

# King Fahd University of Petroleum and Minerals

Department of Mathematics and Statistics

Spring Semester (Term 162)

Final Exam

## MATH 132

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Serial Number \_\_\_\_\_

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MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Provide an appropriate response.

1)  $\lim_{x \rightarrow 1} \frac{2x^2 + x - 3}{x^2 + 4x - 5} =$  1) \_\_\_\_\_

- A) 0                      B)  $\frac{2}{5}$                       C)  $\frac{5}{6}$                       D)  $\frac{1}{4}$                       E)  $\frac{3}{5}$

2) If  $f(x) = \begin{cases} x, & \text{if } x \geq 2 \\ 2 - x, & \text{if } x < 2 \end{cases}$ , then  $\lim_{x \rightarrow 2} f(x) =$  2) \_\_\_\_\_

- A) 0  
B) 1  
C) 2  
D)  $\infty$   
E) does not exist

3) Let  $f(x) = \frac{x^2 - 9}{x^2 + 2x + 1}$ . The only value(s) of  $x$  for which  $f$  is discontinuous is (are) 3) \_\_\_\_\_

- A) -1.  
B) 1, -3 and 3.  
C) -1, 1, -3, and 3.  
D) -1 and 1.  
E) -3 and 3.

4) By direct use of the definition of a derivative, the derivative of  $f(x) = \frac{1}{x}$  is 4) \_\_\_\_\_

- A)  $\lim_{h \rightarrow 0} \frac{1}{x+h}$ .  
B)  $\lim_{h \rightarrow 0} \frac{\frac{1}{x+h} - \frac{1}{x}}{h}$ .  
C)  $\lim_{h \rightarrow 0} \left[ \frac{1}{x+h} + \frac{1}{x} \right]$ .  
D)  $\lim_{h \rightarrow 0} \frac{1}{h}$ .  
E)  $\frac{1}{x^2}$ .

5) A value of  $x$  for which the slope of the curve  $y = \frac{x^3}{3} - \frac{3x^2}{2} + 2x + 1$  is zero is 5) \_\_\_\_\_

- A) -1.                      B) 2.                      C) 3.                      D) 0.                      E) -2.

6) If  $g(x) = x^4(2x - 1)^{10}$ , then  $g'(1) =$  6) \_\_\_\_\_

- A) 14.                      B) 80.                      C) 24.                      D) 0.                      E) 1.

7) If  $f(x) = \frac{x^2 + 4}{x^2 - 2}$ , then  $f'(x) =$  7) \_\_\_\_\_

A)  $-\frac{12x}{(x^2 - 2)^2}$   
 B)  $\frac{12x}{(x^2 + 2)^2}$   
 C)  $\frac{6}{(x^2 - 2)^2}$   
 D) 1  
 E)  $\frac{4x + 26x - 9x^2}{(3x + 2)^2}$

8) If  $7x^2 + 4y^2 = 1$ , then  $\frac{dy}{dx} =$  8) \_\_\_\_\_

A)  $7x + 4y$ .      B)  $\frac{1 - 14x}{8y}$ .      C)  $14x + 8y$ .      D)  $\frac{4y}{7x}$ .      E)  $-\frac{7x}{4y}$ .

9) If  $f(x) = x^{3x} + 1$ , then  $f'(x) =$  9) \_\_\_\_\_

A)  $\frac{3x + 1}{x} + 3 \ln x$ .  
 B)  $(3x + 1)x^{3x}$ .  
 C)  $(2x + \ln x)x^{3x + 1}$ .  
 D)  $(\ln x)x^{3x}$ .  
 E)  $x^{3x} + 1 \left[ \frac{3x + 1}{x} + 3 \ln x \right]$ .

10) The function  $f(x) = x^2 - 6x + 8$  is decreasing on 10) \_\_\_\_\_

A)  $(3, \infty)$ .  
 B)  $(-\infty, 3)$ .  
 C)  $(2, 4)$ .  
 D)  $(-\infty, 2)$  and  $(4, \infty)$ .  
 E)  $(-3, 3)$ .

11) The function  $y = x^3 + 15x^2 - 33x$  has a relative maximum when  $x =$  11) \_\_\_\_\_

A) 11      B) 0.      C) -1.      D) -11.      E) 1.

12) On the interval  $[-1, 1]$ , the function  $y = 4 + x^2 - x^3$  has an absolute maximum when  $x =$  12) \_\_\_\_\_

A) -1.      B) 1.      C)  $\frac{1}{2}$ .      D) 0.      E)  $-\frac{1}{2}$ .

13) If  $f(x) = x^4 - 6x^2 + 3$ , then  $f$  has an inflection point when  $x =$  13) \_\_\_\_\_

A) 2.      B) 3.      C)  $\sqrt{3}$ .      D) 0.      E) 1.

