

KING FAHD UNIVERSITY OF PETROLEUM & MINERALS
DEPARTMENT OF MATHEMATICS & STATISTICS
STAT 319.05 Quiz #3

Name: _____ ID #: _____

1) Let c be a constant and consider the density function $f(x) = \begin{cases} c(2-x) & \text{if } 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$.

a) Find the value of c .

b) Find the cumulative distribution function.

- 2) The amount of time X in minutes that a train is late is a continuous random variable with probability density $f(x) = \begin{cases} \frac{3}{500}(25 - x^2) & \text{if } -5 \leq x \leq 5 \\ 0 & \text{otherwise} \end{cases}$.

Find the mean and variance of the amount of time the train is late.

- 3) The life of a semiconductor laser at a constant power is normally distributed with a mean of 7000 hours and a standard deviation of 600 hours.
- a) What is the probability that a laser fails before 6000 hours?

b) What is the life in hours that 95% of the lasers exceed?

- 4) The time between calls is exponentially distributed with a mean of 5 minutes.
- a) What is the probability that the time until the first call is less than 5 minutes?

 - b) What is the probability that the time until the first call is between 5 and 15 minutes?

 - c) Determine the length of interval of time such that the probability of at least one call in the interval is 0.9.

 - d) If there has not been a call in 10 minutes, what is the probability that the time until the next call is less than 5 minutes?

 - e) What is the probability that there are no calls in the interval from 10:00 am to 10:05 am?