

ID #: _____ Name: _____ Quiz 5 (MATH 202) Serial: _____

Q1. If $y = \sum_{n=0}^{\infty} c_n x^n$ is a power series solution of the LDE $(1-x^2)y'' - 2xy' + 4y = 0$ about the ordinary point $x = 0$, find the recurrence relation that determines c_n .

Q2. (i) Find the indicial equation (without solving the LDE) of the LDE: $xy'' - (3 - 2x^2)y' - \frac{5}{x}y = 0$ about the regular singular point $x = 0$, and find its roots.

(ii) Considering the roots in (i), state the nature of both series solutions of the above LDE .

Q.3 (i) Find the singular points of of the LDE: $x^3(x^2 - 25)^2 y'' + 3x^2(x + 5)y' + 7y = 0$.

(ii) Classify each singular point obtained in (i) as regular or irregular. (Show all steps)

Q.4. Setting $y = \sum_{n=0}^{\infty} c_n x^n$ in the LDE $y'' - xy' - x^2 y = 0$ gives us $2c_2 + 6c_3 x - c_1 x + \sum_{k=2}^{\infty} [(k+1)(k-1)c_k + (k+2)(k-1)c_{k+2}] x^k = 0$.

Find One Power Series solution of the LDE about the Ordinary Point $x = 0$.

Q.1. If $y = \sum_{n=0}^{\infty} c_n x^n$ is a power series solution of the LDE $y'' - xy' - x^2y = 0$ about the ordinary point $x = 0$, find the recurrence relation and other relations that determine all c_n 's.

Q.2. (i) Find the singular points of of the LDE: $x^3(x-4)(x-2)^2 y'' + 3x(x-2)y' + 7(x-4)y = 0$.

(ii) Classify each singular point obtained in (i) as regular or irregular. (Show all steps)

Q.3. Find the radius of convergence of a power series solution of the LDE about its ordinary point $x = 4$:

$$(x-2)(x^2+9)y'' + xy' - y = 0$$

Q.4. Setting $y = \sum_{n=0}^{\infty} c_n x^{n+r}$ in the LDE $2xy'' + (1+x)y' + y = 0$ gives us

$$x^r \left[r(2r-1)c_0 x^{-1} + \sum_{k=0}^{\infty} [(k+r+1)(2k+2r+1)c_{k+1} + (k+r+1)c_k] x^k \right] = 0.$$

(i) Find the Indicial Equation and its roots:

(ii) Find the Recurrence Relation:

(iii) Find the Frobenius solution for the larger root of indicial equation.