

King Fahd University of Petroleum and Minerals
Department of Mathematics and Statistics
Math605-01 / Instructor: Prof. Bilal Chanane
Major Exam II Duration 2hrs

Name:.....ID:.....

Question	Points	Mark
1	30	
2	30	
3	40	
Total	100	

Exercise 1 Use the WKB method to find asymptotic approximations of the eigenvalues μ^2 and corresponding eigenfunctions for large values of μ^2 for the following eigenvalue problem

$$\begin{cases} -\frac{d^2y}{dx^2} = \mu^2 xy, & 0 < x < 1 \\ \lim_{x \rightarrow 0^+} y(x) = 0, & y(1) = 0 \end{cases}$$

Exercise 2 Find the asymptotic solution of

$$\begin{cases} y'' + y' + \epsilon y^2 = 0, & x > 0 \\ y(0) = 1, & y'(0) = 0 \end{cases}$$

where ϵ is a small parameter.

Exercise 3 Use the method of stationary phase to obtain the leading asymptotic behaviour as $x \rightarrow \infty$ of

$$g(x) = \int_0^1 \exp(ix \{t - \sin t\}) dt$$