

Q1. Evaluate the limits

i. $\lim_{x \rightarrow \infty} \frac{3x^3 - 2x^2 + x}{x^3 + 1}$

ii. $\lim_{x \rightarrow 0} \frac{2^x - 1}{3^x - 4^x}$

iii. $\lim_{x \rightarrow \infty} \left(\frac{x}{2x + 1} \right)^x$

iv. $\lim_{x \rightarrow 0} (e^x + x)^{\frac{1}{x}}$

v. $\lim_{x \rightarrow \infty} \frac{5^x - 3^x}{5^x + 3^x}$

vi. $\lim_{x \rightarrow 0^+} (2^x - 1)^x$

Q2. Use Newton's Method to estimate the positive solution of $x^2 - 2 = 0$.

Start with $x_0 = 1$ and find x_2 .

Q3. Evaluate the indefinite integrals;

i. $\int (\sin(2x) - \cos(\pi)) dx$

ii. $\int \frac{1}{x} dx$

iii. $\int \left(\frac{1}{k^2 + x^2} \right) dx$

Q4. Find f if $f'' = e^{-x}$ and $f'(\ln 2) = -\frac{1}{2}$, $f(0) = 1$