

Name:

ID #:

Section:

Q1: You are given:

- (i) The annual number of claims for an insured has probability function:

$$p(x) = \binom{3}{x} q^x (1 - q)^{3-x}, x = 1, 2, 3$$

- (ii) The prior density is $\pi(q) = 2q$, $0 < q < 1$.

A randomly chosen insured has zero claims in Year 1.

Using Bühlmann credibility, estimate the number of claims in Year 2 for the selected insured.

Q2: An insurer writes a large book of home warranty policies. You are given the following information regarding claims filed by insureds against these policies:

- (i) A maximum of one claim may be filed per year.
- (ii) The probability of a claim varies by insured, and the claims experience for each insured is independent of every other insured.
- (iii) The probability of a claim for each insured remains constant over time.
- (iv) The overall probability of a claim being filed by a randomly selected insured in a year is 0.10.
- (iv) The variance of the individual insured claim probabilities is 0.01.

An insured selected at random is found to have filed 0 claims over the past 10 years.

Determine the Bühlmann credibility estimate for the expected number of claims the selected insured will file over the next 5 years.

Q3: You are given:

- (i) Two risks have the following severity distributions:

Amount of Claim	Probability of Claim Amount for Risk 1	Probability of Claim Amount for Risk 2
250	0.5	0.7
2,500	0.3	0.2
60,000	0.2	0.1

- (ii) Risk 1 is twice as likely to be observed as Risk 2.
A claim of 250 is observed.

Determine the Bühlmann credibility estimate of the second claim amount from the same risk.
