

King Fahd University Of Petroleum and Minerals  
College of Sciences  
Mathematics and Statistics Department  
Math 260-02  
Quiz#1

Name:..... ID#:..... Serial#:.....

1. Verify that  $y(x) = x^3(c + \ln x)$  satisfies the differential equation  $xy' - 3y = x^3$ . Then determine a value of the constant  $C$  so that  $y(x)$  satisfies the initial condition  $y(1) = 17$ .

2. Find values of  $r$  so that  $y = e^{rx}$  is a solution of the equation  $y'' + y' - 2y = 0$ .

3. Find the position function  $x(t)$  of a moving particle with the acceleration  $a(t) = \frac{1}{\sqrt{t+4}}$  and initial position  $x_0 = 1$  and initial velocity  $v_0 = -1$ .

4. Find all solutions of the differential equation  $\frac{dy}{dx} = 6x(y-1)^{\frac{2}{3}}$ .

5. Solve the following differential equations

(a)  $x^2y' = 1 - x^2 + y^2 - x^2y^2$

(b)  $y' = (1 - y) \cos x$

6. A certain city had a population of 25,000 in 1960 and a population of 30,000 in 1970. Assume that its population will continue to grow exponentially at a constant rate. What population can its city planners expect in the year 1980?