

NAME: \_\_\_\_\_

ID: \_\_\_\_\_ Section: \_\_\_\_\_

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**Exercise 1** (5 points)

Let  $y_1 = x$  and  $y_2 = x^2$  be solutions of the homogeneous equations  $x^2 y'' - 2xy' + 2y = 0$ .

Solve the differential equation  $x^2 y'' - 2xy' + 2y = x^5$ .

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**Exercise 2** (5 points)

Find the eigenvalues and eigenvectors of the matrix  $\begin{pmatrix} 1 & -1 & 1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{pmatrix}$

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**Exercise 1** (5 points)

Find the eigenvalues and eigenvectors of the matrix  $\begin{pmatrix} 1 & 0 & 1 \\ -1 & 0 & 2 \\ 1 & 0 & 1 \end{pmatrix}$

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**Exercise 2** (5 points)

Let  $y_1 = x$  and  $y_2 = x^2$  be solutions of the homogeneous equations  $x^2 y'' - 2xy' + 2y = 0$ .

Solve the differential equation  $x^2 y'' - 2xy' + 2y = x^4$ .

