

$$1. \quad \lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{5}{2n} \left(9 + \frac{4i}{n}\right)^{1/2} =$$

$$(a) \quad \frac{5}{12} (13\sqrt{13} - 27)$$

$$(b) \quad \frac{5}{12} (\sqrt{13} - 3\sqrt{3})$$

$$(c) \quad \frac{1}{12} (\sqrt{13} - 3\sqrt{3})$$

$$(d) \quad \frac{5}{12} (\sqrt{13} - 1)$$

$$(e) \quad \frac{1}{12} (1 - 3\sqrt{3})$$

$$2. \quad \int_1^2 \frac{x^2 + 1}{3x - x^2} dx =$$

$$(a) \quad -1 + \frac{11}{3} \ln 2$$

$$(b) \quad -3 + \ln 2$$

$$(c) \quad -11 + \ln \frac{3}{2}$$

$$(d) \quad \ln 2 - \ln 3$$

$$(e) \quad 2 - \ln 5$$

3. If $f(x) = \int_1^{e^x} (\ln t)^2 dt$, then $f'(\ln x) =$

(a) $x (\ln x)^2$

(b) $(\ln x)^2$

(c) $(x \ln x)^2$

(d) $x^2 \ln x$

(e) $\ln(x^2)$

4. $\int \frac{dx}{9\sqrt{x-1} + (x-1)^{3/2}} =$

(a) $\frac{2}{3} \tan^{-1} \left(\frac{\sqrt{x-1}}{3} \right) + C$

(b) $\frac{1}{3} \tan^{-1} \left(\sqrt{\frac{x}{3}} \right) + C$

(c) $\frac{2}{3} \tan^{-1} \left(\frac{\sqrt{x^2+x}}{3} \right) + C$

(d) $\frac{2}{3} \tan^{-1} \left(\sqrt{\frac{x^2-1}{3}} \right) + C$

(e) $\frac{1}{3} \tan^{-1} \left(\frac{\sqrt{x^2-1}}{3} \right) + C$

5. $\int \frac{x-1}{\sqrt{1-x^2}} dx =$

(a) $-\sqrt{1-x^2} - \sin^{-1} x + C$

(b) $\sqrt{1-x^2} - \sin^{-1} x + C$

(c) $-2\sqrt{1-x^2} - \sin^{-1} x + C$

(d) $2\sqrt{1-x^2} - \sin^{-1} x + C$

(e) $-(1-x^2) - \sin^{-1} x + C$

6. The volume of the solid obtained by rotating the region enclosed by the curves $y = x^2$ and $y = -x$ about the y -axis is

(a) $\frac{\pi}{6}$

(b) $\frac{\pi}{2}$

(c) $\frac{\pi}{4}$

(d) $\frac{2\pi}{3}$

(e) $\frac{\pi}{3}$

7. The area of the region in the first quadrant bounded on the left by the y -axis, below by the line $y = \frac{x}{4}$, above left by the curve $y = 1 + \sqrt{x}$, and above right by the curve $y = \frac{2}{\sqrt{x}}$ is:

(a) $\frac{11}{3}$

(b) 2

(c) $\frac{1}{3}$

(d) $\frac{5}{3}$

(e) $\frac{2}{3}$

8. A region bounded by the triangle with vertices $(0, 1)$, $(1, 0)$, and $(2, 0)$ is revolved about the x -axis. Then the volume of the resulting solid is

(a) $\frac{\pi}{3}$

(b) $\frac{\pi}{6}$

(c) $\frac{2\pi}{3}$

(d) $\pi - 1$

(e) $\pi - 2$

9. $\int_0^{\pi/4} \sec^4 x \tan^2 x \, dx =$

(a) $\frac{8}{15}$

(b) $\frac{2}{5}$

(c) $\frac{7}{15}$

(d) $\frac{4}{15}$

(e) $\frac{16}{15}$

10. $\int \frac{x^5}{\sqrt{1-x^4}} \, dx =$

(a) $\frac{\sin^{-1}(x^2)}{4} - \frac{x^2\sqrt{1-x^4}}{4} + C$

(b) $x^2 \sin^{-1}(x^2) - \frac{\sqrt{1-x^4}}{4} + C$

(c) $\sin^{-1}(x^2) + \frac{1}{2x^5}\sqrt{1-x^4} + C$

(d) $\sin^{-1}(x^4) - \sqrt{1-x^4} + C$

(e) $\frac{\sin^{-1}(x^2)}{4} - \frac{x^2}{4} + C$

11. $\int_0^1 \ln(x^2 + 1) dx =$

(a) $-2 + \frac{\pi}{2} + \ln 2$

(b) $-1 + \frac{\pi}{4} + \ln 2$

(c) $-1 + \frac{\pi}{3} + \ln 2$

(d) $-2 + \pi + \ln 2$

(e) $-2 + \ln 2$

12. The improper integral $\int_{-\infty}^0 x e^{4x} dx$

(a) converges to $-\frac{1}{16}$

(b) converges to $-\frac{1}{4}$

(c) diverges

(d) converges to $\frac{1}{4}$

(e) converges to 0

13. The limit of the n^{th} term of a sequence, given by

$$a_n = \frac{1}{n} \sin\left(\frac{n\pi}{4}\right) + \frac{3n^3 + 6n^2 + 1}{n^3 + n^2 + 4}, \text{ is equal to}$$

- (a) 3
- (b) $\frac{\pi}{4}$
- (c) $\frac{\pi}{2}$
- (d) $\sqrt{3}$
- (e) 9

14. The sum of $\sum_{n=2}^{\infty} 2^{n+1} \cdot 9^{\frac{1-n}{2}}$ is

- (a) 8
- (b) 1
- (c) $\frac{2}{3}$
- (d) $\frac{4}{3}$
- (e) $\frac{2}{9}$

15. The number of terms of the series $\sum_{n=2}^{\infty} \frac{1}{n(\ln n)^2}$, we need to add to ensure that the sum is accurate to within 0.01 is n bigger than

