

King Fahd University of Petroleum & Minerals
Department of Math and Stat
Math 132 Semester 141 - Exam 1

Name _____ ID No. _____

Points: Q1=2, Q2=3, Q3=2, Q4=4, Q5=2, Q6=2, Q7=2, Q8=1, Q9=2, Q10=3, Q11=2

1) Find the following limit. If it is $+\infty$ or $-\infty$ or does not exist, then say so.

$$\lim_{x \rightarrow 1^+} \frac{x-1}{x^2-2x+1}$$

2)

$$f(x) = \begin{cases} 2 - x^2 & \text{if } x > 1 \\ -2 + 3x & \text{if } 0 \leq x \leq 1 \\ 4 - x^2 & \text{if } x < 0 \end{cases}$$

Find

(a) $\lim_{x \rightarrow 1^+} f(x) =$

(b) $\lim_{x \rightarrow 1^-} f(x) =$

(c) $\lim_{x \rightarrow 0^-} f(x) =$

(d) $\lim_{x \rightarrow \infty} f(x) =$

(e) $\lim_{x \rightarrow -\infty} f(x) =$

3) If $y = \sqrt[3]{x^2 + 3x + 8}$, then find the rate of change of y with respect to x when $x=0$.

4)

$$\text{Let } f(x) = \begin{cases} \frac{1}{3+x} & \text{if } x \geq 0 \\ \frac{2}{5+x} & \text{if } x < 0 \end{cases}$$

Find all points where this function $f(x)$ is not continuous.

5) By direct use of the definition of a derivative, find $\frac{d}{dx}[f(x)]$ if $f(x) = \frac{1}{x+6}$.

6) Find all values of x for which the curve $y = 6x^2 + 4x - 5$ has slope 2.

7) If $y = \frac{x^2 + 1}{x + \ln x}$, then find $y'(1)$.

8)

Differentiate: $f(x) = e^{\frac{-2}{x^2}}$

9) Find y' if $\ln(xy) + y = 2$.

10) Use logarithmic differentiation to find $\frac{dy}{dx}$ from $y = (x^2 + x + 3)^{x^2 - 1}$.

11) If $y = (2x + 1)^{11}$, then find $y''(0)$.