

Q1. Sketch a function that satisfies the following ;

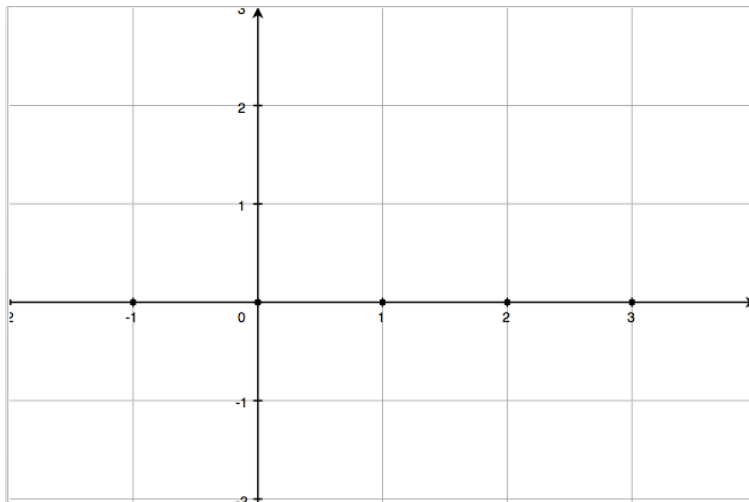
i. $\lim_{x \rightarrow \infty} f(x) = 0$

ii. $f(0) = f(1) = -1$

iii. $\lim_{x \rightarrow 0^+} f(x) = 1$

iv. $f(x)$ has a vertical asymptote, $x = 1$

v. $f(x)$ has a horizontal asymptote, $y = 2$



Q2. Find the equation of the horizontal asymptote(s) of $f(x) = \frac{\sqrt{x^2 + 1}}{\sqrt[3]{x^3 - 1}}$

Q3. Evaluate

i. $\lim_{x \rightarrow -\infty} (x^3 - x - 3)$

ii. $\lim_{x \rightarrow -\infty} (e^x + x)$

iii. $\lim_{x \rightarrow \infty} \frac{x^{-2} - x^{-1} + 1}{x^{-3} + x^{-1} - 1}$

iv. $\lim_{x \rightarrow -1^-} \left(\frac{x^4 + 2x}{x^2 - 1} \right)$