King Fahd University of Petroleum and Minerals Department of Mathematics and Statistics

MATH 131 // Major Exam II (121) Instructor: Bilal Chanane

ID: Name:..... Section:....

Exercise #1: (12 pts) Solve the following linear system using Gauss elimination

 $\begin{cases} 2x - 2y - z = 1\\ x - y + 3z = -2\\ x + y + 2z = 3 \end{cases}$

Exercise #2: (15 pts) Solve, using the simplex method (only), the linear programming problem,

Maximize
$$z = x + y$$

subject to
$$\begin{cases} x + y \le 1\\ 2x + 5y \le 3\\ x \le 5/6\\ x, y \ge 0 \end{cases}$$

Exercise #3: (10 pts) Find the dual of the linear programming problem,

Minimize
$$z = x_1 + 2x_2 + 5x_3$$

subject to
$$\begin{cases} x_1 - x_2 + 2x_3 \ge 2\\ -x_1 + 2x_2 + x_3 \ge 3\\ x_1, x_2, x_3 \ge 0 \end{cases}$$

(Do not solve the resulting system).

Exercise #4: (8 pts) John borrows \$2000 on November 20, 2012 with a simple interest rate of 5%.

- (i) What amount must be paid back on November 20, 2013?
- (ii) What is the value of the loan on November 20, 2013?
- (iii) What is the interest on the loan ?

Exercise #5: (15 pts) Which is better investment

(i) 8% compounded monthly

(ii) 8.8% compounded continuously

(iii) 8.6% compounded semi-annually ?

Exercise #6: (10 pts) Find the present value of the following ordinary annuities:

1750 per month for 5 years at 7.3% compounded monthly.

Exercise #7: (12 pts) A debt of \$12000 due 9 years from now, is instead to be paid of by 3 payments: \$2000 now, \$2000 in 4 years, and a final payment at the end of 9 years. What would this payment be if an interest rate of 6% compounded annually is assumed?

Exercise #8: (18 pts) David invested \$70000, a portion earning a simple interest rate at 6% per year and the rest earning an interest of 8.2% per year. After one year the total interest earned on these investments was \$5021. How much money did he invest at each rate?