

Name: \_\_\_\_\_ ID #: \_\_\_\_\_ Serial #: \_\_\_\_\_

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1. Let  $A = \begin{bmatrix} 1 & 8 \\ 0 & 2 \end{bmatrix}$ . Use diagonalization to find  $A^{10}$ .

2. Let  $A = \begin{bmatrix} 3 & -1 \\ 5 & -3 \end{bmatrix}$ ,  $x_1 = e^{-2t} \begin{bmatrix} 1 \\ 5 \end{bmatrix}$ , and  $x_2 = e^{2t} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$

- (a) Verify that  $x_1$  is a solution of  $Y' = AY$ .
- (b) Given that  $x_2$  is also a solution of  $Y' = AY$ , verify that  $x_1$  and  $x_2$  are linearly independent.
- (c) Write the general solution of the system  $Y' = AY$ .