King Fahd University of Petroleum and Minerals Department of Mathematics and Statistics Math-301 Semester-132 QUIZ II

NAME:

S.No. ID:

Maximum Marks: 10 Section:03 Time Allowed: 40 minutes (1) Show that $\mathbf{F}(\mathbf{x}, \mathbf{y}) = (xy + \cos y) \ \vec{i} + (\frac{1}{2}x^2 - x \sin y) \ \vec{j}$ is a conservative field and find its potential. Then, evaluate $\int_{(0,0)}^{(1,2)} \mathbf{F} d\mathbf{r}$. (2) Find a parametrization of the cylinder $x^2 + (y-3)^2 = 9; 0 \le z \le 5$. (3) Use Stokes theorem to compute the integral $\int \int_S Curl \mathbf{F} \cdot \mathbf{n} dS$, where $\mathbf{F}(\mathbf{x}, \mathbf{y}, \mathbf{z}) = \langle xz, yz, xy \rangle$ and S is the part of the sphere $x^2 + y^2 + z^2 = 4$ that lies inside the cylinder $x^2 + y^2 = 1$ and above the xy -plane.