14) An equation of a horizontal asymptote for the graph of  $y = \frac{2x}{9x^2 - 1}$  is 14) \_\_\_\_\_

A)  $x = \frac{2}{9}$ .

B)  $x = \frac{1}{3}$ .

C)  $y = 0$ .

D)  $y = \frac{1}{3}$ .

E)  $y = \frac{2}{9}$ .

15) If  $f(x) = x^3 - 7x^2 + 2x - 5$ , then  $f$  is concave down on the interval 15) \_\_\_\_\_

A)  $\left(-\infty, \frac{7}{3}\right)$ .

B)  $\left(\frac{2}{3}, \infty\right)$ .

C)  $\left(\frac{7}{3}, \infty\right)$ .

D)  $\left(-\infty, \frac{2}{3}\right)$ .

E)  $(-\infty, \infty)$ .

16) If  $f(x) = x^3 + 3x^2 - 24x + 8$ , then  $f$  is 16) \_\_\_\_\_

A) increasing on  $(2, \infty)$ , concave up on  $(-\infty, -1)$ , and has a relative minimum when  $x = 2$ .

B) increasing on  $(-4, 2)$ , concave down on  $(-\infty, \infty)$ , and has a relative maximum when  $x = 2$ .

C) decreasing on  $(-4, 2)$ , concave down on  $(-\infty, -1)$ , and has a relative maximum when  $x = -4$ .

D) decreasing on  $(1, 2)$ , concave up  $(0, \infty)$ , and has a relative minimum when  $x = -4$ .

E) decreasing on  $(-\infty, 4)$ , concave up on  $(-1, \infty)$ , and has no relative minimum point.

17) If  $y = x \ln x$ , then  $dy =$  17) \_\_\_\_\_

A)  $(x + \ln x) dx$ .

B)  $1 + \ln x$ .

C)  $x + \ln x$ .

D)  $(1 + \ln x) dx$ .

E) none of the above

18) If  $\frac{dy}{dx} = 3x^2 - 3 - 4e^{2x}$  and  $y(0) = 8$ , then  $y =$  18) \_\_\_\_\_

A)  $x^3 - 3x - 2e^{2x} + 8$ .

B)  $x^3 - 3x - 2e^{2x}$ .

C) 8.

D)  $x^3 - 3x - 4e^{2x}$ .

E)  $x^3 - 3x - 2e^{2x} + 10$ .

19)  $\int e^{3x+4} dx =$  19) \_\_\_\_\_

A)  $\frac{e^{3x+5}}{3x+5} + C$

B)  $e^{3x+4} + C$

C)  $(3x+4)e^{3x+3} + C$

D)  $\frac{1}{3}e^{3x+4} + C$

E)  $3e^{3x+4} + C$

Evaluate the integral by using a substitution prior to integration by parts.

20)  $\int \cos(\ln x) dx$  20) \_\_\_\_\_

A)  $x[\cos(\ln x) + \sin(\ln x)] + C$

B)  $x \cos(\ln x) + \sin(\ln x) + C$

C)  $\frac{x}{2}[\cos(\ln x) + \sin(\ln x)] + C$

D)  $\frac{x}{2}[\cos(\ln x) - \sin(\ln x)] + C$

Provide an appropriate response.

21)  $\int \frac{x^2 + 4x - 3}{x - 1} dx =$  21) \_\_\_\_\_

A)  $\frac{1}{3} \ln|x - 1| + C$

B)  $\frac{x^2}{2} + 5x + 2 \ln|x - 1| + C$

C)  $\frac{x^2}{2} + 6x + 3 \ln|x - 1| + C$

D)  $\frac{7x^2}{2} - 2x + C$

E)  $\frac{1}{2} \ln|x - 1| + C$

22)  $\int \frac{4x}{x^2 + 1} dx =$  22) \_\_\_\_\_

A)  $\ln(x^2 + 1) + C$

B)  $4 \ln|x + 1| + C$

C)  $\frac{1}{2} \ln(x^2 + 1) + C$

D)  $\frac{2}{x} + C$

E)  $2 \ln(x^2 + 1) + C$

23)  $\int_{-2}^0 \frac{1}{\sqrt{1 - 4x}} dx =$  23) \_\_\_\_\_

A) 1

B) 2

C) 3

D) 4

E) 5

24)  $\int_{-1}^0 4(x + 1)e^{(x+1)^2} dx =$  24) \_\_\_\_\_

A)  $2(e - 1)$

B)  $1 - e$

C) 0

D)  $\frac{1}{2}(e - 1)$

E)  $e(3e - 2)$

25) The exact area of the region bounded by the graphs of  $y = x$  and  $y = x^2$  is 25) \_\_\_\_\_

A)  $\frac{5}{6}$  sq unit.

