

**Problem 1:** (10 points) Find the limit if it exists. If it does not exist, show why. Use the symbols  $\infty$  or  $-\infty$  as appropriate.

(i)  $\lim_{x \rightarrow 3^+} \frac{x^2 + x - 12}{\sqrt{x} - 3}$

(ii)  $\lim_{x \rightarrow \infty} \sqrt{x^2 + x} - x$

**Problem 2:** (5 points) Find all values of  $C$  which will make the following function continuous.

$$f(x) = \begin{cases} Ax - x^2 & \text{if } x \leq 1, \\ 2x + 3 & \text{if } x > 1. \end{cases}$$

**Problem 3:** (5 points) Use the definition of the derivative to find  $f'(2)$  for the function  $f(x) = x^2 - x$ .

**Problem 4:** (15 points) Find  $f'(x)$  for each function:

(a)  $f(x) = (2x + 1)(x^2 - x^3)$

(b)  $f(x) = \frac{2x + 1}{x^2 - x^3}$

(c)  $f(x) = (x^2 - x)^5$

**Problem 5:** (5 points) Find the **equation of the tangent** line to the curve  $y = \frac{4}{\sqrt{9x^2 + 1}}$  at  $x = 1$ .