## King Fahd University of Petroleum and Minerals Department of Mathematics and Statistics STAT-361 Operations Research I <sup>1</sup> MidTerm Exam I

Three Problems, March  $12^{th},\,2015$   $^2$ 

## Problem 1 (30 pts)

Given the following linear program:

 $\min_{\substack{x_1, x_2 \\ \text{s.t.}}} 2x_1 + 3x_2 \\ x_1 + 2x_2 \le 4, \\ 2x_1 + x_2 \ge 3, \\ x_1, x_2 \ge 0.$ 

(a) Solve the linear program graphically. (10 points)

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<sup>&</sup>lt;sup>2</sup>This is NOT an open book exam. The exam lasts 90 minutes.

(b) If the objective function coefficient  $c_1$  of  $x_1$  is changing, for which values of  $c_1$  the solution obtained in (a) would remain optimal? Explain. (5 points)

(c) If the objective function coefficient  $c_2$  of  $x_2$  is changing, for which values of  $c_2$  the solution obtained in (a) would remain optimal? Explain. (5 points)

(d) If the right hand side  $b_1$  of constraint 1 is changing, for which values of  $b_1$  the solution structure obtained in (a) remain optimal? Explain. (5 points)

(e) If the right hand side  $b_2$  of constraint 2 is changing, for which values of  $b_2$  the solution structure obtained in (a) remain optimal? Explain. (5 points)

## Problem 2 (35 pts)

Consider the following linear program:

 $\max_{\substack{x_1, x_2, x_3 \\ \text{s.t.}}} x_1 + 3x_2 + 2x_3$ s.t.  $2x_1 + x_2 + x_3 \le 4,$  $x_1 + 2x_2 + x_3 \ge 4,$  $x_1 + x_2 + 2x_3 \le 4,$  $x_1, x_2, x_3 \ge 0.$ 

(a) Solve the linear program using the Simplex algorithm. (20 points)

(b) If the objective function coefficient  $c_1$  of  $x_1$  is changing, for which values of  $c_1$  the solution obtained in (a) would remain optimal? Explain. (5 points)

(c) If the objective function coefficient  $c_2$  of  $x_2$  is changing, for which values of  $c_2$  the solution obtained in (a) would remain optimal? Explain. (5 points)

(d) If the objective function coefficient  $c_3$  of  $x_3$  is changing, for which values of  $c_3$  the solution obtained in (a) would remain optimal? Explain. (5 points)

## Problem 3 (35 Points)

The following Simplex tableau corresponds to the representation of a basic feasible solution of a linear program during its optimization.

$c^t$	?	?	?	0	0	0		
Basis	$x_1$	$x_2$	$x_3$	$e_1$	$e_2$	$e_3$	$b_j$	$\frac{b_j}{c_{pj}}$
$x_1$	1	2	0	1	0	0	2	
$e_2$	0	-1	0	-2	1	1	1	
$x_3$	0	2	1	0	0	4	3	
RC	0	3	0	-1	0	4		

(a) Complete the missing values in the Tableau.(5 points)

(b) Peform a single pivot iteration in case the objective has to be maximized. (10 points)

(c) Peform a single pivot iteration in case the objective has to be minimized. (10 points)

(d) Give a possible original expression of the linear program.(10 points)

END