

NAME:

S.No.

ID:

Maximum Marks: 8

Section:

Time Allowed: 25 minutes

(1)(a) Find  $f'_-(4)$  and  $f'_+(4)$  for the function  $f(x) = \begin{cases} 0 & x \leq 0 \\ 5 - x & 0 < x < 4 \\ \frac{1}{5 - x} & x \geq 4. \end{cases}$

(b) Sketch the graph of the function  $f$ .

(2) For what values of  $a$  and  $b$  is the line  $2x + y = b$  tangent to the parabola  $y = ax^2$  when  $x = 2$  ?

(3) If  $f(x) = \frac{x^2 - 1}{e^x(x^2 + 1)}$ , find  $f'(x)$ .