

King Fahd University of Petroleum & Minerals

Department of Mathematics and Statistics

Semester II, 2012/2013 (122)

Math 513.02, Dr. Rajai S. Alassar

Homework Assignment No. 3

1. Find the Laplace transform of $f(t) = \begin{cases} -4 & \text{if } 0 \leq t < 1 \\ 0 & \text{if } 1 \leq t < 3 \\ e^{-t} & \text{if } t \geq 3 \end{cases}$.
2. Find the Laplace transform of $f(t) = (t^4 + 2t^2 + t)e^{-5t} \cos(3t)$.
3. Find the inverse Laplace transform of $F(s) = \frac{1}{s(s^2 + 16)} e^{-21s}$.
4. Solve the differential equation $y'' + 16y = 1 + t$; $y(0) = -2$; $y'(0) = 1$.
5. Solve the integral equation $f(t) = e^{-3t} \left[e^t - 3 \int_0^t f(x) e^{3x} dx \right]$