

1. Determine whether  $\sum_{n=2}^{\infty} \frac{(n-3)(n+4)}{n(n+1)(n-1)}$  converges or diverges.

2. Determine whether  $\sum_{n=1}^{\infty} \frac{(-1)^n}{n \ln(n)}$  converges or diverges

3. Determine whether  $\sum_{n=1}^{\infty} (3^n n - 2)^{-1}$  converges or diverges

4. For the convergent alternating series  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n^4}$ , what is the smallest number of terms needed to approximate the sum within  $10^{-8}$  of its actual value?

5. Find the interval and radius of convergence for  $\sum_{n=1}^{\infty} \frac{(x+1)^{2n}}{(-4)^n n^{1/3}}$

6. Find the interval and radius of convergence for  $\sum_{n=1}^{\infty} \frac{(-1)^n (x)^{2n}}{n 4^n}$

7. Find a power series representation and its interval of convergence for

$$f(x) = \frac{3x^2}{(x-3)^2}$$

8. Determine whether  $\sum_{n=1}^{\infty} (3^{1/n} - 1)$  converges or diverges

9. Determine whether  $\sum_{n=1}^{\infty} \frac{(n!)^n}{n^{4n}}$  converges or diverges

10. Determine whether  $\sum_{n=1}^{\infty} \frac{2^{1/n}}{n^2}$  converges or diverges

11. Determine whether  $\sum \frac{1}{n + n \cdot \cos^2 n}$  converges or diverges

12. Find the sum of  $\sum_{n=1}^{\infty} \frac{n}{2^n}$

13. Find the sum of  $\frac{1}{1 \cdot 2} - \frac{1}{3 \cdot 2^3} + \frac{1}{5 \cdot 2^5} - \frac{1}{7 \cdot 2^7} \cdots$

14. Find the sum of  $\sum_{n=1}^{\infty} \frac{1}{n(n+3)}$

15. Express the repeating decimal  $4.17326326326 \dots$  as a fraction.