : x = \ln(y+z)\}$  a subspace of  $\mathbb{R}^3$ ? Justify!

**Quiz 2:**

For what values of  $a$  and  $b$  is the matrix

$$\begin{pmatrix} 3 & a & 0 \\ -6 & 0 & 6 \\ 0 & b & -3 \end{pmatrix}$$

orthogonally diagonalizable, find the passage matrix and the diagonal matrix.

**Quiz 3:**

Verify Stoke's theorem for  $F = 3x^2yi - 4xzj + yz^2k$

a)  $S_1$  is the upper half sphere with radius  $\sqrt{2}$  and center  $(0,0,0)$ .

b)  $S_2$  is the disc of radius  $\sqrt{2}$  and center  $(0,0,0)$ .

**Quiz 4:** Let  $I := \int_{(0,0,0)}^{(1,1,1)} (2xdx + 3y^2dy + 4z^3dz)$ .

Prove that the system is conservative

Find the potential

Use the FTC to evaluate the integral