

MATH 311 - Exam 3 - Term 141

Duration: 90 minutes

Student Name:

1. State without proof the following:
 - (a) Mean Value Theorem.
 - (b) Darboux's Theorem (Intermediate value property of derivatives)
2. Show that if $f : I \rightarrow \mathbb{R}$ is differentiable at $c \in \mathbb{R}$ then f is continuous at c .
3. Use Mean Value Theorem to show that for $x > 1$,

$$\frac{x-1}{x} < \ln x < x-1.$$

4. Prove that if $f \in \mathcal{R}[a, b]$, then f is bounded on $[a, b]$.
5. Prove that if $f : [a, b] \rightarrow \mathbb{R}$ is increasing on $[a, b]$, then $f \in \mathcal{R}[a, b]$.

Question Number	Points	Maximum Points
1		10
2		10
3		10
4		10
5		10
Total		50