King Fahd University of Petroleum and Minerals Department of Mathematics and Statistics Math 101 Major Quiz 2

Name : Sec# Sec# Serial #:

Question 1[6 points]: Please, find the following limits:)

1.
$$\lim_{x\to 5^-} [|3x|] + [|-3x|]$$

2.
$$\lim_{x\to 2} \frac{x^3-8}{2x^2-x-6}$$

3.
$$\lim_{x\to 1^-} \frac{|x^2-3x+2|}{x\sqrt{x}-\sqrt{x}}$$

Question 2 [3 points]: Use the Sandwich (Squeeze) Theorem to calculate the limit,

$$\lim_{x \to 0} \tan(\pi x) \cos\left(\frac{\pi}{x}\right).$$

Question 3 [3 points]: Use the Intermediate Value Theorem to show that the equation, $x^x = 3x - 1$, has a solution.

Question 4 [4 points]: Use limits to find the horizontal and vertical asymptotes of the curve,

$$g(x) = \frac{x^2 - 5x + 6}{4 - x^2}.$$

Question 5 [4 points]: Consider the curve, $f(x) = \sqrt{2x+5}$.

a) Use limits to find the derivative of f.

b) Find the equation of the tangent line to the curve at x = -2.