

Sec. 10.4] Tests Concerning Means

TABLE 10.1  
Tests Concerning Means

$H_0$	Value of Test Statistic	$H_1$	Critical Region
$\mu = \mu_0$	$z = \frac{\bar{x} - \mu_0}{\sigma/\sqrt{n}}$ ; $\sigma$ known or $n \geq 30$	$\mu < \mu_0$ $\mu > \mu_0$ $\mu \neq \mu_0$	$z < -z_{\alpha}$ $z > z_{\alpha}$ $z < -z_{\alpha/2}$ and $z > z_{\alpha/2}$
$\mu = \mu_0$	$t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}$ ; $v = n - 1$ , $\sigma$ unknown and $n < 30$	$\mu < \mu_0$ $\mu > \mu_0$ $\mu \neq \mu_0$	$t < -t_{\alpha}$ $t > t_{\alpha}$ $t < -t_{\alpha/2}$ and $t > t_{\alpha/2}$
$\mu_1 - \mu_2 = d_0$	$z = \frac{(\bar{x}_1 - \bar{x}_2) - d_0}{\sqrt{(\sigma_1^2/n_1) + (\sigma_2^2/n_2)}}$ ; $\sigma_1$ and $\sigma_2$ known	$\mu_1 - \mu_2 < d_0$ $\mu_1 - \mu_2 > d_0$ $\mu_1 - \mu_2 \neq d_0$	$z < -z_{\alpha}$ $z > z_{\alpha}$ $z < -z_{\alpha/2}$ and $z > z_{\alpha/2}$
$\mu_1 - \mu_2 = d_0$	$t = \frac{(\bar{x}_1 - \bar{x}_2) - d_0}{s_p \sqrt{(1/n_1) + (1/n_2)}}$ ; $v = n_1 + n_2 - 2$ , $\sigma_1 = \sigma_2$ but unknown; $s_p^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}$	$\mu_1 - \mu_2 < d_0$ $\mu_1 - \mu_2 > d_0$ $\mu_1 - \mu_2 \neq d_0$	$t < -t_{\alpha}$ $t > t_{\alpha}$ $t < -t_{\alpha/2}$ and $t > t_{\alpha/2}$
$\mu_1 - \mu_2 = d_0$	$t' = \frac{\bar{x}_1 - \bar{x}_2 - d_0}{\sqrt{(s_1^2/n_1) + (s_2^2/n_2)}}$ ; $v = \frac{(s_1^2/n_1 + s_2^2/n_2)^2}{(s_1^2/n_1)^2 + (s_2^2/n_2)^2}$ ; $n_1 - 1$ , $n_2 - 1$ ; $\sigma_1 \neq \sigma_2$ and unknown	$\mu_1 - \mu_2 < d_0$ $\mu_1 - \mu_2 > d_0$ $\mu_1 - \mu_2 \neq d_0$	$t' < -t_{\alpha}$ $t' > t_{\alpha}$ $t' < -t_{\alpha/2}$ and $t' > t_{\alpha/2}$
$\mu_D = d_0$	$t = \frac{\bar{d} - d_0}{s_d/\sqrt{n}}$ ; $v = n - 1$ , paired observations	$\mu_D < d_0$ $\mu_D > d_0$ $\mu_D \neq d_0$	$t < -t_{\alpha}$ $t > t_{\alpha}$ $t < -t_{\alpha/2}$ and $t > t_{\alpha/2}$

hypotheses. [Ch. 10

if  $\mu = \mu_0$ ; otherwise  $\mu \neq \mu_0$ . The

effort to finding a  $\mu_0$  lies in the alternative hypothesis, the construction of the

Chapter 9 to construct the difference  $z$  or  $t$  value to test an appropriate hypothesis. This is described in Chapter 9. This can refer to the

to test specified critical regions of these tests are

developed a new strength of 8 kilograms if a mean breaking

Section 10.3, we