

Write clearly, explain and simplify your answers

---

1. [7pts] Let  $f(x) = \begin{cases} 1 + 2x & \text{if } x < 1 \\ x^2 + 2 & \text{if } x > 1 \end{cases}$ .

Find  $\lim_{x \rightarrow 2} f(x)$ ,  $\lim_{x \rightarrow 1^+} f(x)$ ,  $\lim_{x \rightarrow 1^-} f(x)$ ,  $\lim_{x \rightarrow 1} f(x)$ ,  $\lim_{x \rightarrow \infty} f(x)$ ,  $\lim_{x \rightarrow -\infty} f(x)$ . Is  $f$  continuous at  $x = 1$ ?

2. [6pts] Find, if they exist:

(a)  $\lim_{x \rightarrow 2} \frac{x^2 + 3x - 10}{x^2 - 6x + 8}$

(b)  $\lim_{x \rightarrow -\infty} \frac{x(3 - x^2)}{x^3 + x + 1}$

**3. [6pts]** Let  $y = x^2 + 3x - 4$ . Find

(a) The rate of change of  $y$  w.r.t.  $x$  when  $x = 3$

(b) The relative rate of change and the percentage rate of change when  $x = 3$ .

**4. [4pts]** The total cost function for a manufacturer is  $c = \frac{(q + 1)^2}{q + 2} + 600$ . Find the marginal cost function.

5. [6pts] A manufacturer has determined that that  $m$

6. [4pts] Find an equation of the tangent line to the curve  $y = x(\ln(x) - 1)$  when  $x = e^2$ .

7. [4pts] Find  $f'(1)$  if  $f(t) = 5^{2t^2+2t-3}$ .

8. [4pts] Find  $y'$  if  $e^y = (y + 1)e^x$ .