King Fahd University of Petroleum and Minerals Department of Mathematics and Statistics Math 260 - Term 172 - Quiz 4

Name:

Student ID #:

Question 1. Consider the matrix $B = \begin{bmatrix} -1 & -1 \\ -2 & 0 \end{bmatrix}$. Use Cayley Hamilton Theorem, to calculate B^2 , B^3 and B^{-1} .

QUESTION 2 IS ON THE BACK OF THE PAGE.

Question 2. Consider the matrix $A = \begin{bmatrix} 1 & 3 & 0 \\ 3 & 1 & 0 \\ 0 & 0 & -2 \end{bmatrix}$

- (a) Find the eigenvalues and the corresponding eigenvectors of the matrix A.
- (b) Find a basis and the dimension of eigenspace of each eigenvalue.
- (c) Explain why the matrix A is diagonalizable.
- (d) Find a diagonal matrix D and an invertible matrix P so that $A = PDP^{-1}$.