B)  $\frac{1}{6}$  sq unit.

C)  $\frac{1}{2}$  sq unit.

D)  $\frac{2}{3}$  sq unit.

E)  $\frac{1}{3}$  sq unit.

26)  $\int_1^2 x \ln(x) dx =$  26) \_\_\_\_\_

A)  $2 \ln(2) - \frac{3}{4}$       B)  $\frac{\ln(2)^2}{4}$       C)  $\ln(2) - 4$       D)  $4 \ln(2) - \frac{1}{4}$       E)  $4 \ln 2$

27) The function  $f(x, y) = \frac{1}{3}x^3 + \frac{1}{2}y^2 + xy - 6x + 3$  has a relative minimum at 27) \_\_\_\_\_

A)  $(-2, 2)$ .      B)  $(2, -2)$ .      C)  $(2, 2)$ .      D)  $(3, -3)$ .      E)  $(-3, 3)$ .

28) The number of critical points of  $f(x, y) = x^2 + x^2y + y^2 - 2y + 2$  is 28) \_\_\_\_\_

A) 0.      B) 1.      C) 2.      D) 3.      E) 4.

Find all the first order partial derivatives for the following function.

29)  $f(x, y, z) = xe^{(x^2 + y^2 + z^2)}$  29) \_\_\_\_\_

A)  $\frac{\partial f}{\partial x} = 2x^2e^{(x^2 + y^2 + z^2)}$ ;  $\frac{\partial f}{\partial y} = xy e^{(x^2 + y^2 + z^2)}$ ;  $\frac{\partial f}{\partial z} = 2xz e^{(x^2 + y^2 + z^2)}$

B)  $\frac{\partial f}{\partial x} = (1 + 2x^2) e^{(x^2 + y^2 + z^2)}$ ;  $\frac{\partial f}{\partial y} = xe^{(x^2 + y^2 + z^2)}$ ;  $\frac{\partial f}{\partial z} = xe^{(x^2 + y^2 + z^2)}$

C)  $\frac{\partial f}{\partial x} = (1 + 2x^2) e^{(x^2 + y^2 + z^2)}$ ;  $\frac{\partial f}{\partial y} = xy^2 e^{(x^2 + y^2 + z^2)}$ ;  $\frac{\partial f}{\partial z} = xz^2 e^{(x^2 + y^2 + z^2)}$

D)  $\frac{\partial f}{\partial x} = (1 + 2x^2) e^{(x^2 + y^2 + z^2)}$ ;  $\frac{\partial f}{\partial y} = 2xy e^{(x^2 + y^2 + z^2)}$ ;  $\frac{\partial f}{\partial z} = 2xz e^{(x^2 + y^2 + z^2)}$

Find all the second order partial derivatives of the given function.

30)  $f(x, y) = e^{x/y}$  30) \_\_\_\_\_

A)  $\frac{\partial^2 f}{\partial x^2} = \frac{e^{x/y}}{y^2}$ ;  $\frac{\partial^2 f}{\partial y^2} = e^{x/y} \left\{ \frac{x^2 + 2xy}{y^3} \right\}$ ;  $\frac{\partial^2 f}{\partial y \partial x} = \frac{\partial^2 f}{\partial x \partial y} = -e^{x/y} \left( \frac{y+x}{y^3} \right)$

B)  $\frac{\partial^2 f}{\partial x^2} = \frac{e^{x/y}}{y^2}$ ;  $\frac{\partial^2 f}{\partial y^2} = e^{x/y} \left\{ \frac{x^2 + 2xy}{y^4} \right\}$ ;  $\frac{\partial^2 f}{\partial y \partial x} = \frac{\partial^2 f}{\partial x \partial y} = -e^{x/y} \left( \frac{y+x}{y^3} \right)$

C)  $\frac{\partial^2 f}{\partial x^2} = \frac{e^{x/y}}{y^2}$ ;  $\frac{\partial^2 f}{\partial y^2} = -e^{x/y} \left\{ \frac{x^2 + 2xy}{y^3} \right\}$ ;  $\frac{\partial^2 f}{\partial y \partial x} = \frac{\partial^2 f}{\partial x \partial y} = e^{x/y} \left( \frac{y+x}{y^3} \right)$

D)  $\frac{\partial^2 f}{\partial x^2} = \frac{e^{x/y}}{y^2}$ ;  $\frac{\partial^2 f}{\partial y^2} = \left\{ \frac{x^2 + 2xy}{y^4} \right\}$ ;  $\frac{\partial^2 f}{\partial y \partial x} = \frac{\partial^2 f}{\partial x \partial y} = \frac{y+x}{y^3}$