King Fahd University of Petroleum & Minerals Department of Mathematics and Statistics Course Syllabus MATH 536 [Functional Analysis II] Semester II---2011-2012(112) (Course Instructor: A.R. Khan)

Textbook: E. Kreyszig, *Introductory Functional Analysis with Applications*, John Wiley & Sons, 1989.

References: i. A.L.Brown and A.Page, Elements of Functional Analysis, Von Nostrand Reinhold, 1970.

ii. C. Groetsch, Elements of Applicable Functional Analysis, Marcel

Dekker, 1980.

iii. E.S.Suhubi, Functional Analysis, Kluwer Academic Publishers, 2003.

Goals: The main objective of this course is to familiarize our students with somewhat advanced concepts of functional analysis in Hilbert spaces and normed (Banach) spaces. The existence of adjoint of a bouned linear operator on a Hilbert space will be established and will be used to define certain classes of operators such as self-adjoint operators, normal operators and unitary operators. Some results about compact operators, projections and weak* convergence will be discussed in the context of a normed space. The spectral theory of some bounded linear operators on normed spaces and Hilbert spaces will be presented.

Catalogue Description:

Algebra of bounded operators, self-adjoint operators in Hilbert Spaces,
Normal operators, compact operators, projections, spectral theory of
linear operators in normed spaces and Hilbert spaces, spectral mapping
theorem, Banach-Alaoglu theorem.

Week	Date	Material
1-2	Jan 28- Feb 8	Review of basic concepts
		Orthonormal sets in Hilbert spaces
3	Feb 11-15	Algebra of bounded linear operators
4-5	Feb 18-29	Self –adjoint operators in Hilbert spaces
		Normal operators
6	Mar 3-7	Unitary operators, Positive operators
7	Mar10-14	Weak and weak* convergence in normed spaces
		Banach- Alaoglu theorem
8	Mar 17-21	Projections
March 24, 2012 – March 28, 2012: Midterm Vacation		
9-10	Mar 31-Apr 11	Compact operators
11-12	Apr 14-25	Spectral theory of linear operators in Hilbert spaces
13-14	Apr 28-May 9	Spectral theory of linear operators in normed spaces
15	May12-16	Spectral mapping theorem

• KFUPM attendance policy will be enforced.

• **Evaluation Policy:** Exams I & II: 22% each; Final exam (comprehensive): 36%, Presentation & Assignments: 20%.