

Name:

KFUPM ID:

**Exercise 1**

Consider the differential equation

$$(x-1)y'' + 2y' = 0. \tag{1}$$

- (1) Find two linearly independent power series solutions around  $x_0 = 0$  of (1).
- (2) Find the general solution of the DE (1).

**Exercise 2**

Consider the differential equation

$$xy'' + y' + xy = 0. \tag{2}$$

- (1) Show that  $x_0 = 0$  is a regular singular point of the DE (2).
- (2) Find the Frobenius solution with the indicial root  $r = 0$ .