

Q1. Two solutions of the differential equation  $x^2 y'' - xy' + y = 0$  are  $y_1 = x$  and  $y_2 = x \ln x$ . Do the following:

(a): Verify that  $y_2 = x \ln x$  satisfies the differential Equation.

(b): Construct general solution of the differential equation.

(c): Find a particular solution of the differential equation that satisfies initial conditions  $y(1) = 7$ ,  $y'(1) = 2$ .

(d): Find an interval over which the solutions are linearly independent.

Q2. Find general solutions of

(a):  $y'' + 2y' + y = 0$

(b):  $y'' + 4y' + 3y = 0$  and

(c):  $y^{(4)} + 18y^{(2)} + 81y = 0$