King Fahd University of Petroleum and Minerals Department of Mathematics and Statistics Math-301 Semester-132 QUIZ V

Maximum Marks: 10 Section:06 Time Allowed: 40 minutes (1) Use separation of variables method to solve the problem

$$a^2 \frac{\partial^2 u}{\partial x^2} = \frac{\partial^2 u}{\partial t^2} \quad 0 < x < \pi, t > 0$$
$$u(0,t) = 0, u(\pi,t) = 0, \quad t > 0$$
$$u(x,0) = 0, u_t|_{t=0} = \sin x, \quad 0 < x < \pi.$$

(2) Classify the PDE as hyperbolic, parabolic or elliptic

$$\frac{\partial^2 u}{\partial x^2} - \frac{\partial^2 u}{\partial x \partial y} - 3\frac{\partial^2 u}{\partial y^2} = 0.$$