SHOW ALL YOUR WORK. NO CREDITS FOR ANSWERS NOT SUPPORTED BY WORK.

- (1) (16 points) Consider the function $f(x) = \frac{1}{x} + \ln(x+2)$
 - 1. Find the domain of f(x).
 - 2. Find the critical numbers if any exists.
 - 3. Find increasing and decreasing intervals
 - 4. Find local extrema if any exists.
 - 5. Does the function have absolute extrema? Explain why.
- (2) (24 points) Find the limit if it exists

(a)
$$\lim_{x \to 1} \frac{x-1}{\ln x - \sin \pi x}$$

(b)
$$\lim_{x \to \infty} \left(1 + \frac{1}{x^2} \right)^x$$

(c)
$$\lim_{x \to \infty} \frac{\sqrt{x+2}}{\sqrt{x}+5}$$