King Fahd University of Petroleum and Minerals Department of Mathematics and Statistics Math 101 Section 03 Quiz II (Term 142)

1. If the function

$$f(x) = \begin{cases} ax+3 & \text{if } x \ge -1 \\ bx^2 - ax & \text{if } x < -1 \end{cases}$$

is differentiable on $(-\infty, \infty)$, then find the values of a and b.

2. Find the equation of the tangent line to the curve $y = x^3 - x^2$ at x = -1.

3. At time t > 0, the position of a particle moving along the s-axis is $s(t) = t^3 - 6t^2$. Find the acceleration of the particle when the velocity is zero.

4. If
$$f(x) = x^2 e^x$$
, then find $\lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$

5. If
$$y = \frac{x}{2 - \sqrt{x}}$$
, then find $\frac{dy}{dx}$ at $x = 9$.