

**Note: Show all your work. No credits for answers not supported by work.**

**Problem 1:** (25 points) Consider the function  $y = f(x) = 4x^2 - x^4$

- Find the critical numbers.
- Find intervals where the function is increasing and those where it is decreasing.
- Find the local maximum and minimum of the function.
- Discuss the concavity of the function and find the inflection points.
- Sketch the graph of the function. Clearly indicate the critical numbers, extrema and inflection points on the graph.

**Problem 2:** (10 points) Find all vertical and horizontal asymptotes of  $y = 1 + \frac{x}{1-x}$ .

**Problem 3:** (10 points) A rectangular portion of a field is to be enclosed by a fence and divided equally into two parts by a fence parallel to one pair of sides. If the total of 600 ft of fencing is to be used, find the dimensions that will maximize the fenced area, and **find this maximum area.**

**Problem 4:** (10 points) Use differentials to approximate  $e^{0.001}$ .

**Problem 5:** (10 points) Find the area enclosed by the graphs of  $y = (x-1)^2$  and  $y = x+1$ .

**Problem 6:** (35 points) Evaluate the integrals:

(a)  $\int_1^2 \frac{e^{\sqrt{x}} dx}{\sqrt{x}}$

(b)  $\int (x+1)e^x dx$

(c)  $\int \frac{1}{x \ln x} dx$

(d)  $D_x \left( \int_1^3 \sqrt{x^3 + x} dx \right)$

(e)  $\int 2\sqrt{10^{4x}} dx$