

**KING FAHD UNIVERSITY OF PETROLEUM & MINERALS
DEPARTMENT OF MATHEMATICAL SCIENCES
DHAHRAN, SAUDI ARABIA**

STAT 319: PROBABILITY & STATISTICS FOR ENGINEERS & SCIENTISTS

Major Examination No. 1, Term 121

Time: 18: 00- 19:30 PM, Tuesday, 25th October, 2012

Please Check/circle the name of your instructor; Write section number and serial number in the top left corner of this booklet or below:

Section # /Serial #

ID#

Name in Capital Letters:

Instructors: Anabosi
 Malik

Joarder

Coordinator: Anwar Joarder

You are allowed to use electronic calculators and other reasonable writing accessories that help write the exam. Try to define events, formulate problem and solve. See example below.

Do not keep your **mobile** with you during the exam, turn off your mobile and leave it aside.

| No | Marks | Marks Obtained | Strengths and Weakness Observed |
|-------|-------|----------------|---------------------------------|
| 1 | 11 | | |
| 2 | 4 | | |
| 3 | 7 | | |
| 4 | 3 | | |
| 5 | 5 | | |
| Total | 30 | | |

Kindly report grade out of 15 so that students know his precise standing. You may assign fractional marks if deemed necessary.

1. A national chain of automobile oil-change franchises claims, "your hood will be open for less than 12 min. when we service your car." To check their claim, times (in minutes), denoted by x , are recorded of oil-change service for 26 randomly selected customers. The times are shown in the table below:

| | | | | | | | | | | | | | |
|-----------------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| Customer number | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| Hood open time | 10.2 | 10.4 | 10.6 | 11.2 | 11.5 | 11.8 | 11.5 | 11.3 | 12.8 | 12.5 | 12.7 | 12.8 | 12.4 |
| Customer number | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 |
| Hood open time | 12.5 | 12.8 | 12.3 | 12.5 | 13.3 | 13.5 | 13.2 | 13.3 | 13.8 | 14.5 | 14.3 | 14.8 | 14.9 |

a. Complete the following table where f stands for frequency, F for cumulative frequency and n the sample size. (4 Marks)

| x | f | f/n | F | F/n |
|----------|-----|-------|---------|-------|
| [10, 11) | 3 | | 3 | |
| [11, 12) | 5 | | 8 | |
| [12, 13) | 9 | | 17 | |
| [13, 14) | 5 | | | |
| [14, 15) | | | | |
| Total | 26 | | No need | |

b. Is the variable discrete or continuous? (1 Mark)

c. Calculate the mean, median and mode of the time hood is open. (6 Marks)

2. As a result of government and consumer pressure, automobile manufacturers in the US are deeply involved in research to improve their product's gasoline mileage. One manufacturer hoping to achieve 40 miles per gallon on one of its compact models, measured the mileage (x_i) obtained by 11 test versions of the model with the following results:

| | | | | | |
|----|----|----|----|----|----|
| 30 | 31 | 32 | 33 | 34 | 35 |
| 36 | 37 | 38 | 39 | 40 | |

Complete the following table:

| x_i | \bar{x} | $x_i - \bar{x}$ | $(x_i - \bar{x})^2$ |
|-------|-----------|-----------------|---------------------|
| 30 | | | |
| 31 | | | |
| 32 | | | |
| 33 | | | |
| 34 | | | |
| 35 | | | |
| 36 | | | |
| 37 | | | |
| 38 | | | |
| 39 | | | |
| 40 | | | |

a. Calculate $\sum_{i=1}^{11} (x_i - \bar{x})$. (2 Marks)

b. Calculate $s_{xx} = \sum_{i=1}^{11} (x_i - \bar{x})^2$. (2 Marks)

3. Suppose that of all individuals buying a certain personal computer, 60% include a word processing (W) program in their purchase, 40% include a spreadsheet (S) program, and 30% include both types of programs. We are interested in knowing the inclusion of the programs.

a. Write out the sample space for the problem. (1 Mark)

b. Find the probability that a word processing program was included given that the selected individual was included a spreadsheet program. (3 Marks)

c. Are the vents "word processing program was included" (A) and the event "selected individual was included a spreadsheet program" (B) independent? (3 Marks)

4. A box contains 6 pens of which 4 are dried.

a. Two pens are selected one after another without replacement. What is the probability that one of them is dried and one has ink? (2 Marks)

b. The pens are selected at random one by one until a good pen is selected. The sequence of test results is noted. What is the sample space? (1 Mark)

5. A chemical engineer keeps repeating an experiment unless he gets the desired result (S) with the restriction that the lab supervisor allows him to repeat the experiments a maximum of 3 times. It is estimated that the probability of getting the desired result in any experiment at a time is 0.75.

- a. Write out the sample space? (2 Marks)
- b. What is the probability that he repeats the experiment 3 times? (3 Marks)