

Full Name:

ID:

Q 1. Determine the order and state whether the following ODEs are linear or nonlinear (Give a brief justification).

a)  $\frac{d^2x}{dt^2} + (1 + \sqrt{x})\frac{dx}{dt} = \sin t$

b)  $x y''' + (1 - x)y' = e^x$

c)  $\frac{d^2u}{dr^2} + \sin(r) u \frac{du}{dr} = r^2$

d)  $y'^2 = \cos y$

Q 2.

a- Verify that  $y = \tan(x + C)$  is a one-parameter family of solutions of:  $y' = 1 + y^2$ .

b- Find a solution of  $y' - y^2 = 1$  such that, it is passing through the point  $(0, 1)$ .

Then find the largest interval of definition of the obtained solution.

Q 3. Find an explicit solution and the corresponding interval of definition of the IVP:

$$(\sqrt{x} + x)dy - (\sqrt{y} + y)dx = 0 \quad \text{with} \quad y(0) = 1.$$