King Fahd University of Petroleum and Minerals
Department of Mathematics and Statistics
STAT-361 Operations Research I [1]
Final Exam
Four Problems, May 16th, 2015 [2]

Problem 1 (**30 pts**)

Consider the following linear program (P):

$$\min_{x_1,x_2} \quad x_1 + 4x_2$$
$$\text{s.t.} \quad x_1 + 3x_2 \geq 4,$$
$$3x_1 + x_2 \geq 4,$$
$$x_1, x_2 \geq 0.$$

(a) Solve the linear program (P) graphically. (10 points)

(b) Formulate the dual linear program (D) associated to the program (P). (5 points)

(c) Solve the linear program (D) graphically. (10 points)

Problem 2 **(25 Points)**

Consider the following transportation problem. The problem involves 3 plants supplying 4 customer zones. The following table 1 displays the unit transportation costs, the supplies and the demands. Find the optimal solution to this problem.

Demand Nodes →	1	2	3	4	
Supply Nodes ↓			Costs		Offer
1	3	3	4	6	1000
2	6	4	5	6	900
3	5	5	5	4	1100
Demand	800	700	900	600	

Table 1: Data for problem 2

You can use the following tables. You have to use **Vogel** initialization method, otherwise you are subject to −5 points.

Interation 1

Demand Nodes	1	2	3	4	
1					1000
2					900
3					1100
Demand	800	700	900	600	

Interation 2

Demand Nodes	1	2	3	4	
1					1000
2					900
3					1100
Demand	800	700	900	600	

Interation 3

Demand Nodes	1	2	3	4	
1					1000
2					900
3					1100
Demand	800	700	900	600	

Interation 4

Demand Nodes	1	2	3	4	
1					1000
2					900
3					1100
Demand	800	700	900	600	

Interation 5

Demand Nodes	1	2	3	4	
1					1000
2					900
3					1100
Demand	800	700	900	600	

Problem 3 (**25 pts**)

Consider the following linear program:

$$\max_{x_1,x_2,x_3} \quad 2x_1 + 2x_2 + 3x_3$$

$$\text{s.t.} \quad x_1 + x_2 + 2x_3 \leq 5,$$
$$x_1 + x_2 + x_3 \geq 3,$$
$$2x_1 + x_2 + x_3 \geq 3,$$
$$x_1, x_2, x_3 \geq 0.$$

(a) Solve the linear program using the Primal Simplex algorithm.(12.5 pts)

(b) Solve the linear program using the Dual Simplex algorithm.(12.5 pts)

Problem 4 (**25 pts**)

Consider the following project scheduling problem detailed in table 2.

Tasks	Condition	Duration (days)
a	–	4
b	–	4
c	after b	5
d	after a	6
e	after c and d	4
f	after d	5
g	after f	6
h	after e and f	6
i	after g	5
k	after g and i	4

Table 2: Data for problem 4

(i).Draw the graph representing the interdependence between the tasks of the project. (10 pts)
(ii).Find the shortest possible duration of the project. (10 pts)
(iii).Find the critical tasks and the critical tasks. (5 pts)