

**King Fahd University of Petroleum and Minerals**  
**Department of Mathematics and Statistics**

Math 202      Section .....      Serial #: ...      Quiz 5(a) (Term 172)

Name : ..... ID #: ..... Marks #: ...../8

1. Find regular and irregular singular points of the differential equation

$$2x(x - 2)^2 y'' + 3xy' + (x - 2)y = 0.$$

2. Solve the nonhomogeneous system

$$X' = \begin{bmatrix} 1 & 3 \\ 1 & -1 \end{bmatrix} X + \begin{pmatrix} 0 \\ t \end{pmatrix}$$

by the variation of parameters method.

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**Math 202      Section .....      Serial #: ....      Quiz 5(b) (Term 172)**

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1. For the system  $X' = \begin{bmatrix} 1 & -1 \\ 1 & -1 \end{bmatrix} X + \begin{bmatrix} \frac{1}{t} \\ \frac{1}{t} \end{bmatrix}$ ,  $X_C = c_1 \begin{bmatrix} 1 \\ 1 \end{bmatrix} + c_2 \begin{bmatrix} t+1 \\ t \end{bmatrix}$ . Find  $X_p$ .

2. Find two Frobenius solutions about regular singular point  $x = 0$  for  $2xy'' - (3 + 2x)y' + y = 0$ .

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**Math 202      Section .....      Serial #: ....      Quiz 5(c) (Term 172)**

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1. For the system  $X' = \begin{bmatrix} 2 & 0 \\ 0 & -3 \end{bmatrix} X + \begin{bmatrix} t \\ e^{-t} \end{bmatrix}$ , fundamental matrix is  $\phi(t) = \begin{bmatrix} e^{2t} & 0 \\ 0 & e^{-3t} \end{bmatrix}$ .  
Find  $X_p$ .

2. Find series solution of  $4xy'' + 2y' + y = 0$  about regular singular point  $x = 0$  corresponding to the larger indicial root.