

King Fahd University of Petroleum and Minerals  
Department of Mathematics and Statistics  
Math-302 Semester-133 QUIZ II

NAME:

S.No.

ID:

Maximum Marks: 10

Section:02

Time Allowed: 30 minutes

(1) Use the divergence theorem to compute  $\int \int_S \mathbf{F} \cdot \mathbf{n} ds$ , where  $\mathbf{F} = \langle y, x, z^2 \rangle$  and  $D$  is the region bounded by the paraboloid  $z = x^2 + y^2$  and the plane  $z = 1$ .

(2) Given a subset  $S$  of  $R^3$  defined by

$$S = \{u = (u_1, 0, u_3) | u_1 + u_3 \geq 0\}.$$

Is  $S$  a subspace? (Why?)

(3) Find the rank of the matrix

$$A = \begin{pmatrix} 6 & 1 & 3 & 8 \\ 4 & 2 & 6 & -1 \\ 10 & 3 & 9 & 7 \\ 16 & 4 & 12 & 15 \end{pmatrix}$$