

**Instructions:** Show Your Work!

1. (5 pts) Suppose that  $f$  is a differentiable function of  $x$  and  $y$  and

$$g(s, t) = f(e^s + \sin t, e^s + \cos t).$$

Use the table of values to calculate  $g_s(0, 0)$  and  $g_t(0, 0)$ .

	$f$	$g$	$f_x$	$f_y$
$(0, 0)$	3	6	4	8
$(1, 2)$	6	3	2	5

2. (5 pts) Show that every normal line to the sphere

$$x^2 + y^2 + z^2 = 9$$

passes through the center of the sphere.

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**Instructions:** Show Your Work!

1. (5 pts) Suppose that  $f$  is a differentiable function of  $x$  and  $y$  and

$$g(s, t) = f(2s - t, t^2 - 4s).$$

Use the table of values to calculate  $g_s(1, 2)$  and  $g_t(1, 2)$ .

	$f$	$g$	$f_x$	$f_y$
(0, 0)	3	6	4	8
(1, 2)	6	3	2	5

2. (5 pts) Show that the sum of the  $x$ -,  $y$ -, and  $z$ -intercepts of any tangent plane to the surface

$$\sqrt{x} + \sqrt{y} + \sqrt{z} = \sqrt{k}$$

is a constant.