(a) e^{100}

(b) e^{10}

(c) 100

(d) 10

(e) $\ln 10$

16. The series $\sum_{n=1}^{\infty} \left(\frac{1}{3}\right)^{\frac{1}{n^3}}$ is

(a) divergent

(b) convergent

(c) convergent by alternating series test

(d) convergent and its sum is $\frac{1}{3}$

(e) conditionally convergent

17. The series $\sum_{n=1}^{\infty} \frac{1}{n^{1+\frac{100}{n}}}$ is

- (a) divergent by the limit comparison test
- (b) convergent by the limit comparison test
- (c) convergent and its sum is $\frac{1}{100}$
- (d) divergent by the divergent series test
- (e) convergent by the integral test.

18. The series $\sum_{n=1}^{\infty} (-1)^{n-1} \frac{e^{\frac{1}{n}}}{n}$ is

- (a) convergent by alternating series test
- (b) divergent by the integral test
- (c) divergent by the ratio test
- (d) convergent by the root test
- (e) divergent by alternating series test

19. By applying the ratio test to the series

$$\sum_{n=0}^{\infty} \frac{n!}{\alpha(\alpha+1)(\alpha+2)\dots(\alpha+n-1)}, \quad \alpha > 0,$$

- (a) the test fails
- (b) the series convergent, but not absolutely convergent
- (c) the series converges
- (d) the series diverges
- (e) the series converges absolutely

20. Which of the following statements is **TRUE**?

- (a) $\sum_{n=1}^{\infty} \left(1 + \frac{1}{n}\right)^{-n^2}$ converges
- (b) $\sum_{n=2}^{\infty} (-1)^n \frac{1}{n \ln n}$ converges absolutely
- (c) If a series $\sum_{n=1}^{\infty} a_n$ converges, then $\sum_{n=1}^{\infty} \frac{a_n}{n}$ converges absolutely
- (d) If $\sum_{n=1}^{\infty} (a_n + b_n)$ converges absolutely, then both $\sum_{n=1}^{\infty} a_n$ and $\sum_{n=1}^{\infty} b_n$ are convergent
- (e) $\sum_{n=1}^{\infty} (-1)^n \frac{\sin\left(\frac{1}{n}\right)}{n}$ converges conditionally

21. The radius of convergence R and the interval of convergence I of the power series $\sum_{n=0}^{\infty} \frac{3^n}{(n+1)^2} (2x-1)^n$ are

(a) $R = \frac{1}{6}, I = \left[\frac{1}{3}, \frac{2}{3}\right]$

(b) $R = \frac{1}{6}, I = \left[\frac{1}{3}, \frac{2}{3}\right)$

(c) $R = \frac{1}{6}, I = \left(\frac{1}{3}, \frac{2}{3}\right)$

(d) $R = \frac{1}{3}, I = \left[\frac{1}{6}, \frac{5}{6}\right]$

(e) $R = \frac{1}{3}, I = \left[\frac{1}{6}, \frac{5}{6}\right)$

22. $\sum_{n=2}^{\infty} n \left(\frac{1}{3}\right)^n =$

(a) $\frac{5}{12}$

(b) $\frac{3}{4}$

(c) 2

(d) $\frac{23}{12}$

(e) $\frac{3}{2}$

$$23. \quad \frac{\pi}{2} \sum_{n=0}^{\infty} (-1)^n \frac{\pi^{2n}}{4^n (2n+1)!} =$$

(a) 1

(b) 0

(c) $\frac{\pi}{2}$

(d) $\frac{\pi}{4}$

(e) -1

24. Let $f(x) = x \cos(x^2)$. Then $f^{(17)}(0) =$

(a) $\frac{17!}{8!}$

(b) $\frac{1}{8!}$

(c) $\frac{1}{10!}$

(d) $\frac{16!}{9!}$

(e) $\frac{16!}{4!}$

25. The arc length along the curve $y = x^2 - \frac{1}{8} \ln x$ from $(1, 1)$ to $\left(e, e^2 - \frac{1}{8}\right)$ is

(a) $e^2 - \frac{7}{8}$

(b) $e - \frac{7}{8}$

(c) $e^2 - 1$

(d) $e^2 - \frac{1}{8}$

(e) $e^2 - 7$

26. The area of the surface obtained by rotating the curve $y = \sqrt{x}$, $2 \leq x \leq 3$ about the x -axis is

(a) $\frac{\pi}{6} (13\sqrt{13} - 27)$

(b) $\frac{\pi}{6} (13\sqrt{13} - 3\sqrt{3})$

(c) $\frac{\pi}{6} (\sqrt{13} - 27)$

(d) $\frac{\pi}{6} (\sqrt{13} - 3\sqrt{3})$

(e) $\frac{\pi}{6} (\sqrt{13} - 9\sqrt{3})$

27. The series $\sum_{n=1}^{\infty} \frac{n}{e^{n^2}}$

- (a) converges by the integral test
- (b) converges by the alternating series test
- (c) diverges by the divergence test
- (d) diverges by the ratio test
- (e) converges as a p – series

28. The series $\sum_{n=1}^{\infty} \frac{1}{(n^2 + n)^p}$ is convergent if

- (a) $p > \frac{1}{2}$
- (b) $p = \frac{1}{2}$
- (c) $p < \frac{1}{2}$
- (d) $p = \frac{1}{4}$
- (e) $p < \frac{1}{4}$